

# MACHINES-2

# NOTES

(Modified)

# Working Model of Generator:

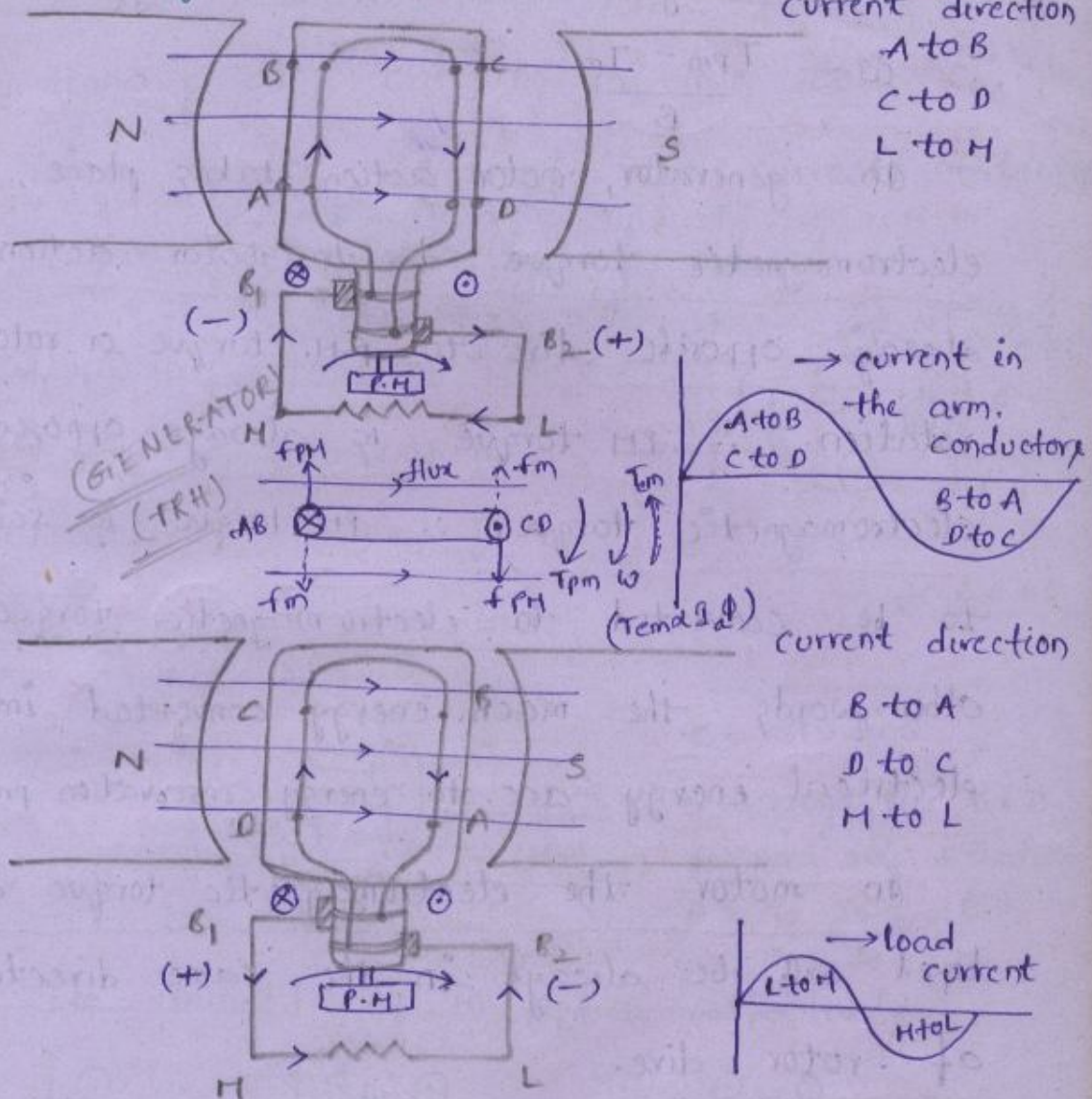
25/07/08

current direction

A to B

C to D

L to M



The induced emf in 2 sides of the coil will be in aiding polarity, i.e. they are said to be in phase.

- \* Fleming's Left Hand Rule  $\rightarrow$  Motor
- \* Fleming's Right Hand Rule  $\rightarrow$  Generator

$$P_{\text{mech}} = T_{\text{pm}} \cdot \omega$$

$$P_{\text{ele}} = T_m \cdot \omega$$

$$T_{\text{pm}} = J \frac{d\omega}{dt} + B \cdot \omega + T_{\text{em}}$$

$\downarrow$  Inertia torque       $\downarrow$  frictional torque

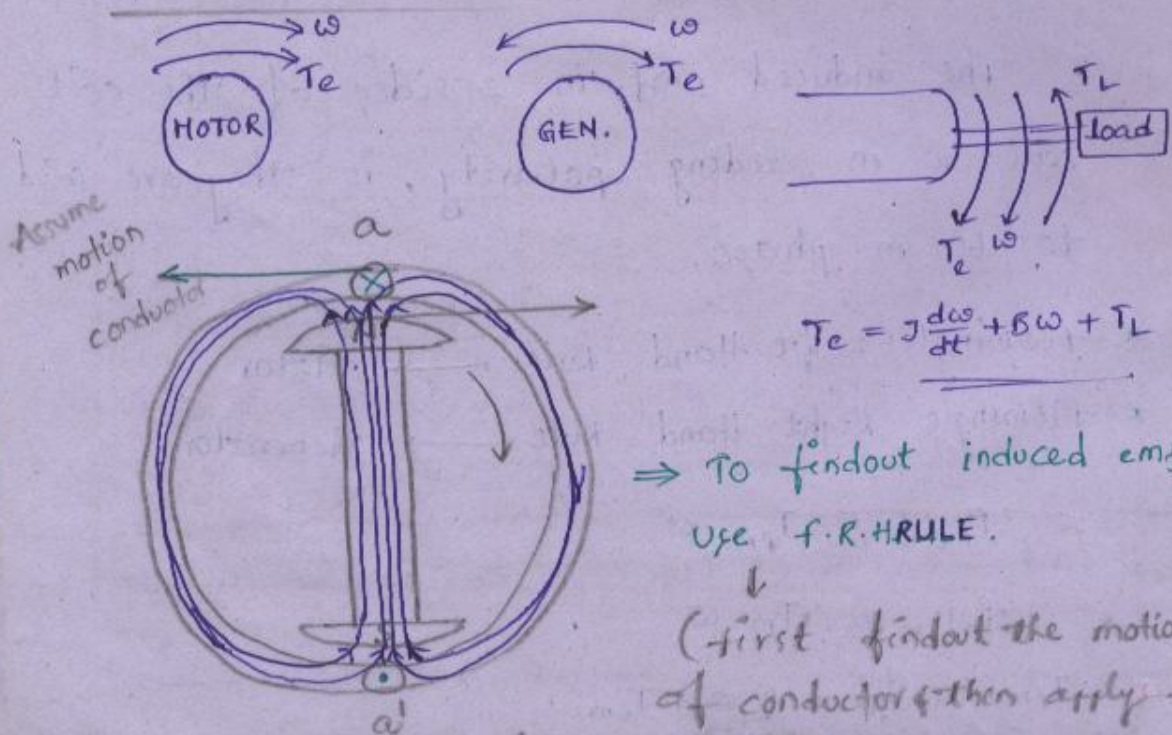


Under steady state condition,  $J \frac{d\omega}{dt} = 0$ .

$$\therefore \omega = \frac{T_{pm} - T_m}{B}$$

In generator, motor action takes place, the electromagnetic torque due to motor action is always opposite dir. to p.m. torque or rotor rotation.  $\therefore$  PM torque is always opposed by electromagnetic torque.  $\therefore$  PM torque is said to be converted to electromagnetic torque. In other words, the mech. energy converted into electrical energy acc. to energy conservation principle.

In motor the electromagnetic torque developed will be always in the same direction of rotor dir.



$$T_e = J \frac{d\omega}{dt} + B\omega + T_L$$

$\Rightarrow$  To find out induced emf  
Use F.R.H. RULE.

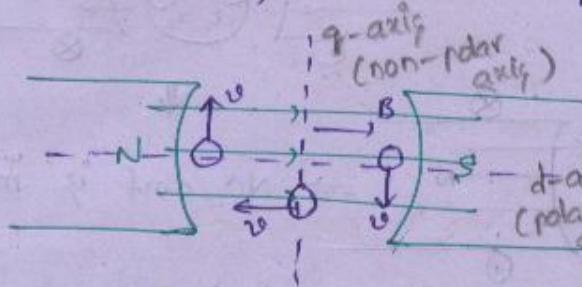
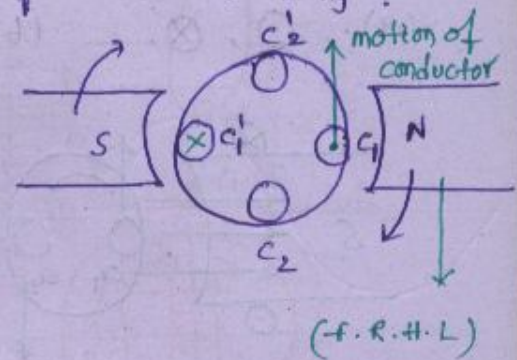
$\downarrow$   
(first find out the motion of conductor then apply)

If rotor dir. is given, then the



Q. Two magnetic poles revolving around stationary arm. carrying the two coils  $c_1, c_1'$  and  $c_2, c_2'$ . Identify the correct statement regarding to polarity of induced emf.

- (a).  $\odot$  in  $c_1$ , no emf in  $c_2$   
 (b).  $\otimes$  in  $c_1$ , no emf in  $c_2$   
 (c).  $\odot$  in  $c_2$ , no emf in  $c_1$   
 (d).  $\otimes$  in  $c_2$ , no emf in  $c_1$



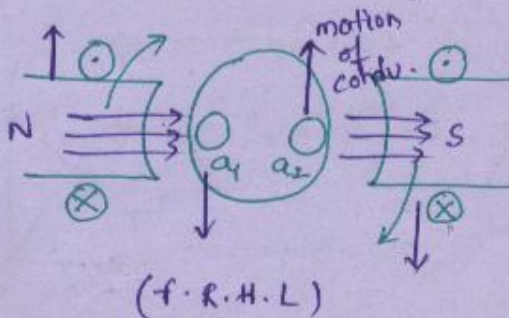
$$e = Blv \sin \theta$$

$\theta \rightarrow$  angle b/w  $B$  &  $v$

\* In polar axis situation,  $\theta = 90^\circ$  so  $e = Blv$

In non-polar region  $\theta = 0^\circ$  so  $e = 0$ .

Q. The induced emf in  $a_1$  &  $a_2$  respectively,



- (a).  $\odot, \otimes$   
 (b).  $\otimes, \odot$   
 (c). no emf  
 (d). data insufficient

Right hand thumb rule: (in case of coil)

If wrapped fingers represent dire. of current, then thumb represents dire. of flux.

(conductor dire. is opposite to the dire. of rotation of the rotor.)

\* Into the paper  $\Rightarrow \otimes$  ; out from the paper  $\Rightarrow \odot$

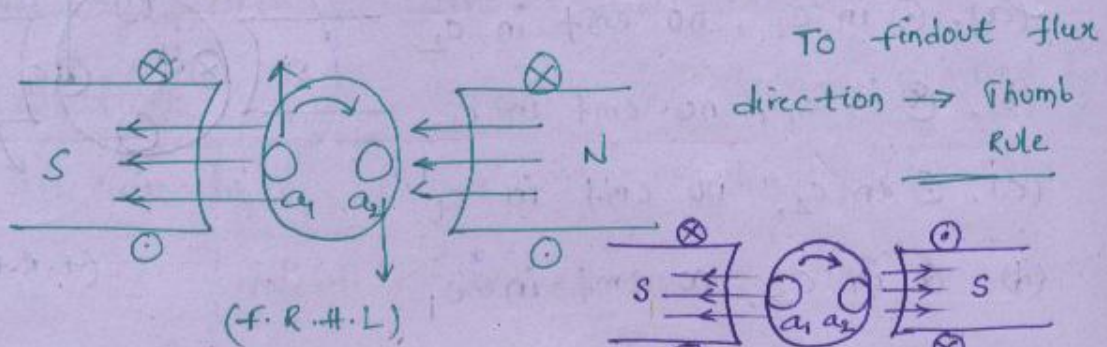


Q.

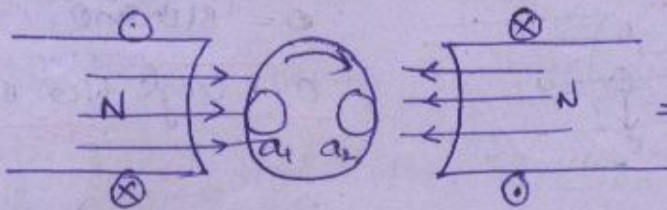


The induced emf's in  $a_1, a_2$  respectively

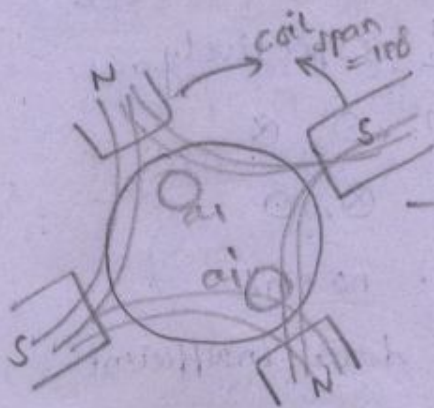
(a).  $\odot, \otimes$  (b).  $\otimes, \odot$  (c). No emf



Q.



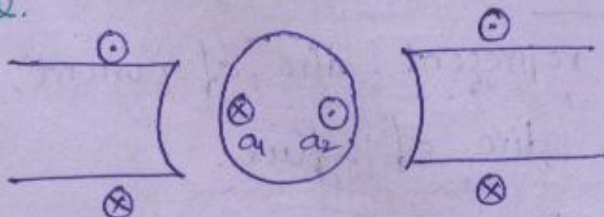
$\Rightarrow$  No emf is induced



Never be coil span  $> 180$

$\rightarrow$  Here coil span =  $360$ .

Q.



The direction of Torque in the above fig-?

(a) cw (b) ccw (c). No torque.



Induced emf  $\Rightarrow$  FRH rule

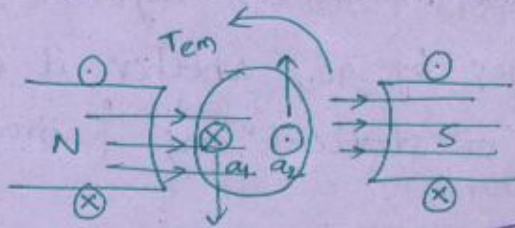
Torque  $\Rightarrow$  FLH rule

flux & current  $\Rightarrow$  Thumb rule

Thumb Rule

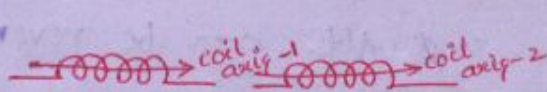
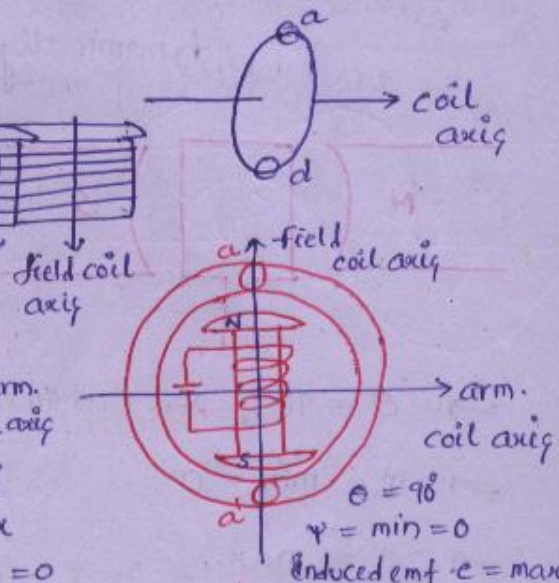
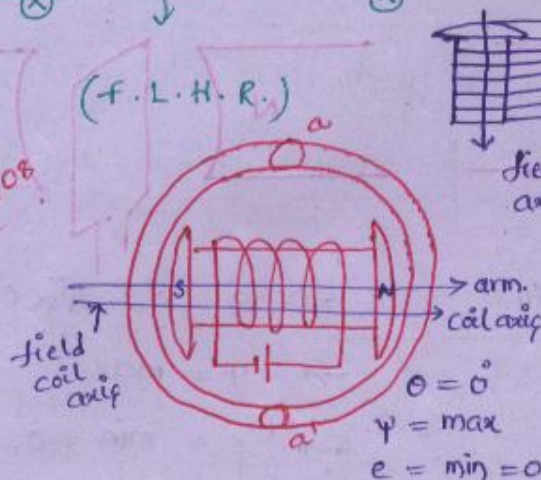
In case of st. conductor:

Thumb  $\rightarrow$  current  
wrapped fingers  $\rightarrow$  flux



(F.L.H.R.)

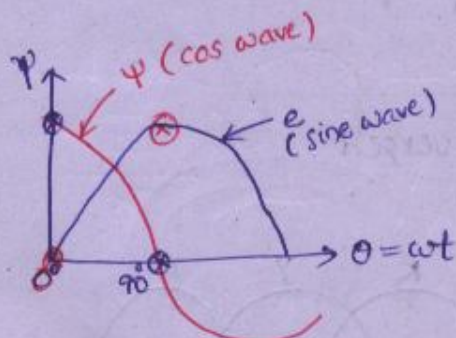
MON.  
04/08/08



In this  $\theta = 0^\circ$   
so flux linkages max.



$\theta = 90^\circ$   
so the flux linkages min



$$\psi \propto \cos \theta \Rightarrow \psi = \phi \cos \theta$$

$$= \phi \cos \omega t \quad \text{--- (1)}$$

$$e = -T \cdot \frac{d\psi}{dt}$$

$$= -T \cdot \frac{d}{dt} (\phi \cos \omega t)$$

$$= T \phi \omega \sin \omega t$$

$$= 2\pi f \phi T \sin \omega t$$

$$= E_{\max} \sin \omega t \quad \text{--- (2)}$$

$$= E_{\max} \cos(\omega t - 90^\circ) \quad \text{--- (3)}$$

$$E_{\max} = 2\pi f \phi T$$

$$\Rightarrow E_{\text{rms}} = \frac{E_{\max}}{\sqrt{2}}$$

$$= \frac{\sqrt{2}}{2} 2\pi f \phi T$$

$$= 4.44 \phi f T$$

$\Rightarrow E = 4.44 \phi f T \rightarrow$  emf eq. of an alternator for a full pitch, concentrated wdg.



$E = 4.44 k_p k_d \phi f T \Rightarrow$  emf eq. of an alternator for short pitch, distributed wdg.

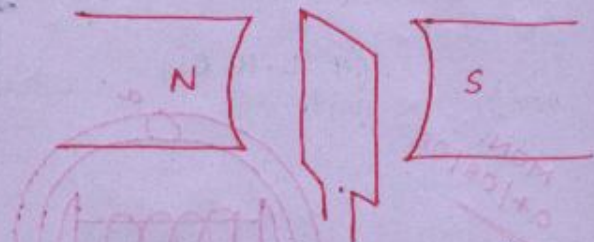
The ~~xxxx~~ induced emf lags the flux flux linkages by  $90^\circ$ , whether it is dynamically or statical <sup>induced</sup> emf. [ $\therefore$  from ① & ③]



$$\Rightarrow \theta = 90^\circ, \psi \propto \cos 90^\circ$$

$$\Rightarrow \psi = \min = 0$$

$$\Rightarrow e = \max$$



$$\Rightarrow \theta = 0^\circ, \psi \propto \cos 0^\circ$$

$$\Rightarrow \psi = \max$$

$$\Rightarrow e = \min = 0$$

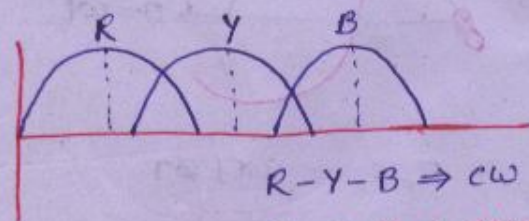
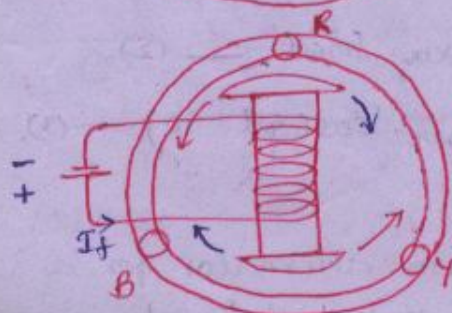
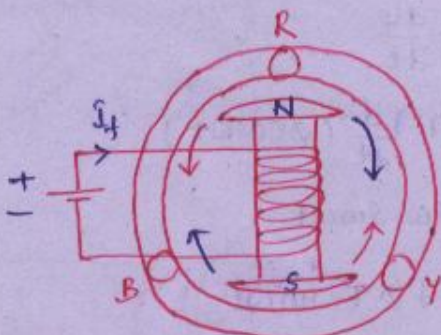
Q. 1 The ph. sequence of 3- $\phi$  Alt. can be reversed

(a). by changing field polarities

(b). by changing the dire. of field rotation.

(c). both (a) & (b)

(d). ph. sequence can't be reversed.



$$\Rightarrow R-Y-B \Rightarrow \text{CW}$$

$$\Rightarrow B - [R-Y-B] \Rightarrow R-Y-B \Rightarrow \text{CW}$$

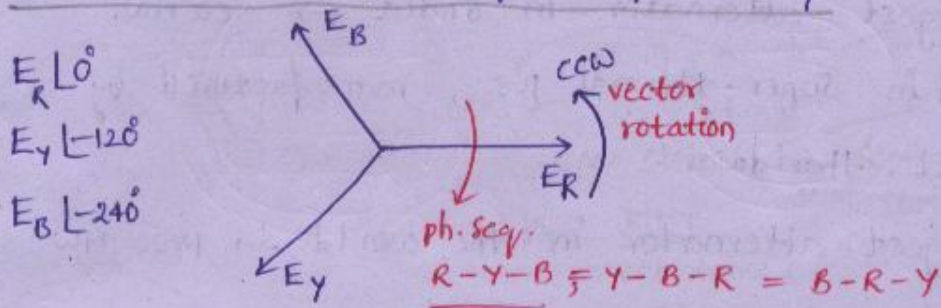
$$\Rightarrow Y - [R-B-Y] \Rightarrow R-B-Y \Rightarrow \text{CCW}$$



\* ph. sequence (or) ph. order :

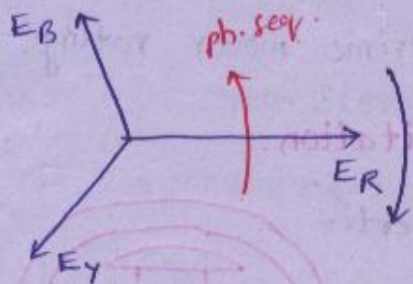
It is the order at which the max. value of induced emf (or) current obtained.

\* The ph. sequence of 3- $\phi$  Alt. can be reversed by changing the rotor rotation [ either field may be rotating or arm. may be rotating ]. The ph. seq. does not depend upon field polarities.



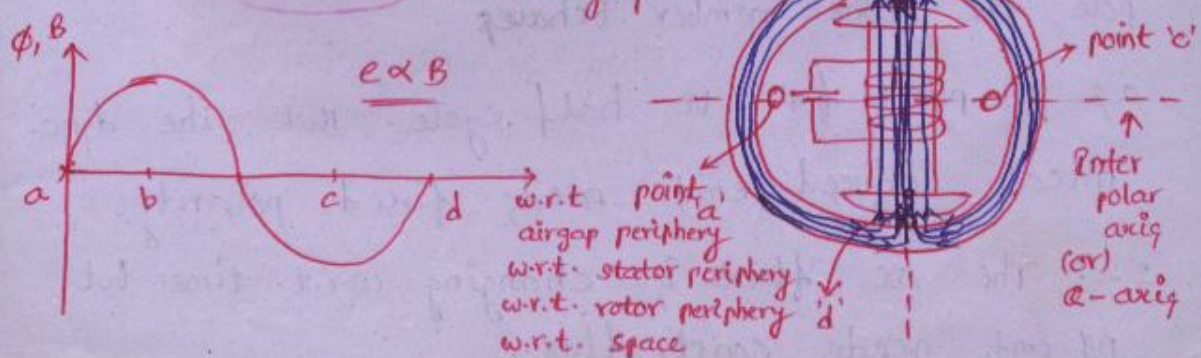
Q. The ph. seq. of the following 3- $\phi$  system is \*

(a). R-Y-B (b). R-B-Y (c). zero seq. (d). None



\* ph. seq. can be always verified in the opp. dir. of vector rotation.

flux Distribution in Airgap :-





\* flux distribution in air gap is assumed to be sinusoidal and always m/c's are designed to obtain the sinusoidal flux dist. If flux distr is sinusoidal then the induced emf also sinusoidal.

∴ The main reason for the production of harmonics is non-sinusoidal flux distr. in the air gap.

\* Largest alternator in India → 500 MW used in super thermal p.s., manufactured by BHEL, Haridwar.

\* Largest alternator in the world → 1700 MW West Germany

\* The rating of an alt. represented by kVA, kW or kw such that active power must be known for the selection of prime mover rating.

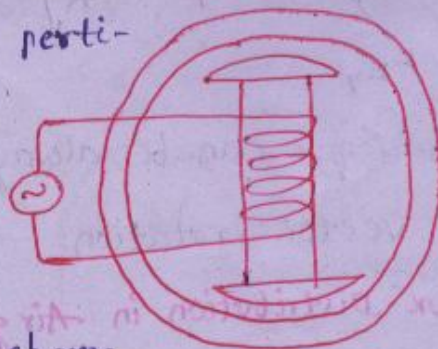
TUE. 05/03/08 **Effect of AC Excitation:**

1. The polarity of a particular pole is not fixed.

for +ve half cycle a member acting as a N pole the same member behaves

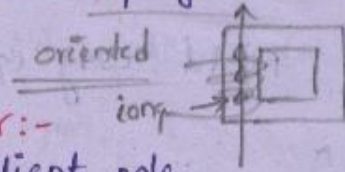
as S-pole for -ve half cycle. But the dynamical induced emf needs fixed polarity.

2. The ac flux is changing w.r.t. time but an emf needs const. flux.





→ The avg. torque in the m/c is zero, so no generated voltage.

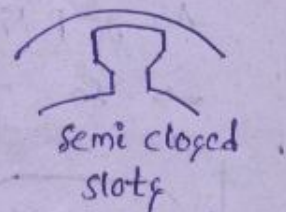
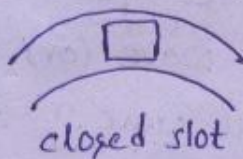
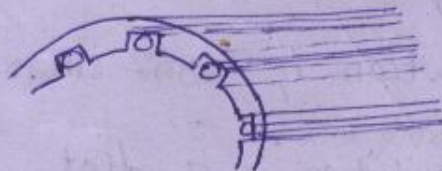


### \* Construction of Alternator:-

1. stator
2. Rotor — salient pole  
Non-salient (or) Round

↓  
cold rolled Non-oriented steel with 3% silicon (ie Si steel) and laminated to reduce eddy current losses.

← due to the circular construction. (or) cylindrical. Go introduce some resistance to reduce eddy current.



$$\downarrow \phi_l = \frac{MMF}{\text{reluctance} \uparrow}$$

$$\Rightarrow \downarrow L = \frac{N\phi}{i}, \quad X_L \downarrow$$

$$\text{stability} \propto \frac{1}{X_s} \rightarrow (X_s = X_L + X_a)$$

$$\Rightarrow \uparrow \text{stability} \propto \frac{1}{X_L \downarrow}$$

### \* Adv-s of open slots:

→ The access of wdg is easy. (placement & replacement)

→ leakage flux is reduced ie  $L \downarrow \Rightarrow X_L \downarrow$

∴ stability is improved and also regulation is improved

$X_L \downarrow \Rightarrow \text{reg. is better.}$

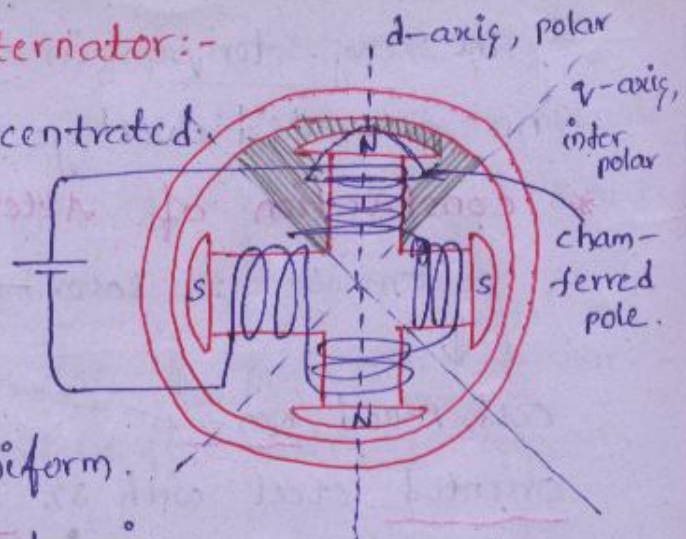


## ⇒ Salient pole Alternator:-

→ field wdg is concentrated.

↺ ccw → N-pole

↻ cw → S-pole

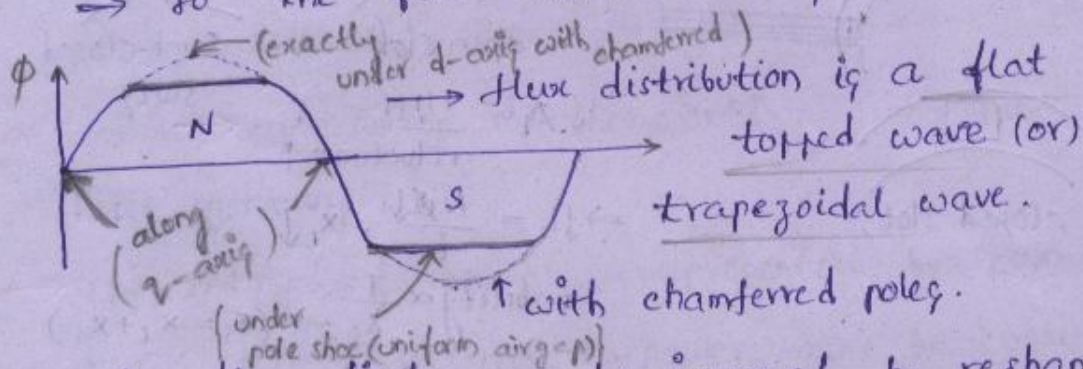


→ Air gap is non-uniform.

Air gap is min → d-axis

Air gap is max → q-axis

→ so the flux distribution is non-sinusoidal



The flux distr. can be improved by reshaping the salient poles such that having min air gap along pole centre and increases along pole ends, this poles are said to be chamfered poles.

\* The air gap length under the pole shoe  $\propto \frac{1}{\cos \theta}$

where  $\theta$  is in electrical degrees measured from pole centre.

→ Due to projecting nature & concentrated wdg, these rotor is not mechanically balanced well. If these



$$\theta = 0 \Rightarrow A \cdot G \propto \frac{1}{\cos 0} = 1 \text{ mm}$$

$$\theta = 60 \Rightarrow A \cdot G \propto \frac{1}{\cos 60} = 2 \text{ mm}$$



rotor driven with high speeds, centrifugal forces are developed, so speeds are restricted.

→ speed ranges: 50 - 1000 rpm

Low speed alternator.

→ No. of poles: 120 - 6

→ power  $\propto$  volume of the rotor

⇒  $P \propto D^2 L$ , D - Diameter of rotor  
L - Rotor axial length.

→ Larger diameter, smaller axial length.

⇒ If the rotor diameter increases, stator dia. also increased, so more no. of slots, more no. of arm. conductors can be accommodated, so they need not to be lengthy. (axial length).

→ Prime movers are: Hydro turbines & Diesel Engines  
So salient pole alternators are used in hydro P.S. & Diesel P.S.

→ Hydro Alternators (Since used in hydro P.S.)

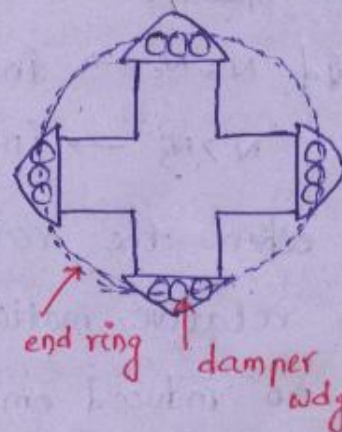
Damper winding:

for Alternator:

- To eliminate Hunting
- To suppress the -ve sequence field

for Syn. motor:

- To eliminate Hunting
- for starting purpose.



{ Hunting occurs only in }  
Syn. m/c's.



→ Causes for Hunting:-

1. Sudden change in load.
2. Sudden change in supply system.
3. Sudden change in excitation system.
4. Load containing harmonic torques.

→ To reduce Hunting: (To eliminate)

1. By using flywheel.
2. By designing the m/c such that having suitable synchronizing power coe.
3. By using damper wdg.

WED.  
13/09/08

→ Damper wdg is short circuited by the end rings.

→ Damper wdg is made with low resistance Cu, Al, brass.

→ w.r.t. damper wdg, rotor behaves as squirrel cage rotor of IM  $\therefore$  Induction m/c action comes into picture, when the speed is other than syn. speed.

$\Rightarrow$  If  $N < N_s \rightarrow$  Induction motor action  $\rightarrow T_d$  (I.M.)

$N > N_s \rightarrow$  Induction generator action  $\rightarrow T_d$  (I.G.)

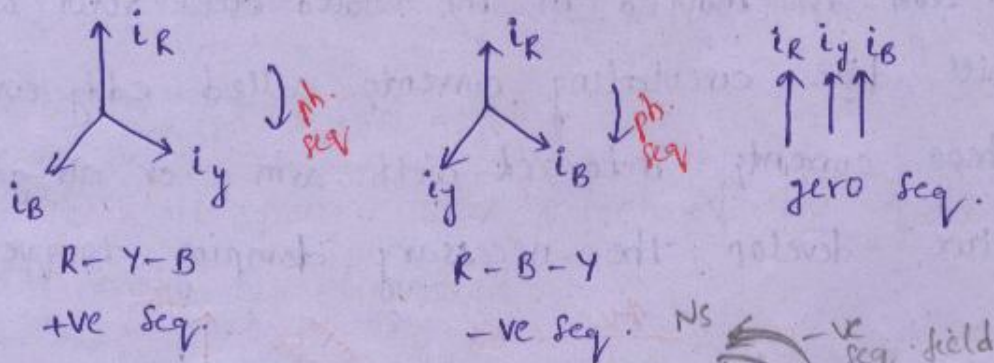
→ when the rotor rotating with  $N_s$ , there is no relative motion b/w arm flux & damper wdg. so no induced emf & no current and hence no damping torque. so the m/c is running at steady state condi.



→ If  $N < N_s$ , induction motor torque in the same dir. of rotor rotation will develop due to which rotor accelerates and finally reaches to  $N_s$ .

→ When the rotor speed is more than  $N_s$ , induction generator torque in the opp. dir. to rotor will develop due to which rotor decelerates and finally reaches to  $N_s$ .

→ The fun. of the damper wdg. is transient in nature, when the disturbance occurs the damping torque comes into picture to maintain <sup>n/m</sup> synchro once the disturbance clear,  $T_d$  reduces to zero.



→ The relative motion b/w -ve seq. field & damper wdg =  $2N_s$ . Due to this an emf is induced, currents hence damping flux is produced in such a dir. to suppress the -ve seq. field acc. to. Lenz's law i.e. always the effect opposes the cause producing it.  $\therefore$  -ve seq. field is opposed by the damping flux



Such that -ve seq. field is suppressed

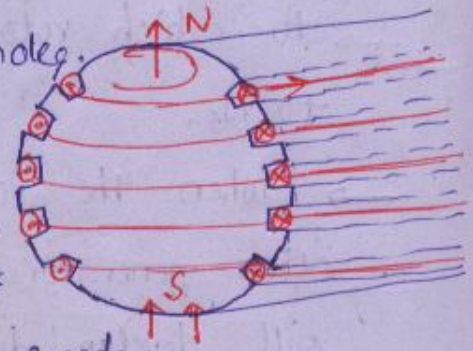
⇒ **Cylindrical rotor Alternator:-**

→ Unslotted area forms the poles.

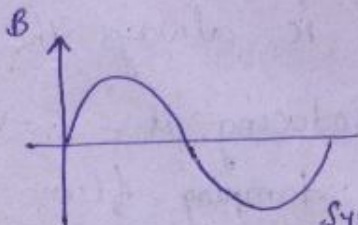
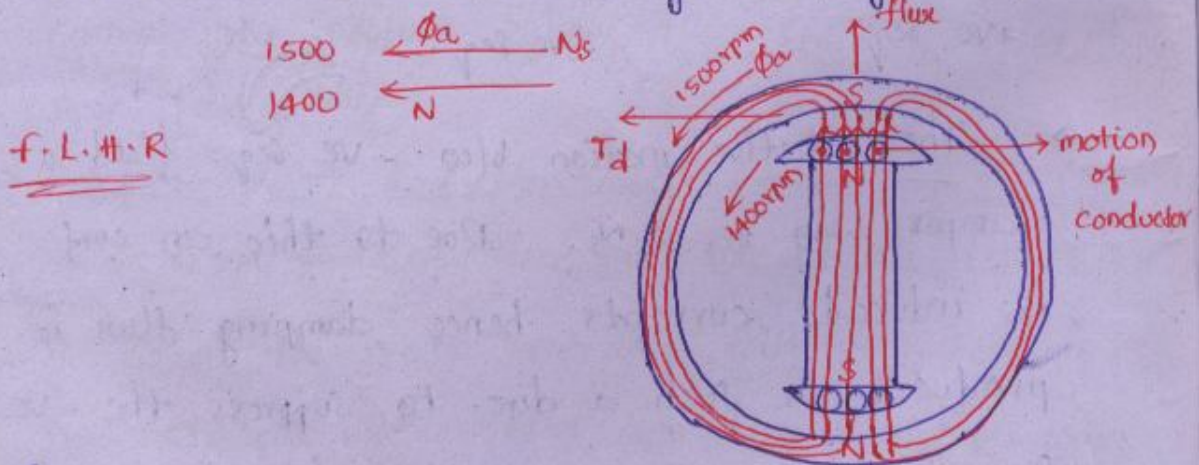
→ The rotor is mech. strong and field wdg also more rigid so these type of rotors

can allow to rotate at high speeds

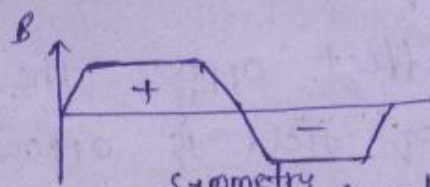
such that it can withstand for high centrifugal forces developed.



→ NO damper wdgs, b'coz hunting is less pronounced though we can eliminate with eddy current damping. When rotor speed is other than  $N_s$ , an emf is induced in the solid steel rotor which will drive circulating currents called eddy currents, these currents interact with arm  $\phi$  or air gap flux, develop the necessary damping torque.



Symmetry  
(even harmonics = 0)



Symmetry (even harmonics = 0)



SAT.  
16/08/08

Q. The coil span to eliminate 7th harmonic is - ?

- (a).  $\frac{5}{6} \times \text{pole pitch}$  (b).  $\frac{6}{5} \times \text{pole pitch}$   
 (c).  $\frac{6}{7} \times \text{pole pitch}$  (d).  $\frac{7}{6} \times \text{pole pitch}$

$$\beta = 180 \left( \frac{n-1}{n} \right)$$

$$= 180 \left( \frac{7-1}{7} \right)$$

$$= \frac{6}{7} \times 180 = \frac{6}{7} \times \text{pole pitch}$$

Q. To eliminate both 5th & 7th harmonics, the coil span is - ?

- (a).  $\frac{4}{5} \times \text{pole pitch}$  (b).  $\frac{5}{6} \times \text{pole pitch}$   
 (c).  $\frac{6}{7} \times \text{pole pitch}$  (d).  $\frac{7}{6} \times \text{pole pitch}$

$$\frac{5}{6} \times \frac{30}{180} = 150^\circ = \beta$$

Q. The coil span =  $160^\circ$ , which of the following harmonic is eliminated.

- (a). 3rd (b). 5th (c). 7th (d). 9th.

$$\beta = 160^\circ \Rightarrow \alpha = 180 - \beta = 20^\circ$$

$$\alpha = \frac{180}{n} \Rightarrow n = \frac{180}{20} = 9\text{th.}$$

Q. A 3- $\phi$ , 2-pole, 18 slot alternator, the coil span is 6 slots. the pitch factor is -

- (a). 0.5 (b). 0.866 (c). 0.707 (d). 1.05

$$S/p = \frac{18}{2} = 9 \text{ slots}$$

for full pitch wdg coil span =  $S/p = 9 \text{ slots.}$



but coil span is 6 slots.  $\therefore$  short pitched by 3 slots.

$$\therefore \alpha = 3 \text{ slots.}$$

$$\begin{aligned} \text{slot angle } r &= \frac{180 \times p}{s} \\ &= \frac{180 \times 2}{18} = 20^\circ \end{aligned}$$

$$\therefore \alpha = 3 \times 20 = 60^\circ.$$

$$\therefore k_p = \cos \frac{\alpha}{2} = \cos 30 = 0.866$$

Q. In a 3- $\phi$  m/c slots/pole/ph. = 5. the coil span = 12 slots then the pitch factor is —

- (a). 0.866 (b). 0.707 (c). 0.951 (d). 1.05

$$s/p = 5 \times 3 = 15.$$

$$r = \frac{180 \times p}{s} = \frac{180}{s/p}$$

$$= \frac{180}{15} = 12^\circ$$

for full pitch wdg  
coil span = 15 slots  
but given  $\beta = 12$  slots  
ie short pitched by 3 slots.

$$\therefore \alpha = 3 \times 12 = 36^\circ$$

$$\therefore \alpha = 3 \text{ slots.}$$

$$\therefore k_p = \cos \frac{36}{2} = 0.951.$$

Q. In a 3- $\phi$  m/c the pole pitch = 18 slots. the wdg is short pitched by  $60^\circ$ . then the coil span is —?

- (a). 10 slots (b). 12 slots (c). 8 slots

- (d). 6 slots.

$$(s/p = 18 \text{ slots}) \quad r = \frac{180}{18} = 10^\circ$$

$$\text{pole pitch} = 18 \text{ slots} = 180^\circ$$

$$\Rightarrow \text{for each slot } r = \frac{180}{18} = 10^\circ.$$

The wdg is short pitched by 6 slots.  
ie  $6 \times 10 = 60^\circ$ .

$$\therefore \text{coil span} = 18 - 6 = 12 \text{ slots.}$$

Q. A 3- $\phi$ , 2-pole, 12 slots alternator, coil span = ~~1-5~~ 1-5. The pitch factor is - ?

- (a). 0.5 (b). 0.866 (c). 0.95 (d). 1

$$s/p = \frac{12}{2} = 6 \text{ slots.}$$

$\Rightarrow$  for full pitch wdg the coil span is 1-7.

but given coil span is 1-5. ie short pitched by 2 slots.

$$\text{slot angle } \gamma = \frac{180 \times p}{s} = \frac{180 \times 2}{12} = 30^\circ.$$

$$\therefore \alpha = 2 \times 30^\circ = 60^\circ.$$

$$\therefore k_p = \cos \frac{\alpha}{2} = 0.866.$$

Q. The coil span =  $150^\circ$ . the 3rd harmonic pitch factor is - ?

- (a).  $\cos 45^\circ$  (b).  $\sin 45^\circ$  (c).  $\cos 225^\circ$

- (d).  $\sin 225^\circ$ .

$$\beta = 150$$

$$\Rightarrow \alpha = 180 - \beta = 30^\circ.$$

$$\therefore k_{p_3} = \cos \frac{3\alpha}{2} = \cos 45^\circ$$

$\Rightarrow$  The pitch factor for full pitch wdg  $k_p \neq 1$ .

$$k_{p_1} = k_{p_3} = k_{p_5} = k_{p_7} \dots = 1.$$

$\Rightarrow$  for the short pitch wdg

$$k_{p_1} > k_{p_3} > k_{p_5} > k_{p_7} \dots$$



$$\Rightarrow KVA (3-\phi) = 3 E_{ph} (3-\phi) \cdot I_{ph} (3-\phi)$$

$$KVA (2-\phi) = 2 \cdot E_{ph} (2-\phi) \cdot I_{ph} (2-\phi)$$

$$\frac{KVA (3-\phi)}{KVA (2-\phi)} = \frac{3 \cdot E_{ph} (3-\phi) \cdot \cancel{I_{ph} (3-\phi)}}{2 \cdot E_{ph} (2-\phi) \cdot \cancel{I_{ph} (2-\phi)}}$$

$$= \frac{3 E_{ph} (3-\phi)}{2 E_{ph} (2-\phi)}$$

$$\frac{KVA_{60} (3-\phi)}{KVA_{90} (2-\phi)} = \frac{3 \cdot K_{d60} \cdot T_{ph} (3-\phi)}{2 \cdot K_{d90} \cdot T_{ph} (2-\phi)}$$

$$= \frac{3 \cdot K_{d60} \times \frac{1}{3}}{2 \cdot K_{d90} \times \frac{1}{2}} = \frac{K_{d60}}{K_{d90}}$$

Q. In a 3- $\phi$  AC m/c ph. emf is  $E_1$  and o/p is  $P_1$  for a ph. spread of  $60^\circ$ . where as emf is  $E_2$  and o/p is  $P_2$  for the ph. spread of  $120^\circ$ . The terms  $E_1, E_2$  &  $P_1, P_2$  relates as under,

(a).  $E_1 = E_2, P_1 = 1.15 P_2$  (b).  $E_1 = 1.15 E_2, P_1 = 1.15 P_2$

(c).  $E_1 = 1.15 E_2, P_2 = 1.15 P_1$  (d).  $E_2 = 1.15 E_1, P_2 = 1.15 P_1$

\*  $120^\circ \rightarrow 100V, 100 kVA$   $\rightarrow$  Triplen harmonics are eliminated in phase voltages.  
 (But)  $60^\circ \rightarrow 115V, 115 kVA$   $\rightarrow$  Triplen are existed in phases.

for 3- $\phi$  m/c,  $60^\circ$  ph. spread (narrow ps) is prefer over  $120^\circ$  ph. spread (wide ps) b'coz with  $60^\circ$  ps, the induced emf & kVA ratings are 15% extra compared with  $120^\circ$  ps.  
 (due to triplen)

Q. The distribution factor for a 3- $\phi$  uniformly distribution wdg is - ?

- (a)  $\frac{2}{\pi}$  (b)  $\frac{3}{\pi}$  (c)  $\frac{4}{\pi}$  (d)  $\frac{5}{\pi}$

Sol. for 3- $\phi$ , ph. spread  $m_r = 60^\circ$ .

$$\therefore K_{du} = \frac{\sin \frac{m_r}{2}}{\frac{m_r}{2} \cdot \frac{\pi}{180}} = \frac{\sin 60/2}{60/2 \cdot \pi/180} = \frac{3}{\pi}$$

Q. The distribution factor for 1- $\phi$  uniformly distr. wdg - ?

- (a)  $\frac{2}{\pi}$  (b)  $\frac{3}{\pi}$  (c) 1, (d)  $\pi$

Sol.  $K_{du} = \frac{\sin \frac{180}{2}}{\frac{180}{2} \cdot \frac{\pi}{180}} = \frac{2}{\pi}$  for 1- $\phi$  ph. spread  $m_r = 180^\circ$

Q. The arm. of a 1- $\phi$  Alt. is completely wound with 'T' single turns coils, distributed uniformly.

The induced volt. in each turn = 2V

The emf of whole wdg is -

- (a). 2T volts (b). 1.11T volts (c). 1.414T volts  
(d). 1.273T volts.

Sol.



2V/turn  
2T Volts  
concentrated  
wdg.



distributed  
 $emf = 2T \times k_d$   
 $= 2T \times \frac{2}{\pi} = \frac{4}{\pi} T$   
 $= 1.273T \text{ volts}$



$$E_{ph} = \text{emf/turn} \times T_{ph} \times k_d = 2 \times T \times \frac{2}{\pi}$$

Q. The arm. of a  $\gamma$  connected alt. is uniformly wound with 'T' coils. Each coil having 'n' full pitched turns, the generated emf/conductor is 2V rms. The per phase emf is -

- (a).  $\frac{3}{\pi}$  NT volts      (b).  $\frac{4}{\pi}$  NT volts  
(c).  $\frac{6}{\pi}$  NT volts      (d).  $\frac{2}{\pi}$  NT volts.

Sol. 'T' coils, each coil having 'n' turns.  
Total turns = NT.  
 $\Rightarrow T_{ph} = \frac{NT}{3}$   
 $k_d = \frac{\sin 60/2}{60/2 \cdot \pi/180} = \frac{3}{\pi}$   
if there are 1 turn in a coil then (coil = turn)  
Simply no. of coils = no. of turns.  
2V/condu. 2V = 4V/turn

$$E_{ph} = \text{emf/turn} \times T_{ph} \times k_d$$

$$= 4 \times \frac{NT}{3} \times \frac{3}{\pi} =$$

one coil may have any no. of turns.  
1-turn = 2 conductors

Q. A 3- $\phi$ , 4-pole, Alternator has 48 stator slots carrying the 3- $\phi$  distributed wdg. Each coil of wdg chorded by 1 slot pitch. The wdg factor is -?

- (a).  $\frac{1}{16} \cos 7.5^\circ$       (b).  $\frac{1}{8} \cot 7.5^\circ$   
(c).  $\frac{1}{16} \sin 7.5^\circ$       (d).  $\cos 7.5^\circ$

Sol. wdg factor  $k_w = k_d \cdot k_p$

$$SPP = m = \frac{48}{4 \times 3} = 4, \text{ slot angle } \gamma = \frac{180 \times 4}{48}$$

$$= 15^\circ$$

$$k_d = \frac{\sin \frac{4 \times 15}{2}}{4 \sin \frac{15}{2}} = \frac{1/2}{4 \sin 7.5^\circ} = \frac{1}{8 \cdot \sin 7.5^\circ}$$

$$\alpha = 1 \text{ slot} = 15^\circ$$

$$\Rightarrow k_p = \cos \frac{\alpha}{2} = \cos \frac{15}{2} = \cos 7.5^\circ$$

$$\therefore k_w = k_p \cdot k_d = \frac{1}{8} \cdot \cot 7.5^\circ$$

Fractional slot wdg :-

→ Integral slot wdg: If the spp is an integer.

Eg: A 3- $\phi$ , 2-pole, 18-slot Alternator, spp = 3

Here spp = 3 → Integer.

Fractional slot wdg: If the spp is not an integer i.e. it is a fraction.

Eg: A 3- $\phi$ , 10-pole, 42 slots Alternator.

$$spp = \frac{42}{10 \times 3} = 1.4 \rightarrow \text{fraction.}$$

for balanced fractional wdg, the no. of slots must be divisible with no. of phases i.e. slots/phase must be an integer.

$$\frac{42}{3} = 14 \rightarrow \text{An integer.}$$

$$\text{slots / pole / phase, } spp = \frac{\text{slots}}{\text{poles} \times \text{ph}} = \frac{\text{slots/ph}}{\text{poles}}$$

$$= \frac{s/3}{p} = \frac{k \cdot \frac{s/3}{k}}{k \cdot \frac{p}{k}} = \frac{k \cdot s_k}{k \cdot p_k} = \frac{s_k}{p_k}$$

\*  $\frac{s_k}{p_k} \Rightarrow$  characteristic ratio,  $k \rightarrow$  highest factor which represent the no. of possible parallel paths & no. of repeatable sections.



Eg: A 3- $\phi$ , 10-pole, 42-slots Alternator.

$$SPP = \frac{42}{10 \times 3} = \frac{42/3}{10} = \frac{14}{10} = \frac{2 \times 7}{2 \times 5}$$

$$= \frac{7}{5} = \frac{S_k}{P_k}$$

$$\text{char. ratio } \frac{S_k}{P_k} = \frac{7}{5}$$

$k=2$ , i.e. no. of possible paths = 2.

no. of repeatable sections = 2.

\* The denominator of char. ratio represents, out of 10 poles, the wdg arrangement considered only for 5 poles, it will just repeat for other 5 poles.

\* The numerator of char. ratio represents, out of 42 slots, the wdg arrangement considered only for 21 ( $7 \times 3$ ) slots, the wdg arrangement repeat for other 21 slots.

\* Distribution factor for fractional slot wdg

$$k_{d.f.s} = \frac{\sin \frac{m r}{2}}{S_k \cdot \sin \frac{m r}{2 S_k}}, \text{ where } S_k, \text{ numerator of char. ratio.}$$

WED.  
20/08/08

Adv.s of fractional slot wdg:-

- (1). Effect of higher order harmonic particularly slot harmonics
- (2). Any existing arm. core can be utilized no special slots are required.
- (3). More flexible for the selection of coil span.

Dis. advs:-

- It is possible only with double layer wdg.
- The no. of  $11^{\text{th}}$  paths are restricted.
- ⇒ No. of possible  $11^{\text{th}}$  paths for integral slot wdg  
 $= P/2$ .

Q. A 6-pole, 3- $\phi$ , 50 Hz Y-connected narrow ph. spread alt. has 42 slots with double layer wdg. flux/pole = 0.012 wb and each full pitch coil has 8 turns.

(i).  $K_d$  is -? (a). 0.964 (b). 0.956 (c). 1  
 (d). 0.985.

(ii). The induced emf line to line is close to

(a). 265V (b) 990V (c). 494V (d). 510V

(iii). The L-L emf if the wdg is connected for 2- $\phi$  operation

(a). 285V (b). 494V (c). 403V (d) 571V

Sol.

No. of coils = no. of slots ( $\because$  double layer wdg).  
 $= 42$ .

$$T = 42 \times 8 = 336$$

$$m\gamma = \frac{7}{3} \times \frac{180}{7}$$

$$= 60$$

$$\underline{3-\phi}: SPP = \frac{42}{6 \times 3} = 2.33$$

$$SPP = \frac{s/ph}{poles} = \frac{42/3}{6} = \frac{14}{6} = \frac{2 \times 7}{2 \times 3} = \frac{7}{3} = \frac{s_k}{p_k}$$

$$\text{slot angle } \gamma = \frac{180 \times P}{S} = \frac{180 \times 6}{42} = 25.71^\circ$$

$$K_d = \frac{\sin m\gamma/2}{s_k \cdot \sin \frac{m\gamma}{2s_k}} = \frac{\sin 60/2}{7 \cdot \sin \frac{60}{2 \times 7}} = 0.956$$



$$T_{ph} = \frac{336}{3} = 112.$$

$$k_p = 1 \quad (\because \text{full pitch wdg})$$

$$E_{ph} = 4.44 k_p k_d \phi f T_{ph}$$

$$= 4.44 \times 1 \times 0.956 \times 0.012 \times 50 \times 112$$

$$= 285.23 \text{ V}$$

$$E_L = \sqrt{3} \times 285.23 = 494 \text{ V.}$$

2- $\phi$ :

$$T_{ph} = \frac{336}{2} = 168, \quad k_p = 1.$$

$$SPP = \frac{S/ph}{\text{pole}} = \frac{42/2}{6} = \frac{21}{6} = \frac{3 \times 7}{3 \times 2} = \frac{7}{2} = \frac{S_k}{r_k}$$

$$m = SPP = \frac{42}{2 \times 6} = 3.5$$

$$\gamma = \frac{180 \times 6}{42} = 25.71$$

$$k_d = \frac{\sin \frac{90}{2}}{7 \cdot \sin \frac{90}{2 \times 7}} = 0.902$$

$$E_{ph} = 4.44 k_p k_d \phi f T_{ph}$$

$$= 4.44 \times 1 \times 0.902 \times 0.012 \times 50 \times 168$$

$$= 403.67 \text{ V}$$

$$E_L = \sqrt{2} \times 403.67 = 571 \text{ V.}$$

(or)  $\frac{E_{ph(3-\phi)}}{E_{ph(2-\phi)}} = 0.707$

$$E_{ph(2-\phi)} = \frac{285.23}{0.707} = 403 \text{ V}$$

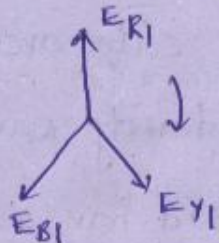
$$E_L = \sqrt{2} \times 403 = 571 \text{ V}$$

## Advantages of $\gamma$ -connected stator:

$$E_L = E_{RY} = E_R - E_Y$$

$$= (E_{R1} + E_{R3} + E_{R5} + \dots) - (E_{Y1} + E_{Y3} + E_{Y5} + \dots)$$

$$= (E_{R1} - E_{Y1}) + (E_{R3} - E_{Y3}) + (E_{R5} - E_{Y5}) + \dots$$



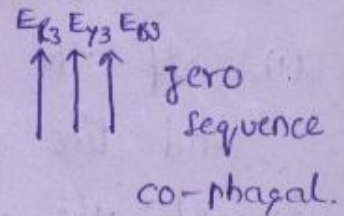
$$E_{R1} \angle 0^\circ; E_{Y1} \angle -120^\circ; E_{B1} \angle -240^\circ.$$

$$R_1 - Y_1 - B_1 \rightarrow \text{ph. seq. (+ve)}$$

$$E_{R3} \angle 120^\circ \times 3 = E_{R3} \angle 0^\circ$$

$$E_{Y3} \angle -120^\circ \times 3 = E_{Y3} \angle -360^\circ = E_{Y3} \angle 0^\circ$$

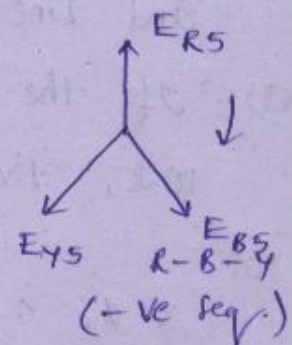
$$E_{B3} \angle -240^\circ \times 3 = E_{B3} \angle -720^\circ = E_{B3} \angle 0^\circ$$



$$E_{R5} \angle 240^\circ \times 5 = E_{R5} \angle 0^\circ$$

$$E_{Y5} \angle -120^\circ \times 5 = E_{Y5} \angle -600^\circ = E_{Y5} \angle -240^\circ$$

$$E_{B5} \angle -240^\circ \times 5 = E_{B5} \angle -1200^\circ = E_{B5} \angle -120^\circ$$



$$6k-1, k=1, 2, 3, \dots$$

$$= 5, 11, 17, 23, \dots \rightarrow \text{(-ve seq.)}$$

$$6k+1, k=1, 2, 3, \dots$$

$$= 7, 13, 19, 25, \dots \rightarrow \text{(+ve seq.)}$$

for  $120^\circ$  ph. spread: In  $\gamma$ -

$$* E_{ph} = \sqrt{E_{ph1}^2 + E_{ph5}^2 + E_{ph7}^2 + E_{ph11}^2 + \dots}$$

$$E_L = \sqrt{3} \cdot \sqrt{E_{ph1}^2 + E_{ph5}^2 + E_{ph7}^2 + E_{ph11}^2 + \dots}$$

\* Circulating currents are zero, when the m/c connected for  $120^\circ$  ph. spread



Q. A 3- $\phi$ , 6-pole, 1000 rpm Alt. has air gap dia. of 28 cm and core length 23 cm, a two layer narrow ph. spread wdg is employed and the wdg is accommodated in 4 slots per pole per ph with 8 condu. per slots. coils are sh. pitched by 1 slot. In the flux density wave the fundamental is found as 0.87 T, 3rd har. 0.24 T and 5th har. 0.14 T.

- (1). If the m/c is Y-connected, the ph. volt - ?  
and line volt - ?
- (2). If the m/c is  $\Delta$ -connected, the ph. volt - ?  
and line volt - ?
- (3). If the per ph. reactance of Alt. at 50 Hz is 10  $\Omega$ , the circulating current in  $\Delta$  will be - ?

Sol.

3- $\phi$ , 6-pole, 1000 rpm,  $D = 28 \text{ cm} = 0.28 \text{ m}$

$L = 23 \text{ cm} = 0.23 \text{ m}$ , narrow ph. spread.

SPP = 4, 8 condu/slot,  $\alpha = 1$  slot

$B_1 = 0.87 \text{ T}$ ,  $B_3 = 0.24 \text{ T}$ ,  $B_5 = 0.14 \text{ T}$

$$\frac{E_{phn}}{E_{ph1}} = \frac{K_{wn}}{K_{w1}} \times \frac{B_n}{B_1}$$

Max. value of fundamental,  $B_1 = \frac{2DL}{p} \times \frac{B_1}{\phi_1}$

Max. value of  $n$ th har. flux density  $B_n = \frac{2DL}{np} \times \frac{B_n}{\phi_n}$

$$f = \frac{PN}{120} = \frac{6 \times 1000}{120} = 50 \text{ Hz}$$

$$\Phi_1 = \frac{2DL}{P} \Rightarrow 0.87 \times \frac{2 \times 0.28 \times 0.23}{6} = \Phi_1$$

$$\Rightarrow \Phi_1 = 0.018 \text{ wb}$$

$$\text{Slots} = 4 \times 6 \times 3 = 72$$

$$T = \frac{72 \times 8}{2} \Rightarrow T_{ph} = \frac{72 \times 8}{2 \times 3} = 96$$

$$spp = m = 4, \quad r = \frac{180 \times P}{S} = \frac{180 \times 6}{72} = 15^\circ$$

$$k_{d1} = \frac{\sin \frac{4 \times 15}{2}}{4 \cdot \sin \frac{15}{2}} = 0.957$$

$$k_{d3} = \frac{\sin \frac{4 \times 3 \times 15}{2}}{4 \cdot \sin \frac{3 \times 15}{2}} = 0.653$$

$$k_{d5} = \frac{\sin \frac{4 \times 5 \times 15}{2}}{4 \cdot \sin \frac{5 \times 15}{2}} = 0.205$$

$$\alpha = 1 \text{ slot} = 15^\circ$$

$$\Rightarrow k_{p1} = \cos \frac{15}{2} = 0.991$$

$$k_{p3} = \cos \frac{3 \times 15}{2} = 0.923$$

$$k_{p5} = \cos \frac{5 \times 15}{2} = 0.793$$

$$\Rightarrow k_{w1} = k_{d1} \cdot k_{p1} = 0.948$$

$$k_{w3} = k_{d3} \cdot k_{p3} = 0.602$$

$$k_{w5} = k_{d5} \cdot k_{p5} = 0.167$$

$$E_{ph1} = 4.44 k_{w1} \Phi_1 f T_{ph}$$

$$= 4.44 \times 0.948 \times 0.018 \times 50 \times 96 = 377.32 \text{ V}$$

$$E_{ph3} = E_{ph1} \times \frac{k_{w3}}{k_{w1}} \times \frac{B_n}{B_1}$$

$$= 377.32 \times \frac{0.602}{0.948} \times \frac{0.24}{0.87} = 66.09 \text{ V}$$



$$E_{ph5} = 377.32 \times \frac{0.167}{0.948} \times \frac{0.14}{0.87} = 10.96 \text{ V}$$

\* SUN. AUG. 24. 2008 \*

→ slot Harmonics

→ space Harmonics →  $(GK \neq 1)$

\* The speed of space harmonics of order  $(GK-1)$  is  $(5, 11, 17, 23, \dots) = (\frac{1}{5}, \frac{1}{11}, \frac{1}{17}, \dots) N_s$

⇒ rotate in reverse (or) opposite dire. that of fundamental, since -ve seq. harmonics.

\* The speed of space harmonics of order  $(GK+1)$  is  $(7, 13, 19, \dots) = (\frac{1}{7}, \frac{1}{13}, \frac{1}{19}, \dots) N_s$ , rotate in the same dire. that of fundamental, since +ve seq. harmonics.

Q. The 83rd harmonic will rotate in -

- (a). In the same dire. of funda.
- (b). In reverse dire. of funda.
- (c). No rotation.

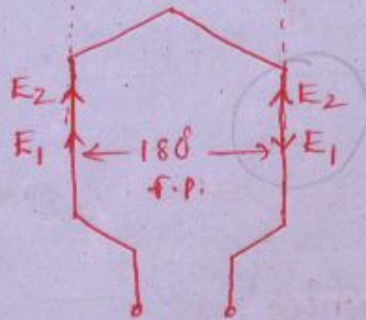
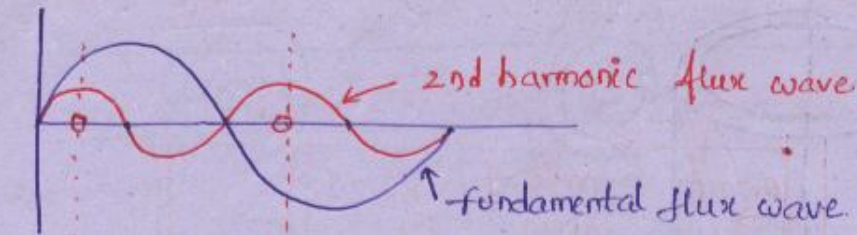
83rd → -ve seq. harmonic

Q. The 81st harmonic will rotate in - ?

- (a). Same dire. that of funda.
- (b). Reverse dire. " "
- (c). No rotation.

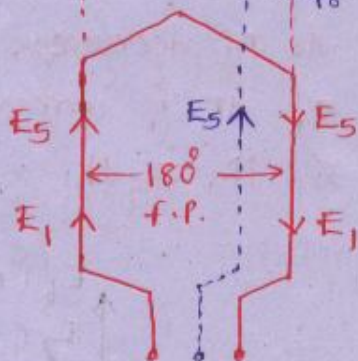
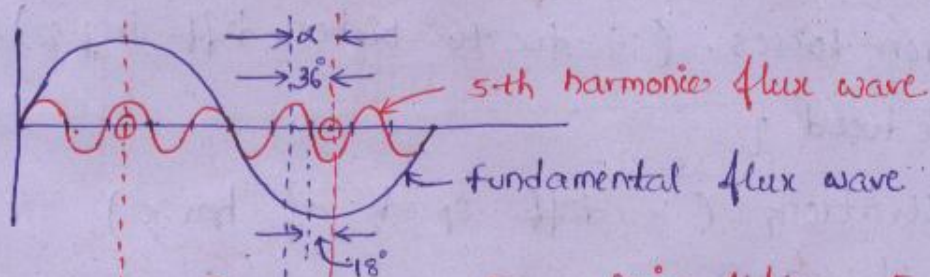
Ans: 81 → Triplen harmonic

zero seq. harmonic → no rotation.



$E_1 \rightarrow$  Series Aiding  $\rightarrow E_{1res} = 2E_1$

$E_2 \rightarrow$  Series opposing  $\rightarrow E_{2res} = 0$ .



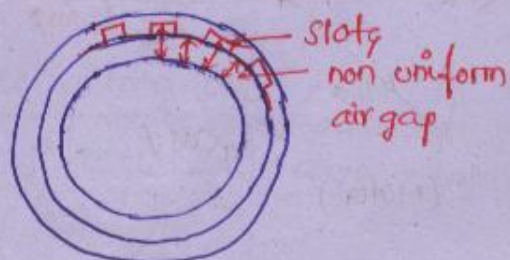
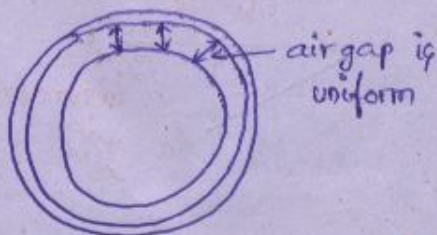
$E_1 \rightarrow$  Series Aiding  $\rightarrow E_{1res} = 2E_1$

$E_5$  with f.p.  $\rightarrow$  Series Aiding  $\rightarrow 2E_5$

$E_5$  with s.p.  $\rightarrow$  Series opposing  $\rightarrow 0$

### SLOT Harmonics :-

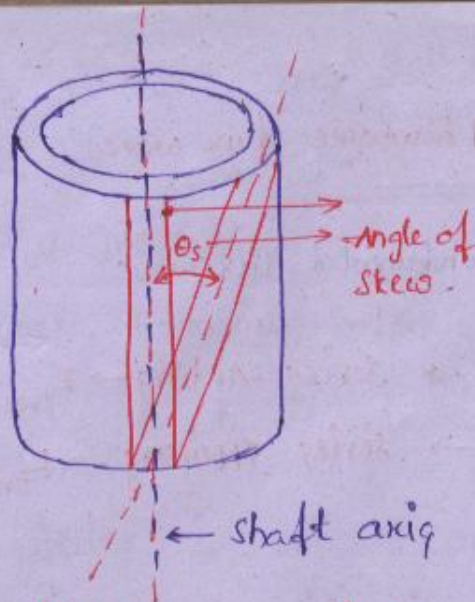
Due to variable reluctance caused by slotting the stator & rotor & both.



$\rightarrow$  SLOT Harmonics are higher order Harmonics.

$\Rightarrow$  Slot Harmonics can be eliminated by skewing the armature slots.

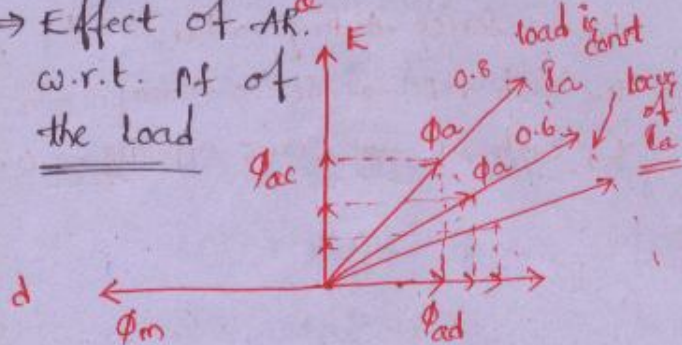




⇒ Effects caused by Harmonics :-

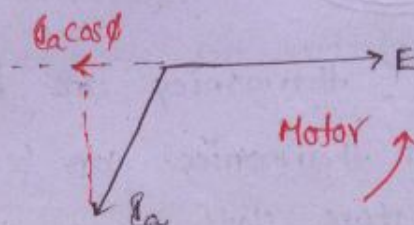
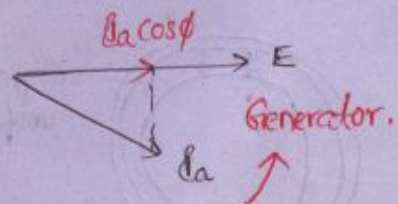
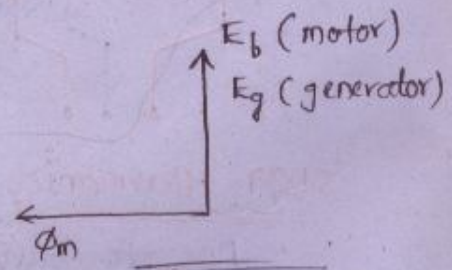
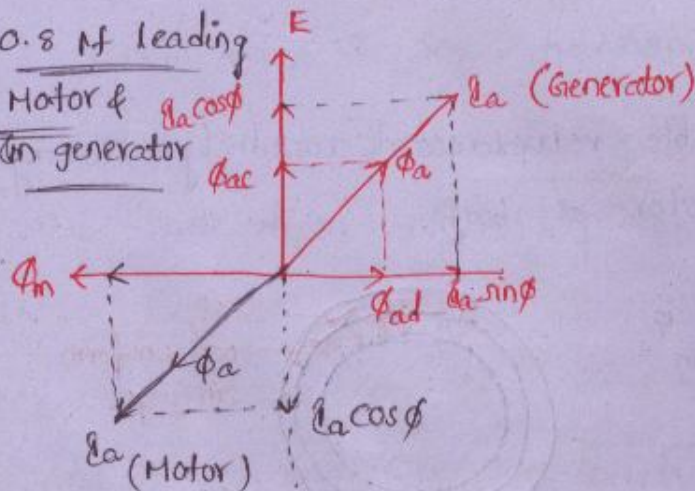
- ↳ Iron losses. ( $\because$  due to higher & diff freq.  $\phi$ )
- ↳ Reduced  $\eta$
- ↳ vibrations ( $\because$  diff speeds of bars)

⇒ Effect of AR<sup>φ</sup> w.r.t. pf of the load



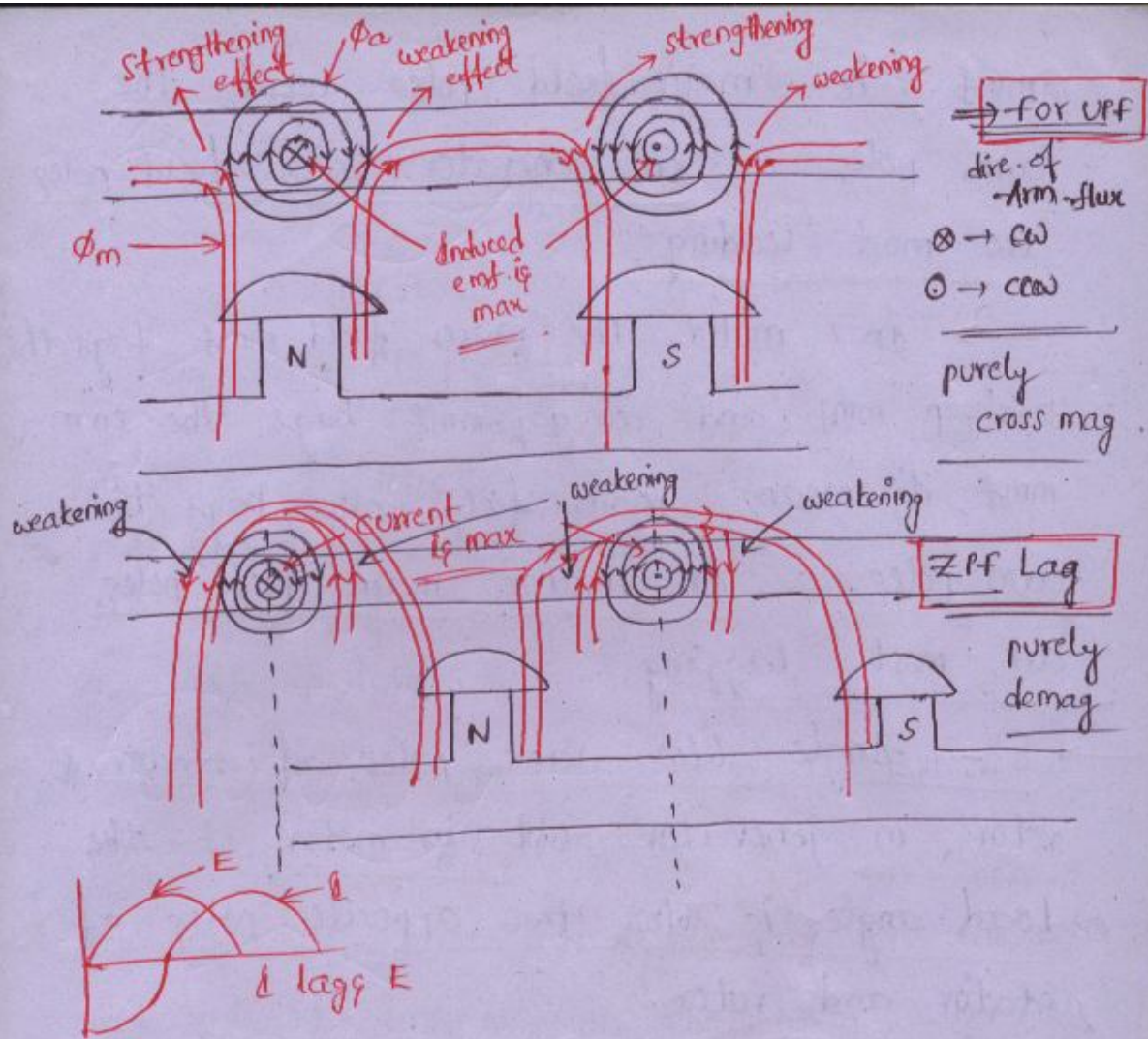
As pf decreases, effect of AR is increased. i.e.  $\phi_{ad} \uparrow$ ,  $\phi_{ac} \downarrow$

⇒ 0.8 pf leading in Motor & in generator



⚡ Angle is more than  $90^\circ$ ,  
→ motor.





### ⇒ Synchronous Speed :-

If the rotating mag. field or poles are rotated at equal angle in the space for the given time angle of current.

→ The magnitude of  $\phi_a = 1.5$  times of max. value due to any phase.

### ⇒ Torque :

Torque is the interaction b/w 2 fields or 2 poles. It may be attraction in case of motor, and repulsion in case of generator.

→ In generator main field mmf leads the airgap mmf & airgap mmf leads the arm



mmf. i.e. main field poles leads the arm. poles  $\therefore$  In generator main field poles are most leading.

→ In motor the main field mmf lags the air gap mmf and air gap mmf lags the arm. mmf, it means main field poles lags the arm poles.  $\therefore$  In motor main field poles are most lagging.

→  $\delta$  - Angle b/w same poles of stator & rotor in generator. but in motor  $\delta$  - the load angle is b/w two opposite poles of stator and rotor.

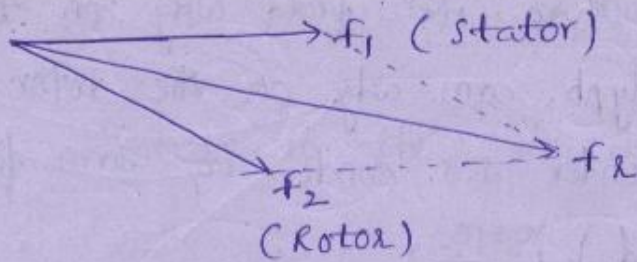
→ In generator the electromagnetic torque will be in opposite dire. to rotor  $\omega$   $T_{pm}$ .

→ In motor  $T_{em}$  developed will be in the same dire. of rotor rotation.

→ for the production of uni dire. torque, the 2 fields must be stationary w.r.t. each other and they should have equal no. of poles. It means the relative speed b/w stator & rotor field must be zero.

→ The no. of stator poles = no. of rotor poles





$$T_{em} = -\frac{p}{2} \mu_0 \frac{\pi x l}{g} f_1 f_2 \sin \delta$$

$p$  - no. of poles

$x$  - radius of rotor core.

$l$  - length of " "

$g$  - Airgap length

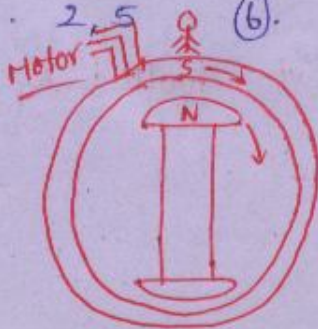
-ve sign is because of always the two fields will try to align themselves.

Q. A syn. m/c have its field wdg on the rotor and poly ph. arm wdg on the stator, when running under steady condns its arm field (airgap field) is

1. stationary w.r.t stator
  2. Rotating at syn. speed  $N_s$  w.r.t. stator
  3. Rotating at double  $N_s$  w.r.t. rotor.
  4. stationary w.r.t rotor
  5. Rotating at  $N_s$  in the dire. of rotor rotation.
- from these correct Ans. is

(a). 2, 5 (b). 1, 4, 5 (c). 2, 3, 4 (d). 2, 4, 5.

Ans:



⇒ Arm. mmf will rotate at  $N_s$  w.r.t. stator.

⇒ Arm mmf or poles are stationary w.r.t. rotor. ( $\because$  relative speed = 0).

⇒ Arm. mmf will rotate in the same dire. that of rotor.



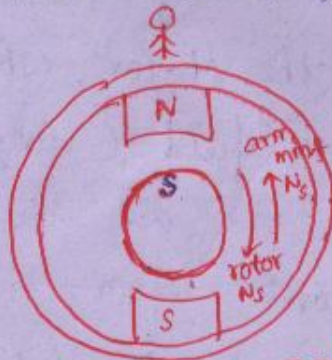
Q. A syn. m/c has its field wdg on the stator and polyph. arm. wdg on the rotor. When running under s.s. condi. its arm field (air gap field) is —?

1. stationary w.r.t stator.
  2. Rotating at syn. speed w.r.t stator.
  3. Rotating at  $N_s$  in the dire. of rotor
  4. Rotating at doubled  $N_s$  w.r.t rotor
  5. Rotating at  $N_s$  w.r.t rotor.
  6. Rotating in a dire. opposite to rotor rotation
- from these correct answer is —?

(a) 2, 5    (b) 1, 4, 6    (c) 2, 4, 6    (d) 1, 3, 5.

Ans:

Motor  
Attraction



⇒ Main field mmf is stationary w.r.t stator.

⇒ Arm. mmf must be stationary w.r.t stator. ∴ the arm mmf must be stationary w.r.t stator mmf.

⇒ when rotor rotates in cw with  $N_s$ , then s-pole (arm. mmf) will try to rotate in ccw with the same speed  $N_s$ .

⇒ arm. mmf will rotate in opposite dire. that of rotor rotation.

⇒ The arm. mmf will rotate at doubled  $N_s$  w.r.t rotor.



Q. In DC generator (or motor) the arm. mmf will.

a). rotate in the same dire. of rotor

b). " " opposite dire. that of rotor

c). stationary w.r.t. stator

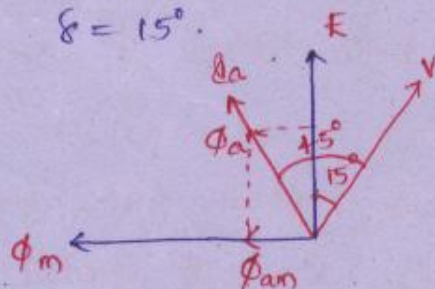
d). both b & c.

5. external characteristics :-

$$\begin{array}{c|c} V_t, V_f, I_a & \begin{array}{l} I_f = \text{const} \\ R_f = \text{const} \\ N = \text{const} \end{array} \end{array}$$

Let  $R_f = 0.707 \text{ lead}$ ,  $\phi = 45^\circ$

$\delta = 15^\circ$ .



effect of AR is magnetisation,

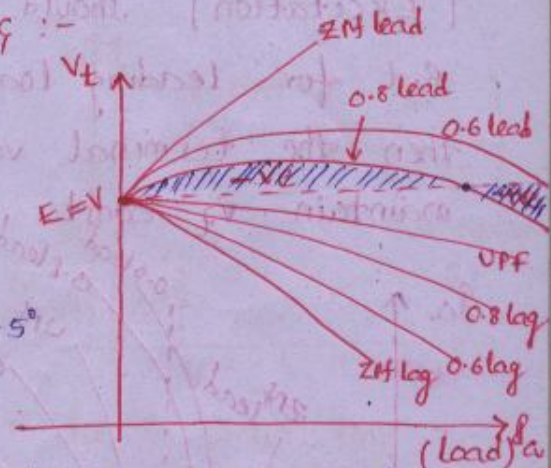
reg  $\rightarrow -ve$ .

\* As the load increases,

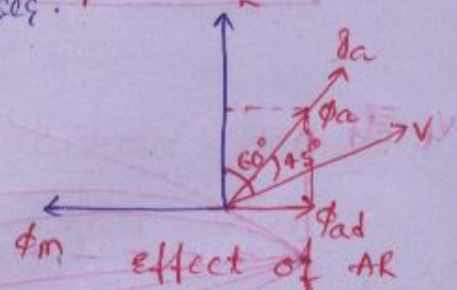
for  $UPF$  (resistive loads) and

for inductive loads, the  $V_t$

terminal voltage will be decreased and so the reg. is  $+ve$ .



Let  $R_f = 0.707 \text{ lead}$ ,  
 $\phi = 45^\circ$ ,  $\delta = 60^\circ$ . Since  
as load increases,  $\delta$  also  
increases.



effect of AR

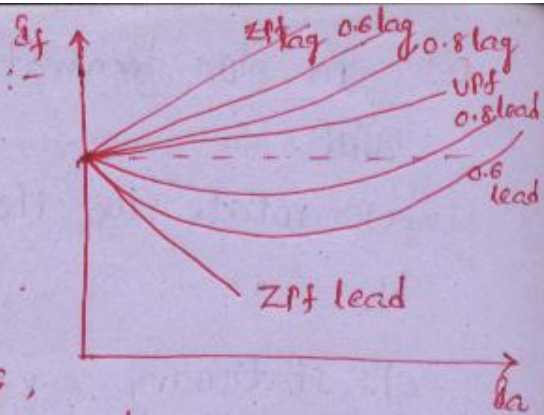
is demagnetisation

reg  $\rightarrow +ve$



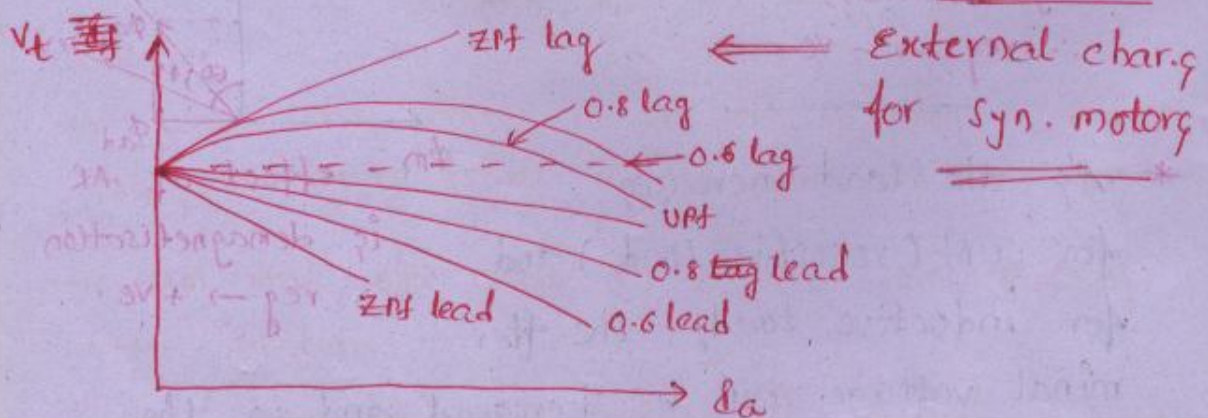
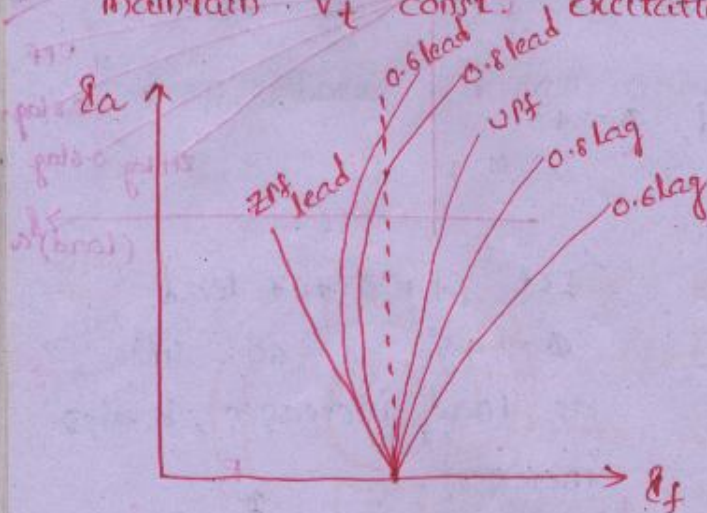
6. compounding char.:

$$\begin{array}{c|c} \delta_f & \begin{array}{l} V_t = \text{const} \\ P_f = \text{const} \\ N = \text{const} \end{array} \\ \hline V_f & \\ \hline I_a & \end{array}$$

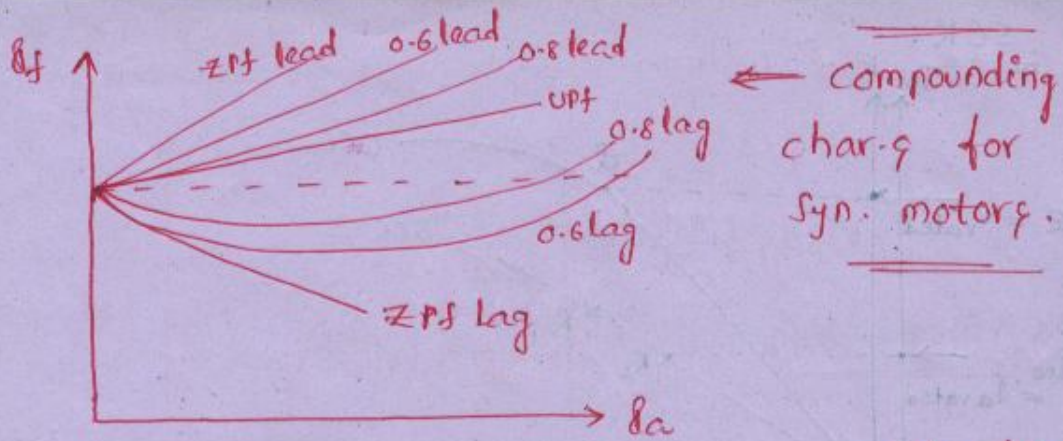


As the load [ $I_a$ ] increases, the terminal voltage decreases for UPF & inductive load, so to maintain  $V_t$  const, field current [Excitation] should be increased.

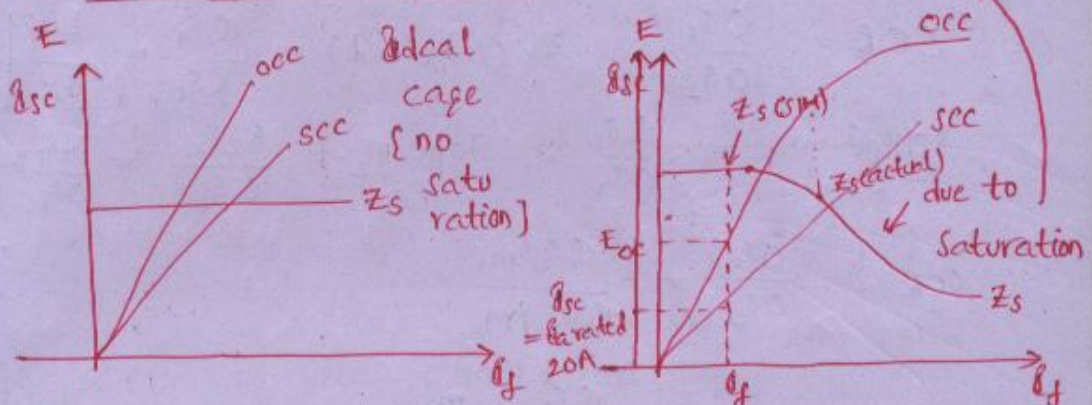
But for leading loads as load ~~the~~ increases, then the terminal volt. increases so in order to maintain  $V_t$  const, excitation should be decreased.







### Synchronous Impedance Method:



$Z_s$  is varied w.r.t excitation due to saturation.

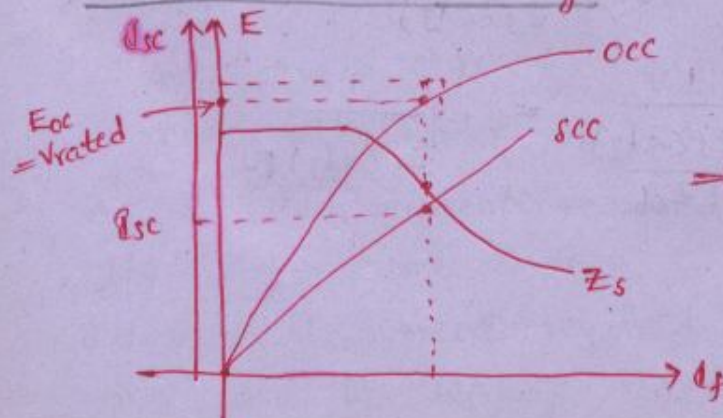
$$Z_s(\text{unsat}) > Z_s(\text{sat})$$

→ In this method  $Z_s$  is measured corr. to field current belongs to rated short circuit current.

$$\text{reg}(\text{sim}) > \text{reg}(\text{actual})$$

### Saturated Syn. Impedance (or reactance) Method:-

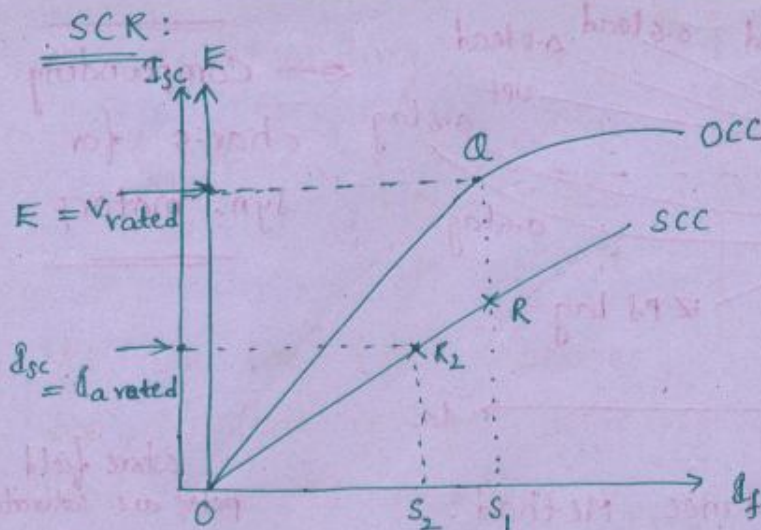
→ In this  $Z_s$  is measured, the field current corr. to rated o/c voltage.



$$Z_s(\text{sat or adjusted}) = \frac{E_{oc}}{I_{sc}} \bigg|_{I_f} \text{ at } E_{oc} = V_{\text{rated}}$$

$$\Rightarrow \text{reg}(\text{EMF of syn. imp. method}) > \text{reg}(\text{sat. syn. imp. method})$$





$$SCR = \frac{OS_1}{OS_2} ; Z_s(\text{adjusted}) = \frac{QS_1}{RS_1} = \frac{E_{oc}}{I_{sc}} \Big|_{\substack{I_f \text{ is} \\ \text{at} \\ E_{oc} = V_{rated}}}$$

$$\text{slope } m_1 = \frac{QS_1}{OS_1} ; \text{slope } m_2 = \frac{RS_2}{OS_2} = \frac{RS_1}{OS_1}$$

$$SCR = \frac{OS_1}{OS_2} = \frac{QS_1/m_1}{R_2 S_2 / m_2}$$

$$= \frac{QS_1}{R_2 S_2} \times \frac{m_2}{m_1}$$

$$= \frac{QS_1}{R_2 S_2} \times \frac{RS_1}{QS_1}$$

$$= \frac{QS_1}{R_2 S_2} \times \left( \frac{QS_1}{RS_1} \right)$$

$$= \frac{V_{rated}}{I_{rated}} \times \frac{1}{Z_s(\text{adj})}$$

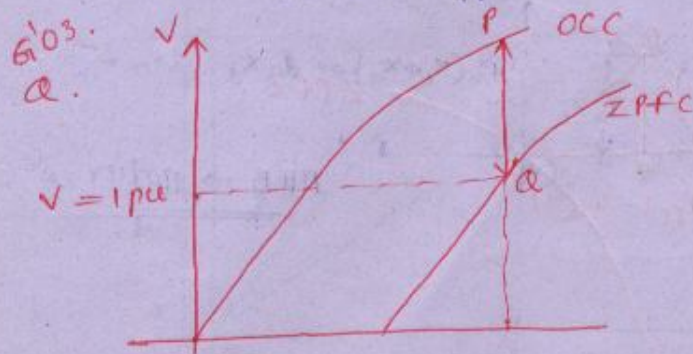
$$= Z_{sb} \times \frac{1}{Z_s(\text{adj})}$$

$$SCR = \frac{1}{\frac{Z_s(\text{adj})}{Z_{sb}}} = \frac{1}{Z_s(\text{adj}) \text{ pu}}$$





#B: field current required to overcome the effect of AR.



$X_a$  = magnetising reactance

leakage reactance = potier "

$P_a$  represent the drop due to,

- (a). leakage reactance      (b). potier reactance
- (c). syn. reactance      (d). magnetising "

\* voltage regulation in descending order:

$$EMF > \text{saturated syn. reactance} > ASA > ZPF > MMF$$

### SLIP TEST :-

\* During slip test, the induced emf in the open field wdg which is AC sinusoidal at slip frequency.

\* A reduced voltage of (20-25) % of  $V$  is applied to the arm.

\* field is driven at less than  $N_s$ , why b'coz, when the field is driven at  $N_s$ , the flux linkages are max, so  $I_a$  min.

always. So we won't get max values of  $I_a$  i.e. field is in locking with the stator poles.

Q. During slip test the induced emf in the open field wdg is - ?

- (a) zero for  $x_d$       (b) zero for  $x_q$



(c). max, +ve for  $x_q$  (d). max, +ve for  $x_d$ .

Q. The results of slip test for determining  $x_d$  and  $x_q$  reactances of a  $\gamma$  connected salient pole alt. are given below (ph. values)

$$\sqrt{3} E_{\max} = 108 \text{ V}, \quad V_{\min} = 96 \text{ V}, \quad I_{\max} = 12 \text{ A} \\ I_{\min} = 10 \text{ A}.$$

then  $x_d = ?$  &  $x_q = ?$

\* At max. power developed condi. alternator operate at leading pf and a syn. motor operate at lagging pf, when the m/c is operating on infinite bus bar.

Q. An alternator with syn. reactance of  $0.8 \text{ pu}$  is connected to an infinite bus at rated volt. with its excitation emf adjusted to  $1.3 \text{ pu}$ . The Alt. delivers an o/p of  $0.5 \text{ pu}$  neglect all losses.

(1). Load angle — ?

(a).  $31^\circ$  (b).  $17.92^\circ$  (c).  $9.6^\circ$  (d).  $21^\circ$ .

(2). The arm. current is — ?

(a).  $0.581 \text{ pu}$  (b).  $0.375 \text{ pu}$  (c).  $1 \text{ pu}$  (d).  $0.8 \text{ pu}$

(3). The pf — ?

Sol: (a).  $x_s = 0.8 \text{ pu}$   $P = 0.5 \text{ pu}$   
 $V = \text{rated volt} = 1 \text{ pu}$   
 $E = 1.3 \text{ pu}$



$$P = \frac{EV}{X_s} \cdot \sin \delta$$

$$\Rightarrow 0.5 = \frac{1.3 \times 1}{0.8} \sin \delta$$

$$\Rightarrow \delta = 17.9^\circ$$

$$I_a = \frac{E \angle \delta - V \angle 0}{Z_s \angle \theta}$$

$$= \frac{1.3 \angle 17.9 - 1 \angle 0}{0.8 \angle 90} = 0.581 \angle -30.63^\circ$$

$$\Rightarrow I_a = 0.581 \text{ pu}; \text{ pf} = \cos(30.63) = 0.86 \text{ lag}$$

Q. A Syn. Gen. is connected to an infinite bus bar at 1 pu volt. and draws 0.6 pu current at upf. Its syn. reactance is 1 pu and resistance is negligible. The excitation volt.  $E$  & load angle  $\delta$  will be res.

(a) 0.8 pu,  $36.86^\circ$  lag (b) 0.8 pu,  $36.86^\circ$  leading

(c) 1.17 pu,  $30.96^\circ$  leading (d) 1.17 pu,  $30.96^\circ$  lag

Sol:-

$$V = 1 \text{ pu}, \quad I_a = 0.6 \text{ pu}, \text{ upf.}$$

$$X_s = 1.0 \text{ pu.}$$

$$E = V \angle 0 + I_a \angle \pm \phi \cdot Z_s \angle \theta$$

$$= 1 \angle 0 + 0.6 \angle 0 \times 1 \angle 90$$

$$= 1.17 \angle 30.96$$

$$\Rightarrow 1.17, 30.96^\circ \text{ leading.}$$

If rated  
kVA is given then  
 $V = 1 \text{ pu}; I_a = 1 \text{ pu}$

Q. A 3,300 V,  $\Delta$  connected syn. gen. has syn impedance of  $(0.4 + j5) \Omega/\text{ph}$ . per an excitation emf of 4,000 V, and power of 1000 kW at rated volt. the line current is —? and pf is —?

Sol:-

$$V = 3,300 \text{ V}, \Delta\text{-connected}$$

$$Z_s = (0.4 + j5) \Omega/\text{ph}$$

$$E = 4000 \text{ V}$$

$$P = 1000 \text{ kW}$$

$$V_{ph} = \frac{3300}{\sqrt{3}} = 1905 \text{ V}$$

$$E_{ph} = \frac{4000}{\sqrt{3}} = 2309 \text{ V}$$

$$Z_s = 0.4 + j5 = 5.01 \angle 85.14^\circ$$

$$P = \frac{EV}{Z_s} \cos(\theta - \delta) - \frac{V^2}{Z_s} \cos \theta$$

$$\Rightarrow \frac{1000 \times 10^3}{3} = \frac{2309 \times 1905}{5.01} \cos(85.14 - \delta) - \frac{(1905)^2}{5.01} \cos(85.14)$$

$$\Rightarrow \delta = 21.8^\circ$$

$$P_a = \frac{E \sin \delta - V \sin \theta}{Z_s \sin \theta} = \frac{2309 \sin 21.8 - 1905 \sin \theta}{5.01 \sin 85.14}$$



Q. The freq. of the existing system is  $50 \text{ Hz}$ . An alt. with the freq  $50.2 \text{ Hz}$  is connected  $11^{\text{th}}$  to the existing system through dark lamp method. The flickering of bulbs per min is —?

- (a) 2      (b) 10      (c) 12      (d) 0.2

$$\begin{aligned} \text{flickering rate} &= f - f' = 50 - 50.2 = 0.2 \text{ Hz} \\ &= 0.2 \text{ flicker/sec} \\ &= 0.2 \times 60 \text{ flickering/min} \end{aligned}$$

⇒ one dark, two lamps equally bright :-

→ two lamps are connected as cross connected.

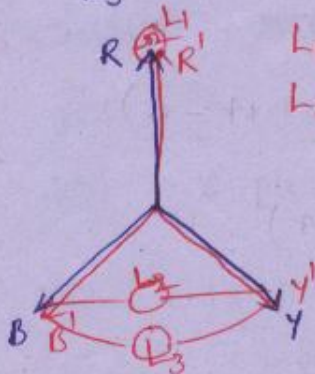
$L_1 \rightarrow R - R'$   
 $L_2 \rightarrow Y - B'$   
 $L_3 \rightarrow B - Y'$

} Cross connected.

$R$   $R'$

$L_1$  — dark

$L_2, L_3$  — equally bright.



→ In the 3 lamps simul. dark & bright method, if the volt. across the lamps falls to  $\frac{1}{3}$  of rated volt, the lamps won't glow, if the switch is closed at this position, results circulating currents, but this dis. adv. can be overcome in one dark, 2 equally bright. At the position of synchronization if 2 are equally bright, it will be confirm



other lamp will be completely dark,  
when the switch is closed at this position  
min circulating currents.

Effect of change in excitation:-  
Syn. power is reactive power

when excitation of one m/c increased,  
Syn. power is reactive power, which will  
produces flux to magnetise other m/c and  
demag. the m/c whose exci. is increased  
During 11<sup>th</sup> operation, an over excited m/c  
will always demag. and under excited  
m/c will always magnetise to maintain  
the terminal voltage.

→ Active power will create torque

→ Reactive power will create flux.

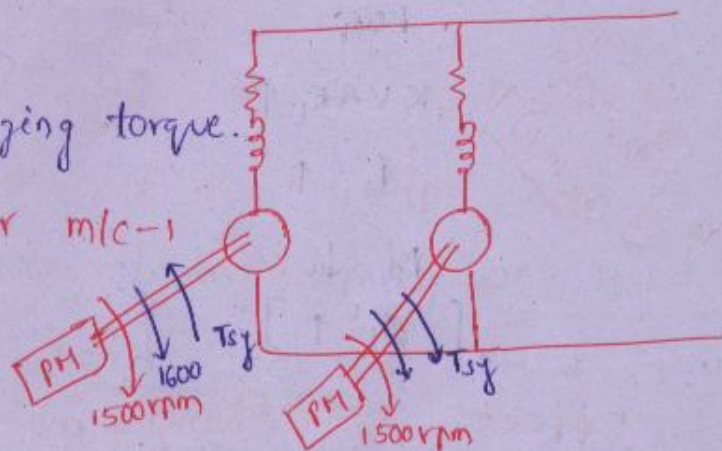
Effect of change in steam i/p (or Mech.  
power i/p):-

$T_{sy}$  - Synchronizing torque.

w.r.t Syn. power m/c-1

acts as Gen &

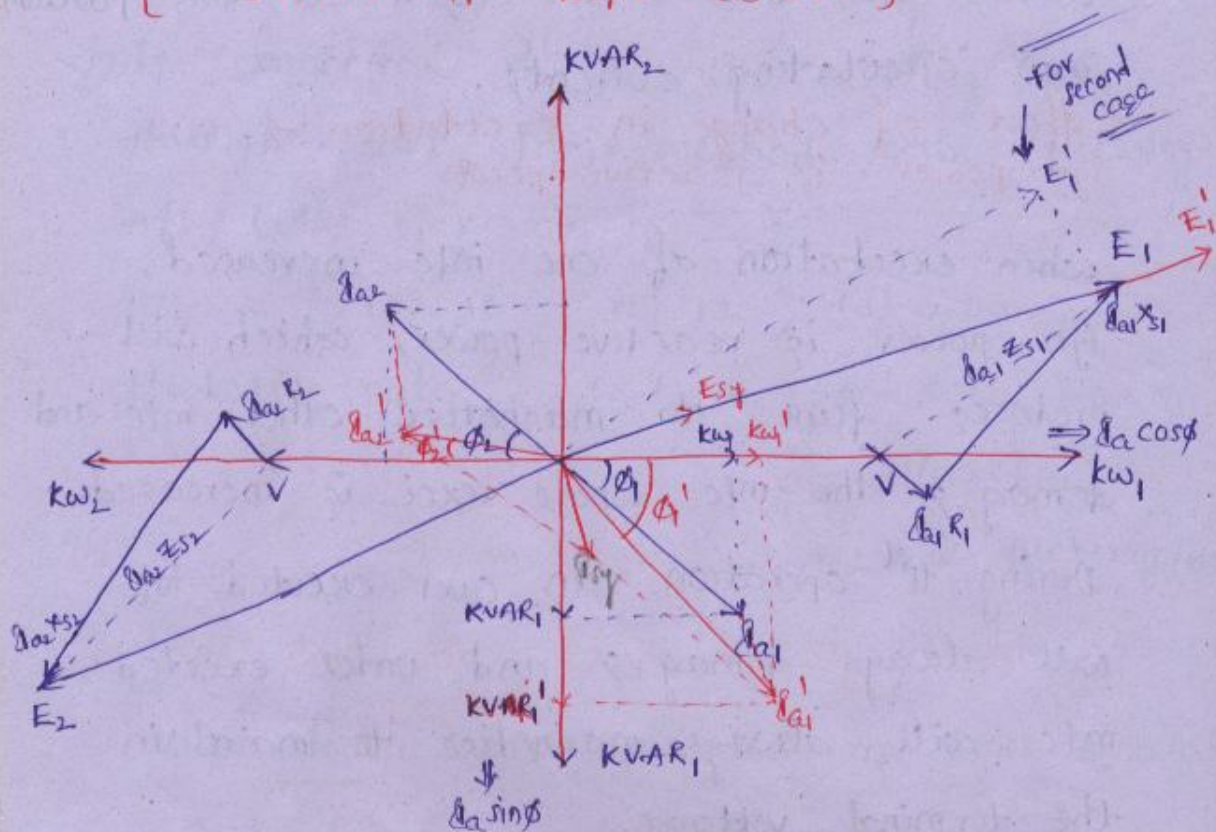
m/c-2 acts  
as motor.



∴  $P_{sy}$ , decelerates 1st m/c & accelerate  
the 2<sup>nd</sup> m/c such that set freq. equalize.



Effect of change in excitation :-  
 [ steam i/p kept const. ]



If excitation of m/c<sub>1</sub> is increased,  
 i.e.  $E_1 \uparrow$  to  $E_1'$ .

	<u>m/c - 1</u>		<u>m/c - 2</u>
	$Kw_1$	=	$Kw_2$
	$KVAR_1 \uparrow$		$KVAR_2 \downarrow$
	$I_{a1} \uparrow$		$I_{a2} \downarrow$
	$Pf \downarrow$		$Pf \uparrow$
	$[\phi_1' \uparrow]$		$[\phi_2' \downarrow]$

$I_a = \sqrt{(I_a \cos \phi)^2 + (I_a \sin \phi)^2}$

Effect of change in steam i/p :-

[ excitation is kept constant ] :-

If the steam i/p of m/c-1 is increased

	<u>m/c-1</u>		<u>m/c-2</u>
	$KVAR_1$	=	$KVAR_2$
$\delta_e = \sqrt{(\delta_a \cos \phi)^2 + (\delta_a \sin \phi)^2}$	$KW_1 \uparrow$		$KW_2 \downarrow$
$Pf \propto \frac{KW}{KVAR}$	$\delta_{a1} \uparrow$		$\delta_{a2} \downarrow$
	$Pf \uparrow$		$Pf \downarrow$

→ change in pf will be more when the change in excitation [1 case].

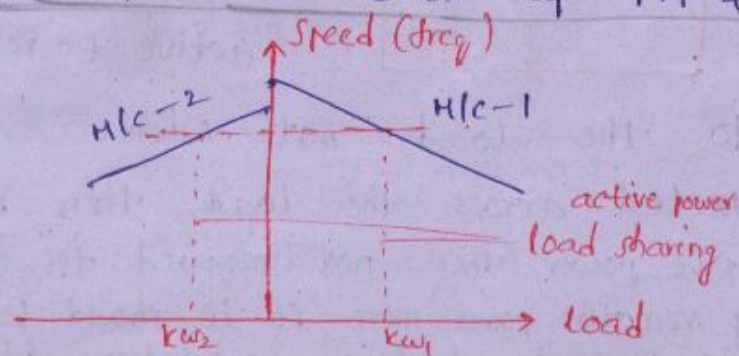
→ The effect of change in excitation causes change in reactive power but no change in active power.

→ the effect of change in steam i/p causes change in its active power but no change in its reactive power.

→ ∴ The reactive power is controlled by varying the excitation thereby pf can be controlled.

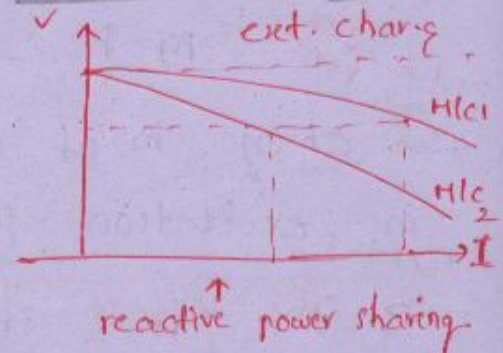
→ The active power can be controlled by controlling steam i/p or PM i/p.

→ Active power sharing depends on speed (or freq) vs load char. of PM & steam i/p.





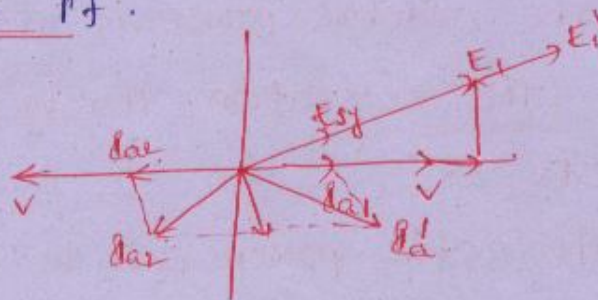
✓ for proper sharing of load PM should have drooping char. i.e. as load  $\uparrow$ , speed  $\downarrow$   
 $\Rightarrow$  Reactive power sharing depends upon the amount of excitation & external char ( $V$  vs  $I$ ) of the Alternator



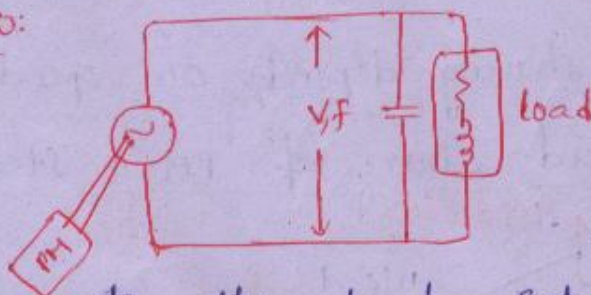
Q. Two alt.-s  $m_1$  &  $m_2$  have been properly syn.cd and connected . . . . [ see in objectives - 5 & 7. no. 5 ].

Ans: MLC-1 magnetizes & MLC-2 demagnetizes so MLC-1 operates with leading pf & MLC-2 with lagging pf.

Q6:



Q10:



If the load is inductive then the Alt delivers both active & reactive powers

to the load. But when a capacitor connected across the load, then it will supply reactive power then not required for the alt. to supply reactive power more so it should be decreased its reactive power by decreasing excitation. If excitation is

not decreased then the terminal volt increase. so to maintain terminal volt. excitation should be decreased.

Q.15: Two 3- $\phi$ , Y-connected

Ans:  $E_{L1} = 3300 \text{ V}$ ,  $E_{L2} = 3200 \text{ V}$

$$X_{S1} = X_{S2} = 1.7 \Omega$$

$$I_{sy} = I_c = \frac{E_1 - E_2}{X_{S1} + X_{S2}}$$

$$= \frac{\frac{3300}{\sqrt{3}} - \frac{3200}{\sqrt{3}}}{1.7 + 1.7}$$

$\left\{ \begin{array}{l} X_{S1} \& X_{S2} \text{ are per} \\ \text{ph. values} \end{array} \right\}$

$= 16.98 \text{ A} \leftarrow \text{ph. current.}$

Q.17: 500 MW, 3- $\phi$ , Y-connected.

$$V_L = 21.5 \text{ kV}, 0.85 \text{ pf.}$$

$$I_L = ? \text{ at fL.}$$

$$\sqrt{3} V_L I_L \cos \phi = P$$

$$\Rightarrow I_L = \frac{P}{\sqrt{3} V_L \cos \phi} = \frac{500 \times 10^6}{\sqrt{3} \times 21.5 \times 10^3 \times 0.85} = 15.97 \text{ kA}$$

Q.16:

400V, 50 kVA, 0.8 pf lead,  $\Delta$ -connected

50 Hz,  $X_s = 2 \Omega$ ,  $R_a = 0$ , friction & windage

loss = 2 kW, core loss = 0.8 kW

shaft supplying 9 kW at 0.8 pf lead.

$$\therefore P_{\text{input}} = P_{\text{out}} + \text{losses}$$

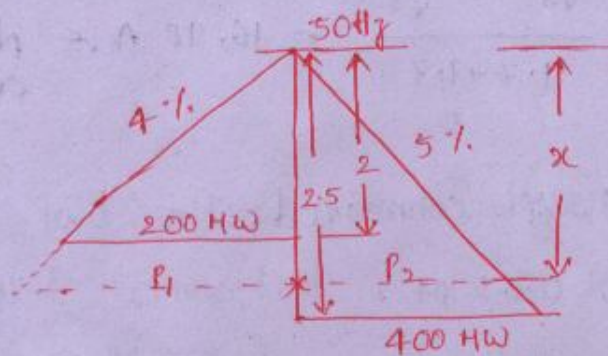
$$= 9 + 2 + 0.8 = 11.8 \text{ kW}$$

$$P_{\text{in}} = \sqrt{3} V_L I_L \cos \phi \Rightarrow I_L = \frac{11.8 \times 10^3}{\sqrt{3} \times 400 \times 0.8}$$

$$= 21.29 \text{ A}$$



Q.9: Two alt.-g rated 200 MW & 400 MW are operating in parallel. The governor drooping char.-g are 4% & 5% res. from NL to FL. At NL the system freq. is 50 Hz when supplying a load of 600 MW, the system freq. will be - ?



$$50 \times 0.05 = 2.5 \text{ Hz}$$

$$47.5 \text{ Hz}$$

$$50 \times 0.04 = 2 \text{ Hz}$$

$$\frac{P_1}{200} = \frac{x}{2.5} \Rightarrow P_1 = 100x$$

$$\frac{P_2}{400} = \frac{x}{2.5} \Rightarrow P_2 = 160x$$

$$P_1 + P_2 = 600$$

$$100x + 160x = 600$$

$$\Rightarrow x = 2.3$$

$$\Rightarrow f = 50 - 2.3 = \underline{\underline{47.3 \text{ Hz}}}$$

Alternator in parallel with infinite Bus Bar:-

$$\phi \propto \frac{V}{f} = \text{const.}$$

$$\phi_r = \phi_m \pm \phi_a = \text{const.}$$

$$\phi_r = \phi_m \pm \phi_a = \text{const.} \quad \begin{array}{l} + \rightarrow \text{mag} \\ - \rightarrow \text{demag} \end{array}$$

$$= 10 \text{ mwb}$$

$$\rightarrow \text{Normal Exci.}, \quad 10 \text{ mwb} = 10 \text{ mwb} + 0$$

$$\rightarrow \text{Under Exci.}, \quad 5 \text{ mwb} + 5 \text{ mwb} = 10 \text{ mwb.}$$

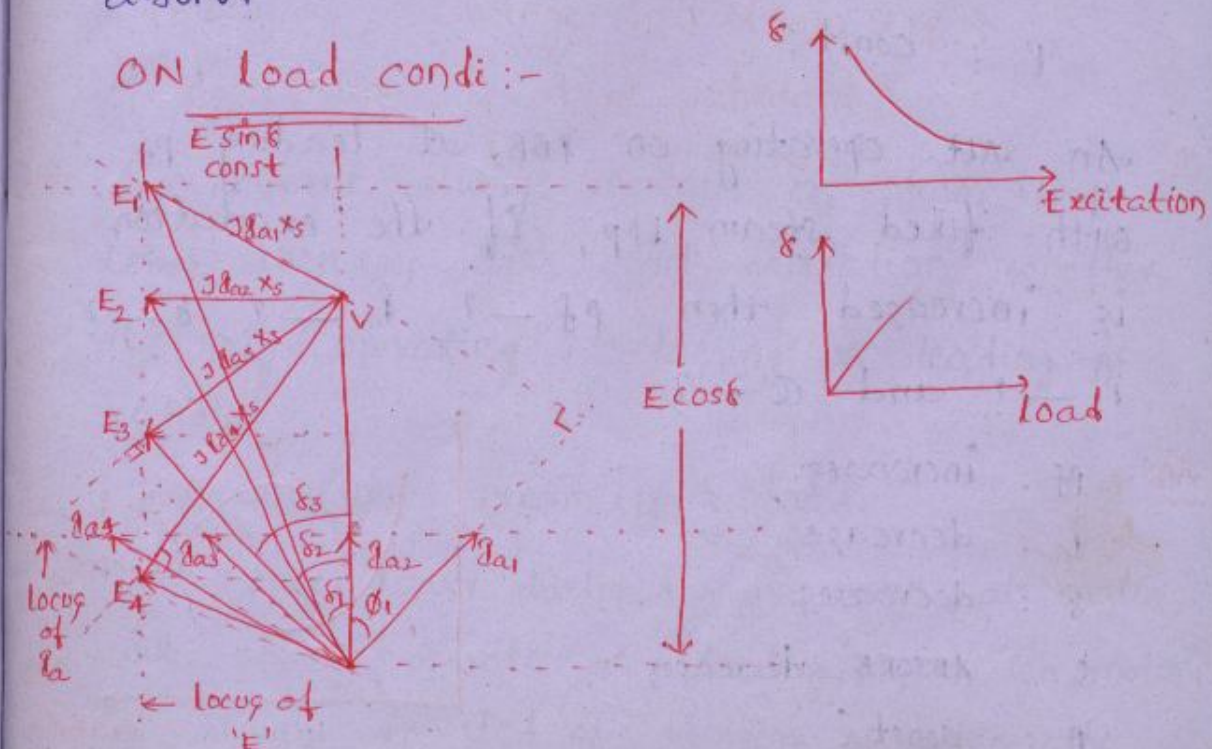
$$\rightarrow \text{Over Exci.}, \quad 15 \text{ mwb} - 5 \text{ mwb} = 10 \text{ mwb}$$

→ The role of the reactive power is to maintain the const. airgap flux. The m/c is under exci.d then it absorb the reactive power, flux aids to the main field flux  $\therefore$  combinely maintain the air gap flux const.

→ when the m/c is o.e'd i.e. field exci. is given more than the m/c required then m/c deliver the reactive power, produces flux which will demag.s main field flux, and hence  $\Phi_r$  maintainng const.

→ for N.E.n the de exci.n is just sufficient to create working flux  $\therefore$  no need of reactive power i.e. neither deliver nor absorb.

ON load condi:-





⇒ when alt.s operate on  $\delta BB$ , for generally over excited b'coz most of the loads are inductive nature, they will absorb reactive power which is supposed to deliver by over excited alternators, with over excitation stability will improve and stable parallel operation. ('V' & 'X' curves).

Q. An alt. operating on  $\delta BB$ , at lagging pf with fixed steam i/p, if excitation is increased then  $pf$  —?,  $I_a$  —?,  $\delta$  —? and  $P$  —?,  $Q$  —?

Ans:

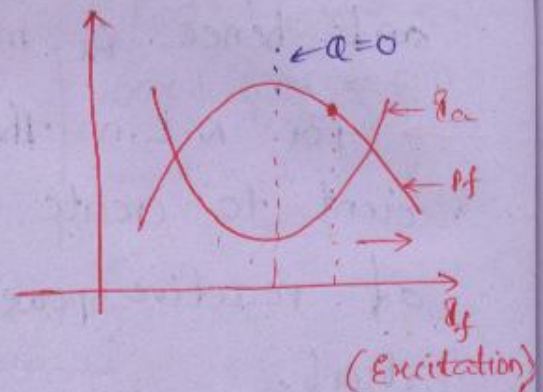
$pf$  : decreases

$I_a$  : increases

$\delta$  : decreases

$Q$  : DELIVER, increases

$P$  : const.



Q. An Alt. operating on  $\delta BB$ , at leading pf with fixed steam i/p, if the excitation is increased then  $pf$  —?,  $I_a$  —?,  $\delta$  —?,  $P$  —? and  $Q$  —?

Ans:

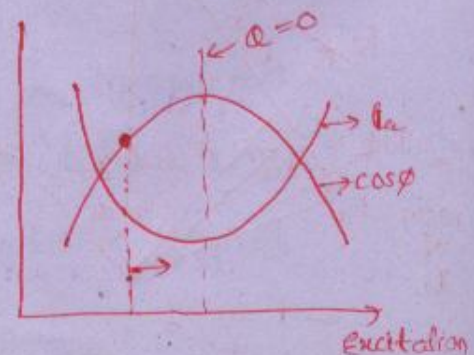
$pf$  : increases

$I_a$  : decreases

$\delta$  : decreases

$Q$  : ABSORB, decreases

$P$  : const.





Q. In the above question, if the excitation is decreased then?

Ans:

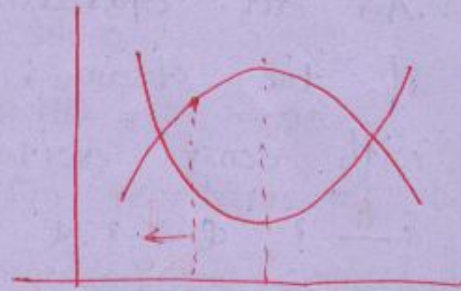
$P_f$  : decreases

$I_a$  : increases

$\delta$  : increases

$Q$  : ABSORB, increases

$P$  : const.



Q. An Alt. operating on 8BB at vpf. with fixed steam i/p, excitation increases then m/c will

(a). absorb  $Q$ , operating at lagging pf

(b). " , operated at leading pf

(c). deliver  $Q$ , operated at lagging pf

(d). " , operated at leading pf

Effect of change in steam i/p :-

[ excitation is kept constant ] :-

⇒ Arm. current always increases as steam i/p or load increases with const. excitation, whether it may operating at lagging or leading pf region.

\*  $\text{current} \propto \text{steam i/p} \propto \text{load}$

⇒ At max. power developed condi. an alternator will always operate at leading pf, a syn motor is always operated at lagging pf when the



m/c is operating on EBB.

Q. An alt. operating on EBB at lagging pf, if the steam i/p or load is increased with const. excitation then pf  $\uparrow$ ?,  $E_a$   $\uparrow$ ?,  $\delta$   $\uparrow$ ?,  $Q$   $\downarrow$ ?, &  $P$   $\uparrow$ ?

$$P \propto \sin \delta$$

$$\delta \uparrow \Rightarrow \sin \delta \uparrow$$

$$\Rightarrow P \uparrow$$

Q. An alt. operating on EBB, at leading pf, if the steam i/p or load is increased with const. excitation then pf  $\downarrow$ ?,  $E_a$   $\uparrow$ ?,  $\delta$   $\uparrow$ ?,  $Q$   $\uparrow$ ?, &  $P$   $\uparrow$ ?

Q. An alt. operating on EBB at upf, if the load is reduced to 50% (half) then the m/c will operate —?

- (a). lagging pf (b). leading pf (c). upf  
(d). depends on m/c parameters.

Q. An alt. operating on EBB at lagging pf. If the steam i/p (or load) is decreased with const. excitation then pf  $\downarrow$ ?,  $E_a$   $\downarrow$ ?,  $\delta$   $\downarrow$ ?,  $Q$   $\uparrow$ ?, &  $P$   $\downarrow$ ?

Q. An alt. operating on EBB with a load angle of  $30^\circ$ . if the load is doubled then its load angle —?

- (a).  $30^\circ$  (b).  $60^\circ$  (c).  $45^\circ$  (d).  $90^\circ$ .

$$P \propto \sin \delta$$

$$\frac{P_2}{P_1} = \frac{\sin \delta_2}{\sin \delta_1} \Rightarrow \frac{2}{1} = \frac{\sin \delta_2}{\sin 30}$$

$$\Rightarrow \sin \delta_2 = \frac{1}{\cancel{0.5}} \Rightarrow \delta_2 = 90^\circ$$

**Q.** A 3- $\phi$  turbo alt. with syn. reactance of  $10 \Omega$  per ph. and negligible arm resistance is connected to 11 kV const. volt, const freq bus bar and supplies 100 A at upf to the system. with the turbine power kept const and excitation of alt. is increased by 25%.

(a). The new load angle will be —?

- (1).  $8.94^\circ$  (2).  $7.14^\circ$  (3).  $58.4^\circ$  (4).  $4.12^\circ$

(b). The new current is —?

- (1). 190.6 A (2). 100 A (3). 125 A (4). 330.2 A

(c). The pf is —?

- (1). 0.524 lag (2). 0.524 lead (3). upf (4). 0.86 lead

**Sol:**

3- $\phi$  turbo,  $X_s = 10 \Omega/\text{ph}$ ,  $R_a = 0$

11 kV 4BB,  $I_a = 100 \text{ A}$ , upf.

Steam i/p const. & Excitation  $E' = 1.25 E$

Then  $\delta' = ?$ ,  $I_a' = ?$  & pf = ?

$$V_{ph} = \frac{11 \times 10^3}{\sqrt{3}} = 6350 \text{ V}$$

$$E = V \angle 0 + I_a \angle \pm \phi \cdot Z_s \angle \theta$$

$$= 6350 \angle 0 + 100 \angle 0^\circ \times 10 \angle 90^\circ$$

$$= 6429 \angle 8.94^\circ$$



$$\Rightarrow E' = 1.25 E$$

$$= 1.25 \times 6429 = 8035 \text{ V}$$

$$\Rightarrow E' \sin \delta' = E \sin \delta$$

$$\Rightarrow \sin \delta' = \frac{E}{E'} \sin \delta$$

$$= \frac{1}{1.25} \sin 8.94 =$$

$$\Rightarrow \delta' = 7.14^\circ$$

$$I_a' = \frac{E' L \delta' - V L_0}{Z_s L_0}$$

$$= \frac{8035 [7.14 - 63.50 L_0]}{10 L_0}$$

$$= 190.54 \angle -58.4^\circ$$

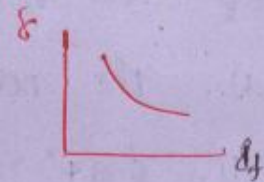
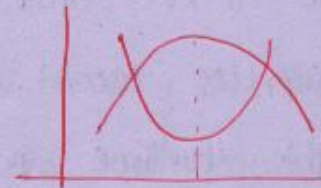
$$\therefore I_a' = 190.54 \text{ A}$$

$$\text{pf} = \cos (-58.4) = 0.54 \text{ lag.}$$

steam i/p const.

$\Rightarrow$  active power const.

$\Rightarrow E \sin \delta = \text{const}$



Q. A 6600 V, 1200 kVA AL. has reactance of 25% and is delivering FL at 0.8 pf lagging. It is connected to const. freq. bus bar. If the steam supply is gradually increased—

(1). The current at which pf to be unity

- (a) 645 (b) 252.96 A (c) 70.25 (d) 252 A

(2). The pf at which power o/p to be max—

- (a) 0.8 lead (b) 0.759 lead (c) 0.759 lag  
(d) 0.8 lag

(3). The max power o/p appr. without loosing synchronism

(a). 4.69 MW (b). 12 MW (c). 3.6 MW (d). 4 MW.

Sol:

6600 V, 1200 KVA,  $\theta_a X_s = 0.25$ , FL at 0.8 lag

$$V_{ph} = \frac{6600}{\sqrt{3}} = 3810 \text{ V}$$

$$I_L = \frac{\text{KVA}}{\sqrt{3} \cdot V_L} = \frac{1200 \times 10^3}{\sqrt{3} \times 6600} = 105 \text{ A} = I_{ph} = I_a$$

$$\theta_a X_s = 0.25 \text{ V}$$

$$\rightarrow 105 X_s = 0.25 \times 3810 \Rightarrow X_s = 9.07 \Omega$$

$$E = V \angle 0 + I_a \angle \pm \theta \cdot Z_s \angle \theta$$

$$= 3810 \angle 0 + 105 \angle -36.87^\circ \times 9.07 \angle 90^\circ$$

$$= 4447 \angle 9.86^\circ$$

For UPF,  $E \cos \delta = V$ . (∵ Excitation const.)

$$\Rightarrow E' \cos \delta' = V$$

$$\Rightarrow 4447 \cos \delta' = 3810$$

$$\Rightarrow \delta' = 31.06^\circ$$

$$I_a' = \frac{E \angle \delta' - V \angle 0}{Z_s \angle 0}$$

$$= \frac{4447 \angle 31.06^\circ - 3810 \angle 0}{9.07 \angle 90^\circ}$$

$$= 252.96 \angle 0.014^\circ$$

At  $P_{max}$ ,  $\delta = 90^\circ$ .

$$I_a \text{ at } P_{max} = \frac{E \angle 90^\circ - V \angle 0}{Z_s \angle 0}$$

$$= \frac{4447 \angle 90^\circ - 3810 \angle 0}{9.07 \angle 90^\circ} = 645.48 \angle +40.5^\circ$$



$$\text{pf at } I_{\max} = \cos 40.5 = 0.76 \text{ lead}$$

$$I_{\max} = \frac{3 EV}{X_s} \cdot \sin \delta$$

$$= \frac{3 \times 444.7 \times 3810}{9.07} \cdot \sin 90^\circ$$

$$= 5.6 \text{ MW.}$$

TVE.  
04/11/08.

### Synchronous Motors

⇒ The speed of a syn. motor can be controlled by varying frequency, to maintain the flux at rated value voltage also controlled. i.e.  $\frac{V}{f}$  ratio control.

Q. The direction of rotation of syn. motor can be reversed — ?

- (a). by changing field polarity
- ✓ (b). by changing the ph. seq.
- (c). both a & b
- (d). dire. of rotation can't be reversed.

Q. The speed of the syn. motor can be controlled by — ?

- (a). freq. (b). voltage (c). a & b (d). none.

⇒ Dire. of rotation can be reversed only by changing the ph. seq but not by the field polarities.

Q. In syn motors  $T_{st} = 0$ .

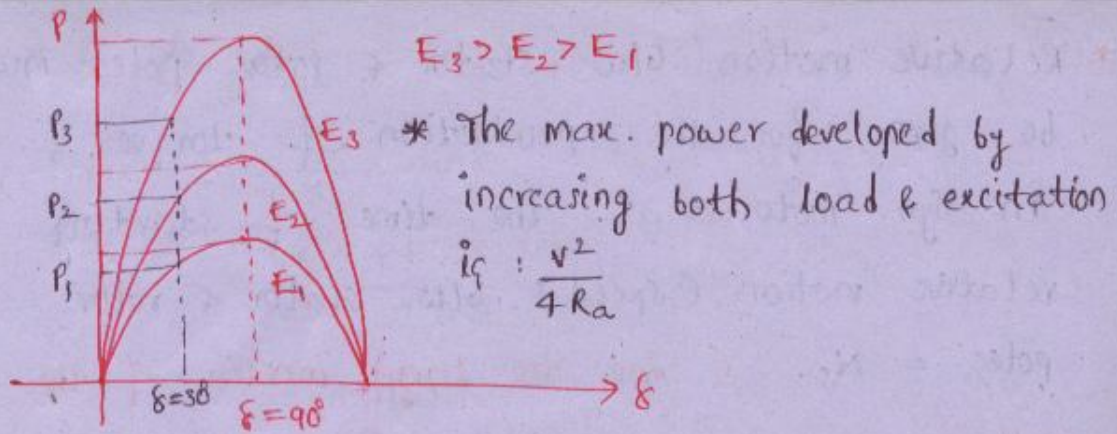
$$\text{So } \frac{T_{st}}{T_{fl}} = 0 \quad \& \quad \frac{T_{fl}}{T_{st}} = \infty.$$

\* Relative motion b/w stator & rotor poles must be zero for the production of torque.

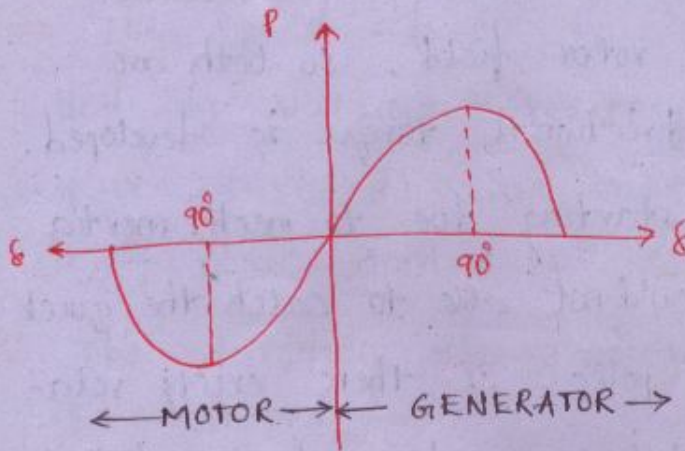
In syn. motor at the time of starting relative motion (speed) b/w stator & rotor poles =  $N_s$ . (due to large inertia of the rotor).

Under running condi, there is no relative motion b/w stator & rotor field, so both are stationary so unidirectional torque is developed. At the time of starting due to mech. inertia of rotor, rotor could not able to catch the quick reversal of stator poles.  $\therefore$  there exists relative motion b/w stator & rotor poles  $\therefore$  torque is zero, hence syn. motor is not self starting. It can be started by applying external force to overcome the inertia. The motor is driven near to  $N_s$ , by the time inertia is overcome and then by giving the excitation, motor will rotate at  $N_s$  due to magnetic locking.





power angle curves:

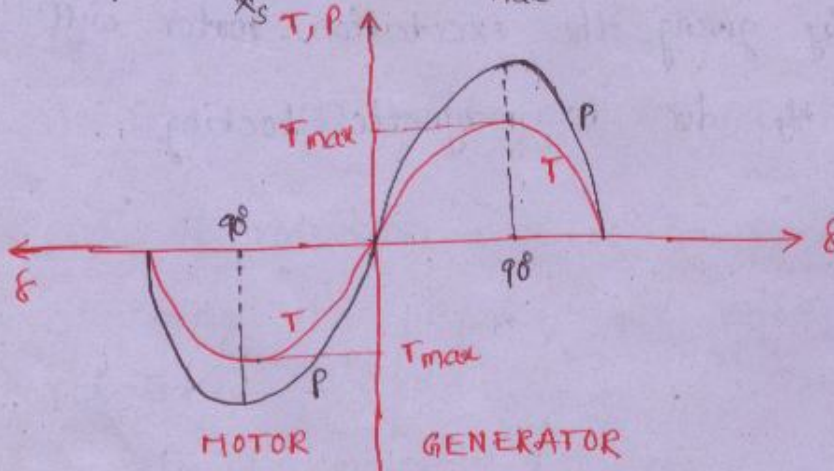


$$T = \frac{P}{\omega}$$

$$= \frac{\frac{EV}{X_s} \cdot \sin \delta}{\omega} = \frac{EV}{X_s \cdot \omega} \cdot \sin \delta$$

$$\Rightarrow T = T_{\max} \cdot \sin \delta$$

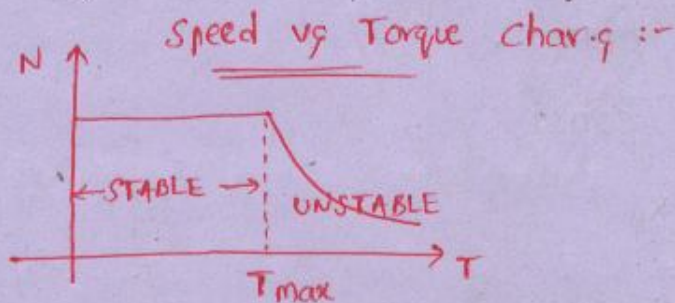
$$P = \frac{EV}{X_s} \cdot \sin \delta = P_{\max} \cdot \sin \delta$$



Maximum torque / breakdown torque / pull out torque / stalling torque.

• Max. torque / pull out torque:

It is the max. torque, that can be developed by a syn. motor without losing its synchronism.



NOTE:

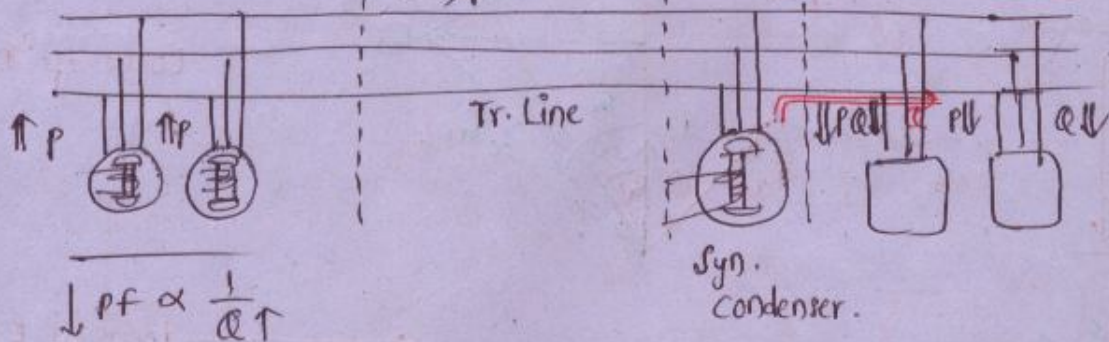
~~Flucting~~ occur for normal excitation under NL condi. only.

OVER EXCITED SYN. MOTOR UNDER NO LOAD :-

deliver LAG. KVAR.

$\Rightarrow Q$   
 $\Rightarrow P$

Improvement of pf:



\* over excited syn. motor under NL condi. is used as syn. condenser to improve the pf.

\* An under excited syn. motor under NL condi behaves as an inductor and used to depvove the pf such that voltage profile is maintained.



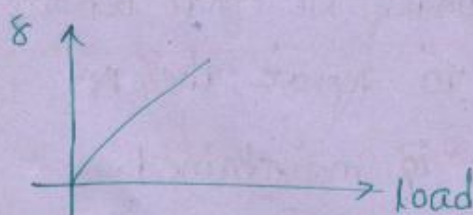
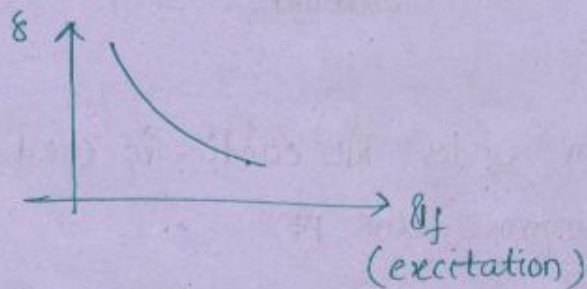
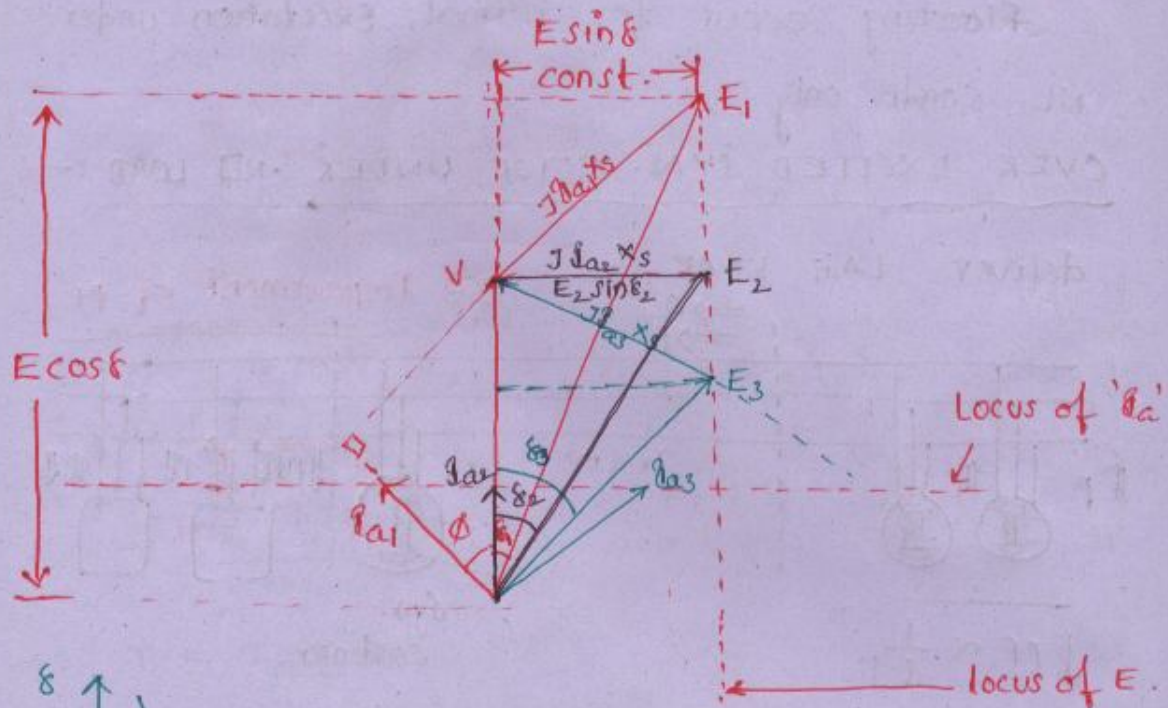
Effect of change in excitation  
with mech. load kept constant:-

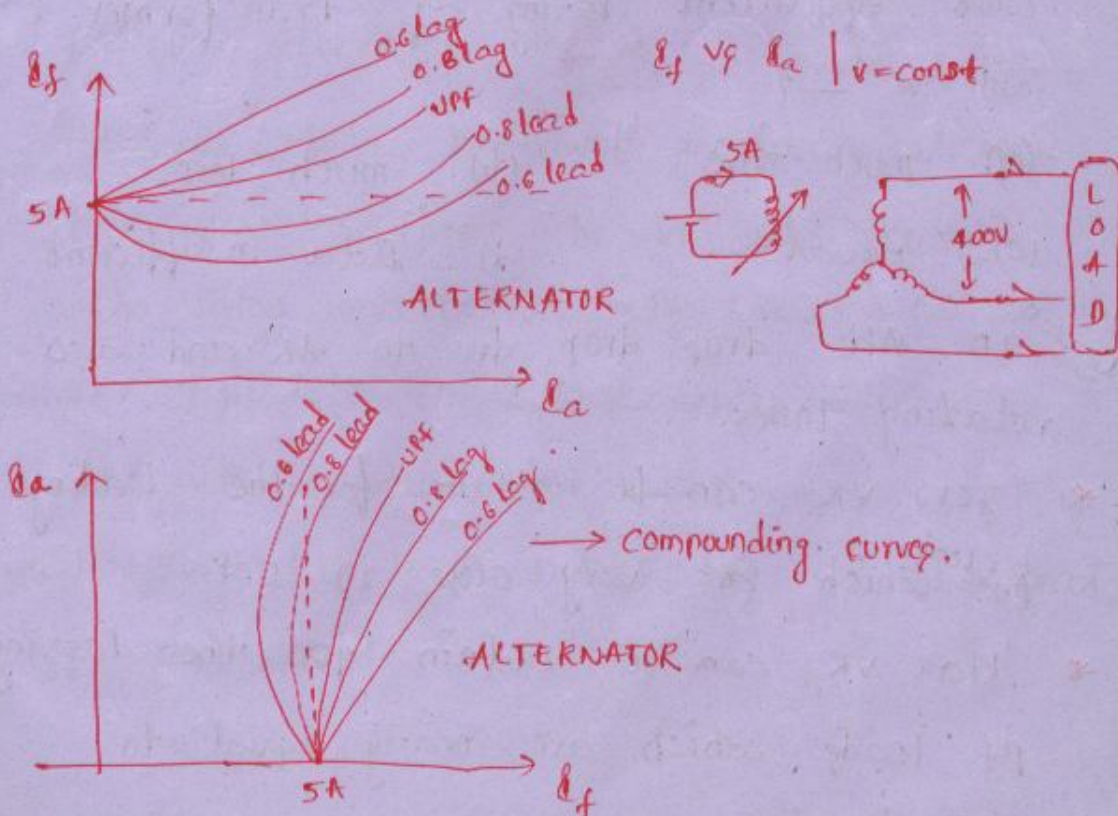
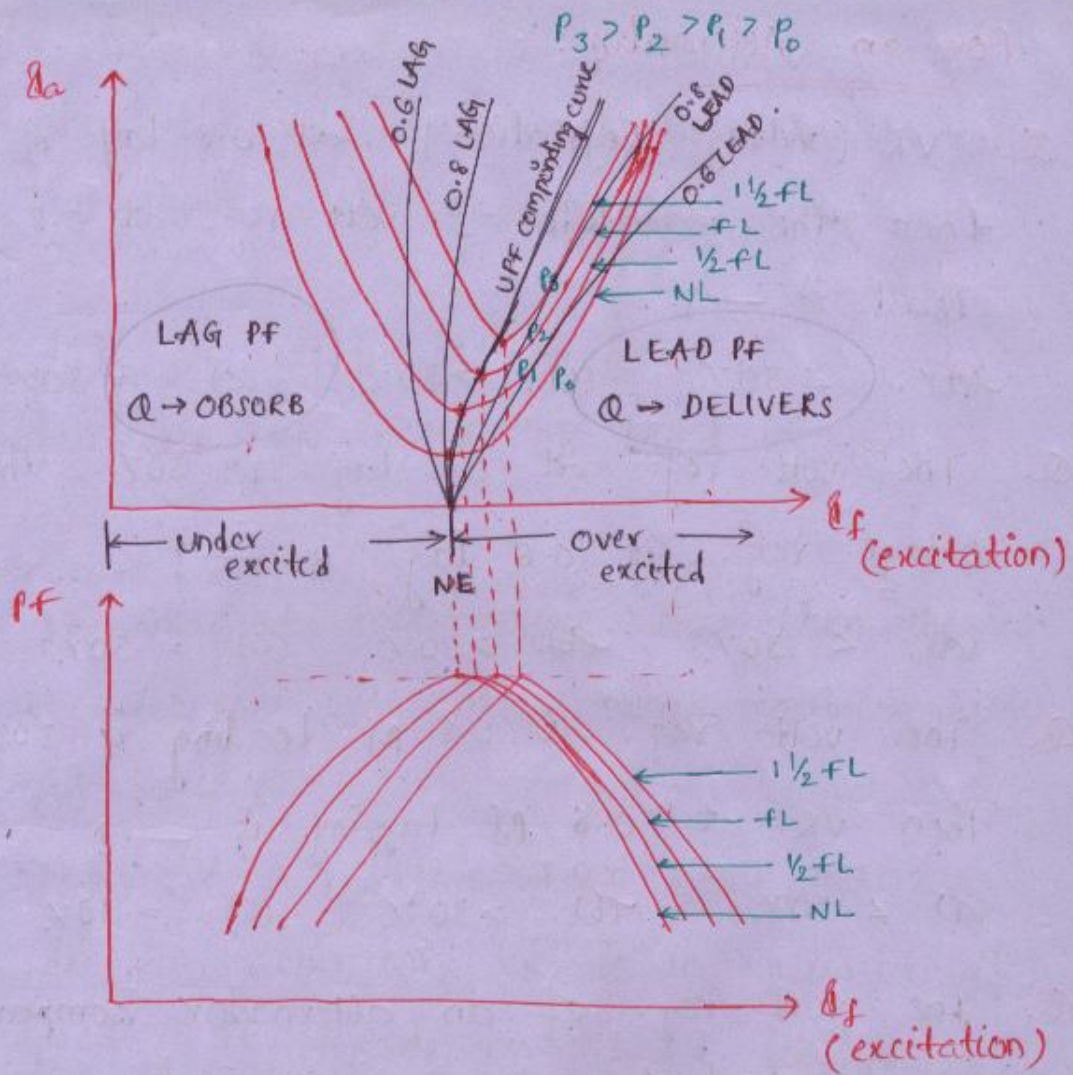
$$P \propto E \sin \delta = \text{const.}$$

$$P \propto I_a \cos \phi = \text{const.}$$

$$V = E + j I_a X_s$$

$$Q = \frac{V}{X_s} [V - E \cos \delta]$$







for an Alternator:

Q. VR (voltage Regulation) at 0.8 lag is 30%.  
then the magnitude of volt. reg. at 0.8  
lead is —?

- (a).  $< 30\%$  (b).  $> 30\%$  (c).  $= 30\%$

Q. The volt. reg. at 0.8 lag is 30%, the  
voltage reg. at 0.6 lag is —?

- (a).  $< 30\%$  (b).  $> 30\%$  (c).  $= 30\%$

Q. The volt. reg. at 0.8 pf leading is 30%.  
then VR at 0.8 pf lagging is —?

- (a)  $< 30\%$  (b).  $> 30\%$  (c).  $= 30\%$

Q. The volt. reg. of an alternator compared  
with equivalent rating of transformer  
will be —?

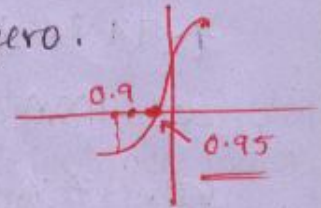
- (a). much more (b). much less  
(c). equal (d). Data insufficient

Reason: In Alt. drop due to AR and also  
rotating losses.

\* zero VR can be obtain for the leading  
pf loads which are very close to upf.

\* Max VR can be obtain for the lagging  
pf loads which are nearly equal to  
zpf lagging

Q. The VR at 0.95 pf load is zero.  
Then the VR at 0.9 pf load will be —?  
(a). +ve (b). -ve (c). zero.



Q. The VR at 0.8 pf lag is 12%.  
then the VR at 0.8 pf lead is —?  
(a).

Q. The VR at 1000 rpm is 20%. then the VR at 900 rpm with other things remaining same will be —?  
(a).  $< 20\%$  (b).  $> 20\%$  (c).  $= 20\%$ .

In Syn. Generator, VR is independent of speed. It depends on load & load pf.

In DC Generator,  $VR \propto \text{Speed}$

Q. The VR of a DC shunt generator at 1000 rpm is 10%. Then the VR at 1200 rpm with same excitation will be —?  
(a).  $> 10\%$  (b).  $< 10\%$  (c).  $= 10\%$ .

Q. The VR is max. for —?

(a). ZPF lag (b). 0.8 pf lag (c). 0.8 pf lead  
(d). ZPF lead



Q. A 1- $\phi$ , 2000V, alternator armature resistance and reactance are  $0.8 \Omega$  &  $4.94 \Omega$  res. Then the VR of alternator at 100A and 0.8 pf lead will be —?

- (a). 7% (b). -8.9% (c). 14% (d). 0%

$$E = \sqrt{(V \cos \phi + I_a R_a)^2 + (V \sin \phi - I_a X_s)^2}$$

$$= \sqrt{(2000 \times 0.8 + 100 \times 0.8)^2 + (2000 \times 0.6 - 100 \times 4.94)^2}$$

$$= 1823.86 \text{ V}$$

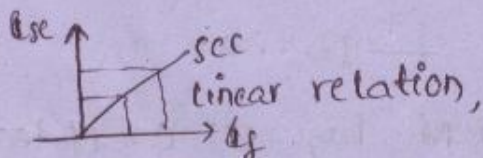
$$\therefore \% \text{ reg} = \frac{E - V}{V} \times 100$$

$$= \frac{1823.86 - 2000}{2000} \times 100$$

$$= -8.9\%$$

Q. The stc current at 1000 rpm at rated field current  $I_f = 2\text{A}$ , is 20A. The stc current at 900 rpm with a field current of 3A will be —?

- (a). 20A (b). > 20A (c). < 20A (d) 30A



$$2\text{A} \rightarrow 20\text{A}$$

$$3\text{A} \rightarrow ?$$

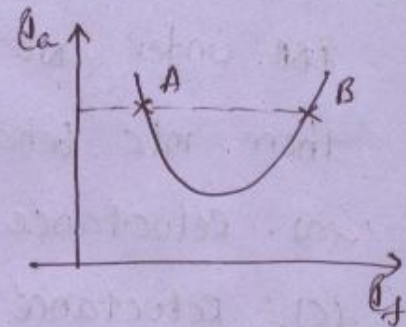
$$\Rightarrow \frac{3}{2} \times 20 = 30\text{A}$$

Q. A Syn. m/c operating at 0.8 under fl. condi. If excitation fails the m/c behaves as —?

- (a). Induction Generator (b). Syn. Generator  
(c). Reluctance Generator (d). Reluctance motor.  
Q. In Syn m/c. the m/c is more stable at —?

- (a) A (b) B (c) None.

But  $\eta$  at point B is little small when compare to A.  
b'coz of excitation losses.  
[ $\therefore I_f$  is more].



\* Synchronizing power is active in nature when the disturbance is in sudden change of load, sudden change in PM, or in supply system.

But  $P_{sy}$  is reactive in nature when there is sudden change in excitation.

Q. A Salient pole Syn. m/c operating on 0.8 under light load condi. acting as generator. If excitation fails then m/c behaves as —?

- (a). Induction generator. (b). Syn. generator.  
(c). Reluctance generator (d). Reluctance motor.



Q A Salient pole syn. generator operating on  $\delta BB$ , if PM fails then m/c will behave as —?

- (a). Syn. motor (b). Induction motor  
(c). Induction generator (d). Reluctance generator.

Q A Salient pole syn. motor operating on  $\delta BB$  under NL condi. If excitation fails then m/c behaves as —?

- (a). Reluctance motor (b). Induction motor  
(c). Reluctance generator (d). Syn. motor.

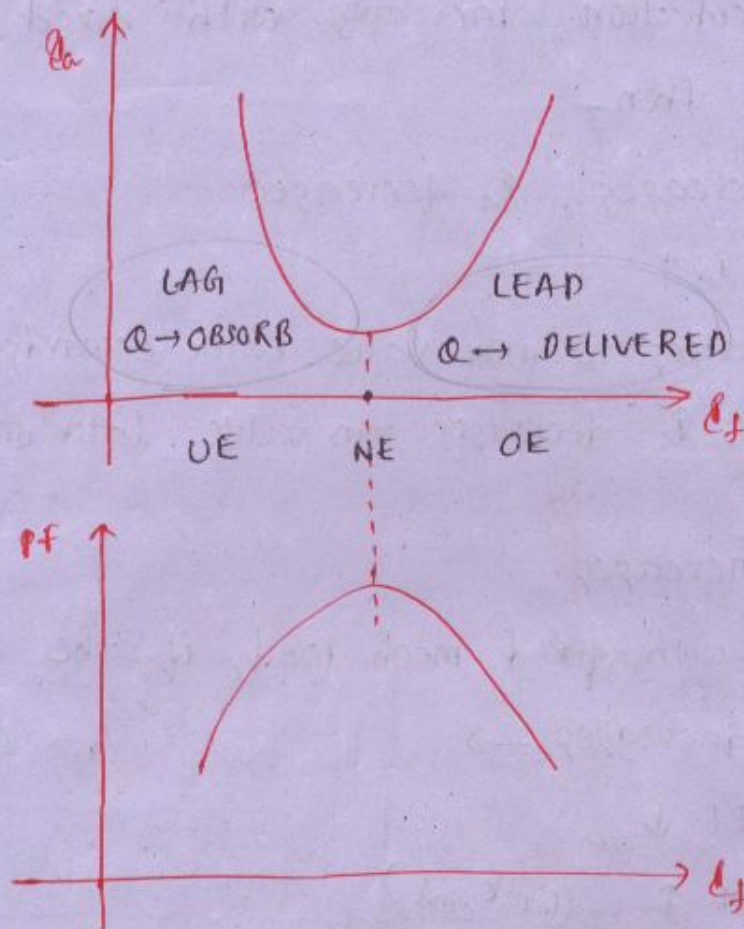
Q A Salient pole syn. motor under FL condi. operating on  $\delta BB$ . If excitation fails —? Then m/c will behave as —?

- (a). Reluctance motor (b). Induction motor  
(c). Syn. motor (d). would stop.

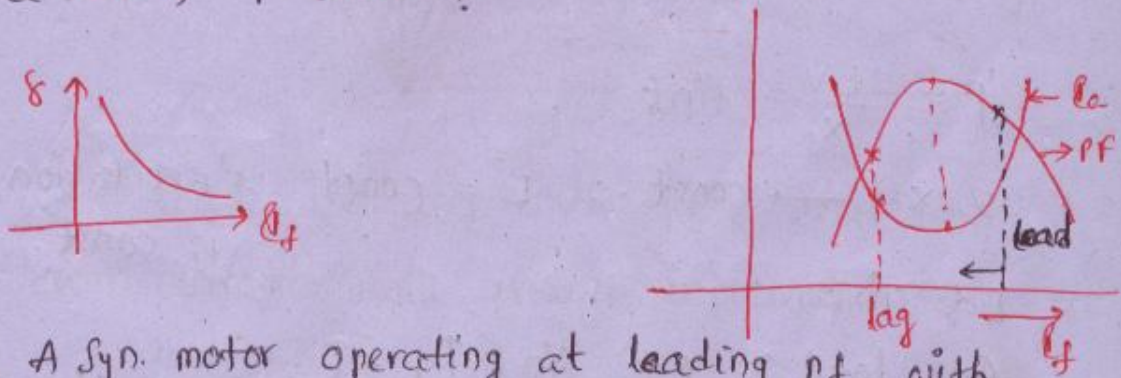
\* In all cases when excitation fails then m/c will absorb reactive power from the bus bar.  $\therefore$  m/c operated at poor pf, with large arm. current.

$\therefore$  Tripping is necessary after some delay

Syn. motor:



Q. A Syn. motor operating at lagging pf with fixed mech. load, if the excitation increases then PF  $\uparrow$ ,  $I_a$   $\downarrow$ ,  $\delta$   $\downarrow$ ,  $Q$  ABSORB  $\downarrow$ ,  $P$  const.?



Q. A Syn. motor operating at leading pf, with fixed mech. load, if excitation decreases then PF  $\uparrow$ ,  $I_a$   $\downarrow$ ,  $\delta$   $\uparrow$ ,  $Q$  DELIVER  $\downarrow$ ,  $P$  const.?



Q. A Syn. motor operating at lagging pf, if the excitation increases with fixed mech load then—

- (a). pf increases,  $I_a$  decreases
- (b). pf ↓,  $I_a$  ↑
- ✓(c). pf increases to max. value later onwards decreases,  $I_a$  decreases min value later onwards increases.
- (d). Both increases.

Q. Syn. motor with fixed mech. load, if the excitation decreases —

- (a).  $I_a$  ↑, pf ↓
- (b).  $I_a$  ↓, pf ↑ (back emf)
- ✓(c). induced emf ↓, load angle ↑
- (d). Both  $I_a$  & pf ↑.

EFFECT OF CHANGE IN MECH. LOAD:

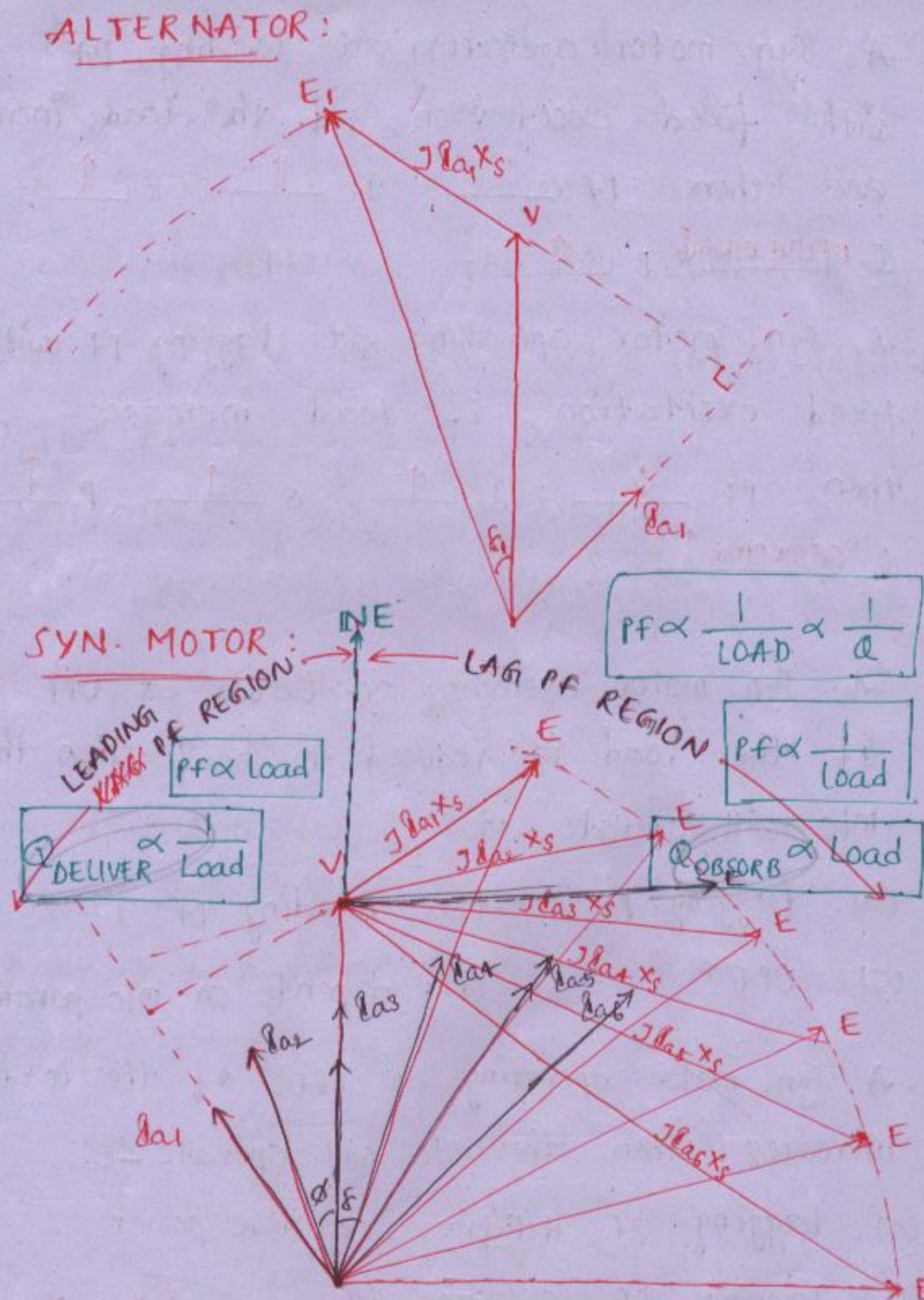
[ EXCITATION IS KEPT CONSTANT ] :-

$$P = \frac{EV}{X_s} \cdot \sin \delta$$

$V, X_s \rightarrow \text{const.}; E = \text{const} \therefore \text{excitation is const.}$

$$P \propto \sin \delta$$

As load ↑,  $P$  ↑,  $\sin \delta$  ↑,  $\delta$  ↑.





Q. A Syn. motor operating at leading pf with fixed excitation, if the load increases then pf  $\uparrow$ ,  $I_a$   $\uparrow$ ,  $\delta$   $\uparrow$ , Q ~~DELIVERING~~  $\downarrow$ , P  $\uparrow$  ?

Q. A Syn. motor operating at lagging pf with fixed excitation, if load increases then pf  $\downarrow$ ,  $I_a$   $\uparrow$ ,  $\delta$   $\uparrow$ , P  $\uparrow$  Q OBSORBING  $\uparrow$  ?

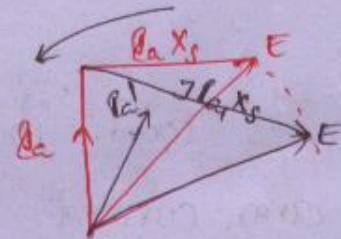
G107.

Q. A Syn. motor operating on busbar at UPF. If the load is reduced to half then the m/c will operate at

- (a). lagging pf (b). leading pf  
(c). UPF (d). depends on m/c parameters

Q. A Syn. motor operating at UPF, if the load increases then the m/c will operate -

- (a). lagging pf, delivering reactive power  
(b). lagging pf, absorbing Q.  
(c). leading pf, delivering Q  
(d). leading pf, absorbing Q



Q. The syn. reactance per ph. of a 3- $\phi$  Y-connected 6600V, syn. motor is  $20\Omega$ . The i/p is 915 kW at normal volt, induced line emf is 8942 V, the line current is —

- (a). 97 A (b). 56 A (c). 168 A (d) 80 A.

(ii). The pf — ?

- (a). 0.82 lag (b) 0.82 leading  
(c). 0 pf (d). 0.7 leading

Sol:  $X_s = 20\Omega/\text{ph}$

$V_L = 6600\text{ V}$

$P_{in} = 915\text{ kW}$

$E_L = 8942\text{ V}$

$\Rightarrow I_L = ? \text{ \& pf} = ?$

$P_{in} = \frac{EV}{X_s} \cdot \sin\delta$

$V_{ph} = \frac{6600}{\sqrt{3}} = 3810\text{ V}$

$E_{ph} = \frac{8942}{\sqrt{3}} = 5163\text{ V}$

(per ph.)  $P_{in} = \frac{EV}{X_s} \cdot \sin\delta$   
 $\frac{915 \times 10^3}{3} = \frac{5163 \times 3810}{20} \cdot \sin\delta$

$\Rightarrow \delta = 18^\circ$

$I_a = \frac{V_L \cos\delta - E_L \sin\delta}{Z_s}$

Alternator  
 $\Downarrow$

$I_a = \frac{E_L \sin\delta - V_L \cos\delta}{Z_s}$



$$I_{a_{ph}} = \frac{3810 \angle 0 - 5163 \angle -18}{20 \angle 90}$$

$$= 97 \angle 34.9^\circ = I_L$$

$$PF = \cos(34.9) = 0.82 \text{ lead}$$

Q. A 2000V, 3- $\phi$ , Y-connected syn. motor has an effective resistance and syn. reactance of  $0.2 \Omega$  &  $2.2 \Omega$  res. The i/p is 800 kw at normal volt & induced line voltage is 2500V.

(i). The line current is <sup>(a)</sup> 254 A

(b). 440 A (c) 231 A (d). 400 A

(ii). The pf is —

(a). 0.908 lagging (b). 0.908 leading

(c). 0.7 lagging (d). 0.7 leading

Sol: 
$$I_a = \frac{V \angle 0 - E \angle -\delta}{Z_s \angle \theta}$$

$$\rightarrow I_a^* = \frac{V}{Z_s} \angle \theta - \frac{E}{Z_s} \angle \theta + \delta$$

$$P = \frac{V^2}{Z_s} \cos \theta - \frac{EV}{Z_s} \cos(\theta + \delta)$$

$$V = 2000 \text{ V, } 3-\phi, Y, R_a = 0.2 \Omega$$

$$X_s = 2.2 \Omega, P_{in} = 800 \text{ kW, } E_L = 2500 \text{ V}$$

$$I_L = ? \text{ \& } PF = ?$$

$$V_{ph} = \frac{2000}{\sqrt{3}} = 1154 \text{ V}$$

$$E_{ph} = \frac{2500}{\sqrt{3}} = 1443 \text{ V}$$

$$Z_s = 0.2 + j2.2 = 2.2 \angle 84.8^\circ$$

$$P_{in} = \frac{V^2}{Z_s} \cos \theta - \frac{EV}{Z_s} \cos(\theta + \delta)$$

$$\Rightarrow \frac{800 \times 10^3}{3} = \frac{1154^2}{2.2} \cos(84.8) - \frac{1443 \times 1154}{2.2} \cos(84.8 + \delta)$$

$$\Rightarrow \delta = 21.4^\circ$$

$$\begin{aligned} I_{a_{ph}} &= \frac{VL - E \cos \delta}{Z_s \sin \delta} = \frac{1154 \angle 0 - 1443 \angle -21.4}{2.2 \angle 84.8} \\ &= 254.3 \angle 24.49^\circ \\ &= 254.3 \text{ A} = I_L \end{aligned}$$

$$\begin{aligned} \text{pf} &= \cos(24.49^\circ) \\ &= 0.908 \text{ leading.} \end{aligned}$$

Q. A 230V, 4 pole, 50Hz, Y-connected syn.

motor has an impedance of  $(0.6 + j3)\Omega/\text{ph}$ .

Its field current is so adjusted that motor draws 10A at UPF from rated voltage source. with the field current unchanged the load on the m/c is increased till it draws 40A from the supply

(1). The operating pf —?

(a). UPF (b). 0.954 lag (c). 0.954 lead

(d). 0.603 lag.



(ii). The torque developed —?

(a). 65.3 Nm (b). 26.5 Nm (c). 78.45 Nm

(d). 45.3 Nm.

Sol:

A 230V, 4-pole, 50Hz, star,

$Z_s = (0.6 + j3) \Omega/\text{ph}$  motor draws 10A

at vrf, with field current unchanged  
ie same the load on the m/c is increased

till  $I_a = 40 \text{ A}$  Then  $\text{Pf} = \text{---?}$   $T = \text{---?}$

$$V_{ph} = \frac{230}{\sqrt{3}} = 132 \text{ V}$$

$$Z_s = 3.054 \angle 78.6^\circ$$

$$I_a = 10 \text{ A, vrf, } E = V \angle 0 - I_a \angle \phi \cdot Z_s \angle \theta$$

$$\Rightarrow E = 132 \angle 0 - 10 \angle 0 \times 3.054 \angle 78.6$$

$$= 130.3 \angle -13.31^\circ$$

$$E' = E \quad \therefore \text{excitation const.}$$

$$E' = E, I_a' = 40 \text{ A} \Rightarrow \text{Pf} = \text{---}$$

$$I_a Z_s = V - E$$

$$= \sqrt{V^2 + E^2 - 2VE \cos \delta}$$

$$\Rightarrow 40 \times 3.054 = \sqrt{132^2 + 130.3^2 - 2 \times 132 \times 130.3 \cos \delta}$$

$$\Rightarrow \delta = 55.5^\circ$$

$$I_a' = \frac{V \angle 0 - E' \angle -\delta}{Z_s \angle \theta}$$

$$= \frac{132 \angle 0 - 130.3 \angle -55.5}{3.054 \angle 78.6} = 40 \angle -17^\circ$$

$$PF = \cos 17^\circ = 0.95 \text{ lag.}$$

$$\begin{aligned} P_{in} &= 3 V_{ph} \cdot I_{ph} \cdot \cos \phi \\ &= 3 \times 132 \times 40 \times 0.95 \\ &= 15.04 \text{ kW} \end{aligned}$$

$$\begin{aligned} P_{out} &= P_{in} - \text{cu loss} \\ &= 15.04 - 3(40)^2 \times 0.6 \\ &= 12.16 \text{ kW} \end{aligned}$$

$$T = \frac{P_{out}}{\omega} = \frac{12.16 \times 10^3}{2\pi \times \frac{1500}{60}} = 77.41 \text{ Nm}$$

Q.08

A Syn. motor is connected to 800 V at 1 pu voltage and draws 0.6 pu current at 0.8 pf. Its syn. reactance is 1 pu and resistance is negligible.

(i). The excitation voltage  $E$  and load angle  $\delta$  will be res. ly

(a). 0.8 pu,  $36.86^\circ$  lag (b). 0.8 pu,  $36.86^\circ$  lead

(c). 1.17 pu,  $30.96^\circ$  lead (d). 1.17 pu,  $30.96^\circ$  lag

(ii). keeping the excitation voltage same, the load on the motor increased such that the motor current increased by 20%.

The operating pf become (a). 0.995 lag,

(b). 0.995 lead (c). 0.791 lag (d). 0.848 lead



sol:  $V = 1.0 \text{ pu}$ ,  $I_a = 0.6 \text{ pu}$  at  $\text{Vpf}$

$$X_s = 1 \text{ pu}, R_a = 0.$$

(i)  $E = ?$  (ii).  $E' = E$ ;  $I_a' = 1.2 I_a$ ,  $\text{PF} = ?$

$$E = V - I_a Z_s$$

$$= 1 \angle 0 - 0.6 \angle 0 \times 1 \angle 90$$

$$= 1.17 \angle -30.96$$

$$= 1.17 \text{ pu and } 30.96 \text{ lag.}$$

(ii).  $E' = E = 1.17 \text{ pu}$

$$I_a' = 1.2 \times 0.6 = 0.72 \text{ pu}$$

$$I_a Z_s = \bar{V} - \bar{E}$$

$$= \sqrt{V^2 + E^2 - 2VE \cos \delta'}$$

$$\Rightarrow 0.72 \times 1 = \sqrt{1^2 + 1.17^2 - 2 \times 1 \times 1.17 \cos \delta'}$$

$$\Rightarrow \delta' = 37.85^\circ$$

$$I_a' = \frac{V \angle 0 - E' \angle -\delta'}{Z_s \angle 0}$$

$$= \frac{1 \angle 0 - 1.17 \angle -37.85^\circ}{1 \angle 90^\circ}$$

$$= 0.72 \angle -6.23^\circ$$

$$\therefore \text{PF} = \cos 6.23^\circ$$

$$= 0.994 \text{ lag}$$

$$E = V - I_a Z_s$$

$$= \sqrt{V^2 + (I_a Z_s)^2 - 2V I_a Z_s \cos(\theta \pm \phi)}$$

Here  $I_a \angle \pm \phi, Z_s \angle \theta, V \angle 0$

$$\Rightarrow I_a \angle \pm \phi \cdot Z_s \angle \theta = I_a Z_s \angle \theta \pm \phi$$

G106

Q. A 3- $\phi$ , 400V, 5kW,  $\gamma$ -connected syn. motor having an internal reactance of  $10\Omega$  is operating at 50% load, upf. Now the excitation is increased 1%. What will be the new load in %, if pf is kept same, neglect all losses and consider linear magnetic circuit.

(a). 67.9% (b). 56.9% (c). 51% (d). 50%

Sol:

A 3- $\phi$ , 400V, 5kW, star

$X_s = 10\Omega$ , 50% load, upf.

Now the excitation increased by 1%

$$\Rightarrow E' = 1.01E$$

What will be the new load in %, for the pf is same as upf.

$$V_{ph} = \frac{400}{\sqrt{3}} = 231V$$

$$I_{fl} = \frac{5 \times 10^3}{\sqrt{3} \times 400 \times 1} = 7.21A$$

(b)  $\rightarrow$





Q. Two alternators of rating 200 kw, 300 kw working in parallel are driven by PM whose speed reg. curve are 3% & 5% res.ly

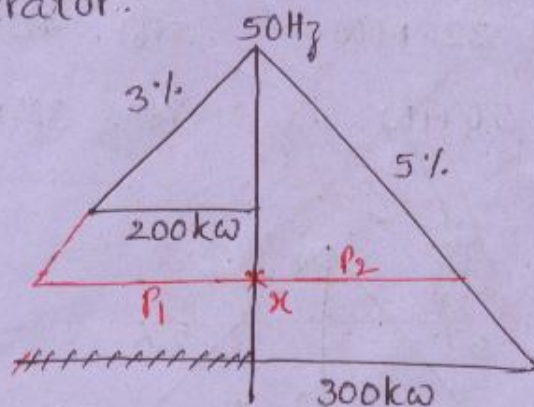
The governor setting gives NL speed for the two PM's a load of 190 kw will be shared by them res.ly

(a). 76 kw, (b). 114 kw, 76 kw  
114 kw

(c). 100 kw, 90 kw (d). 90 kw, 100 kw.

Sol:

- for proper sharing of load, the turbine should have drooping char.s.
- The active power sharing depends on mech. power i/p and turbine char.s (freq vs load char.).
- Reactive power sharing depends on the excitation and v- $\delta$  char.s (external char.s) of generator.



$$\frac{P_1}{200} = \frac{x}{3} \Rightarrow P_1 = 66.66x$$

$$\frac{P_2}{300} = \frac{x}{5} \Rightarrow P_2 = 60x$$



$$P_1 + P_2 = 190$$

$$\Rightarrow 66.66x + 60x = 190$$

$$\Rightarrow x = 1.5$$

$$\therefore P_1 = 66.66 \times 1.5 = 100 \text{ kW}$$

$$P_2 = 60 \times 1.5 = 90 \text{ kW}$$

$$100 \text{ — } 1.5$$

$$50 \text{ — } ?$$

$$\frac{50 \times 1.5}{100} = 0.75 \text{ Hz}$$

$$50 \times 0.015 = 0.75$$

$$\Rightarrow \frac{50}{100} \times 1.5 = 0.75 \text{ Hz}$$

$$\Rightarrow f = 50 - 0.75 = 49.25 \text{ Hz}$$

~~Two generators rated at 200 MW, 400 MW~~

Q. Two A/c's working parallel and supplying total load of 80 MW.

M/c-1: 40 MW with 5% speed reg.

M/c-2: 60 MW with 5% speed reg.

The total load sharing b/w m/c-1 & 2 res. by

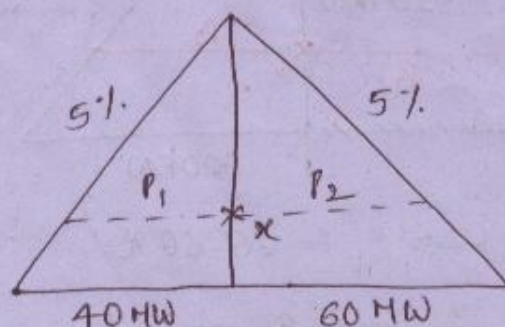
(a). 48 MW, 32 MW

(b). 40 MW, 40 MW

(c). 30 MW, 50 MW

(d). 32 MW, 48 MW

Sol:



$$\frac{P_1}{40} = \frac{x}{5} \Rightarrow P_1 = 8x$$

$$\frac{P_2}{60} = \frac{x}{5} \Rightarrow P_2 = 12x$$

$$P_1 + P_2 = 8x + 12x = 80$$

$$\Rightarrow x = 4$$

$$P_1 = 8 \times 4 = 32$$

$$P_2 = 12 \times 4 = 48$$

### CIRCLE DIAGRAMS:

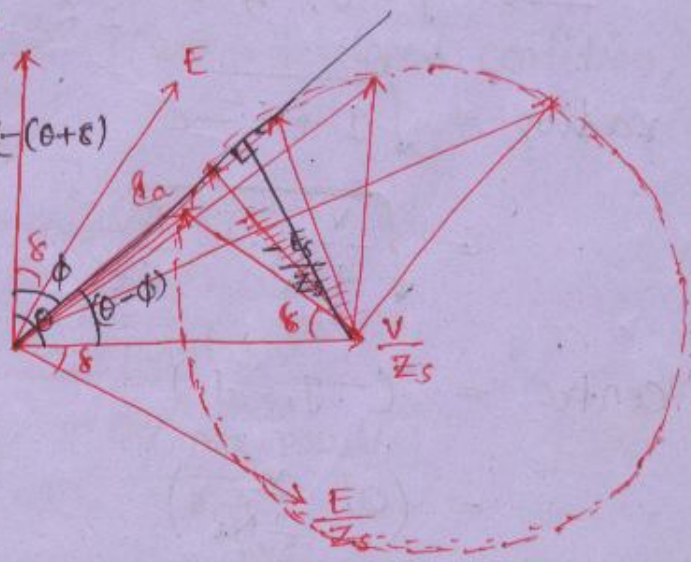
(1). Excitation ~~circle~~ circle  $\rightarrow$  Locus of arm. current  $I_a$ , with <sup>fixed</sup> excitation for variable loads.

(2). power circle  $\rightarrow$  Locus of arm. current  $I_a$ , with fixed load (or power) for variable excitation.

### EXCITATION CIRCLE :-

$$I_a = \frac{V \angle 0 - E \angle \delta}{Z_s \angle \theta}$$

$$= \frac{V}{Z_s} \angle (-\theta) - \frac{E}{Z_s} \angle (\theta + \delta)$$



\* Radius of the circle =  $\frac{E}{Z_s}$



$$\sin(\theta - \phi) = \frac{E/Z_s}{V/Z_s} = \frac{E}{V}$$

$$\sin(\theta - \phi) = \frac{E}{V}$$

where  $\phi$  is the pf angle at max. pf  
ie max pf =  $\cos \phi$ .

### POWER CIRCLE:

Mech. power developed,  $P_m = P_{in} - \text{arm. cu loss.}$

$$P_m = V I_a \cos \phi - I_a^2 R_a$$

$$I_a^2 = \frac{V}{R_a} I_a \cos \phi - \frac{P_m}{R_a}$$

$$(I_a \sin \phi)^2 + (I_a \cos \phi)^2 = \frac{V}{R_a} I_a \cos \phi - \frac{P_m}{R_a}$$

$$\text{Let } x = I_a \sin \phi$$

$$y = I_a \cos \phi$$

$$x^2 + y^2 - \frac{V}{R_a} y + \frac{P_m}{R_a} = 0 \rightarrow \text{eq. of circle.}$$

$$x^2 + y^2 + 2gx + 2fy + c = 0$$

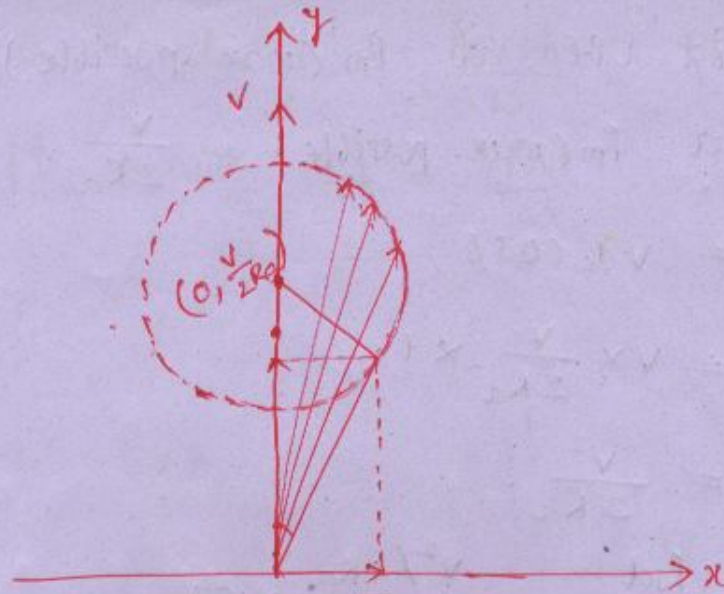
$$\rightarrow g = 0; f = -\frac{V}{2R_a}; c = \frac{P_m}{R_a}$$

$$\text{radius} = \sqrt{g^2 + f^2 - c}$$

$$= \sqrt{\frac{V^2}{4R_a^2} - \frac{P_m}{R_a}}$$

$$\text{centre} = (-g, -f)$$

$$= \left(0, \frac{V}{2R_a}\right)$$



$$\text{Radius} = \sqrt{\frac{V^2}{4R_a^2} - \frac{P_m}{R_a}}$$

As load increases,  $P_m \uparrow \Rightarrow \text{radius} \downarrow$

As load decreases,  $P_m \downarrow \Rightarrow \text{radius} \uparrow$ .

At NL condi,  $P_m = 0$ .

$$\therefore \text{Radius} = \sqrt{\frac{V^2}{4R_a^2} - 0}$$

$$= \frac{V}{2R_a}$$

NL Circle passes through origin.

At max. possible power developed condition,  
radius = 0.

$$0 = \sqrt{\frac{V^2}{4R_a^2} - \frac{P_m(\text{max. possible})}{R_a}}$$

$\therefore$  circle is a point i.e.:

$$\Rightarrow \frac{V^2}{4R_a^2} = \frac{P_m(\text{max. possible})}{R_a}$$

$$\Rightarrow P_m(\text{max. possible}) = \frac{V^2}{4R_a}$$



pf is UPF, at  $P_m$  (max. possible).

$$I_a \text{ at } P_m (\text{max. possible}) = \frac{V}{2R_a}$$

$$P_{in} = VI_a \cos \phi$$

$$= V \times \frac{V}{2R_a} \times 1$$

$$= \frac{V^2}{2R_a}$$

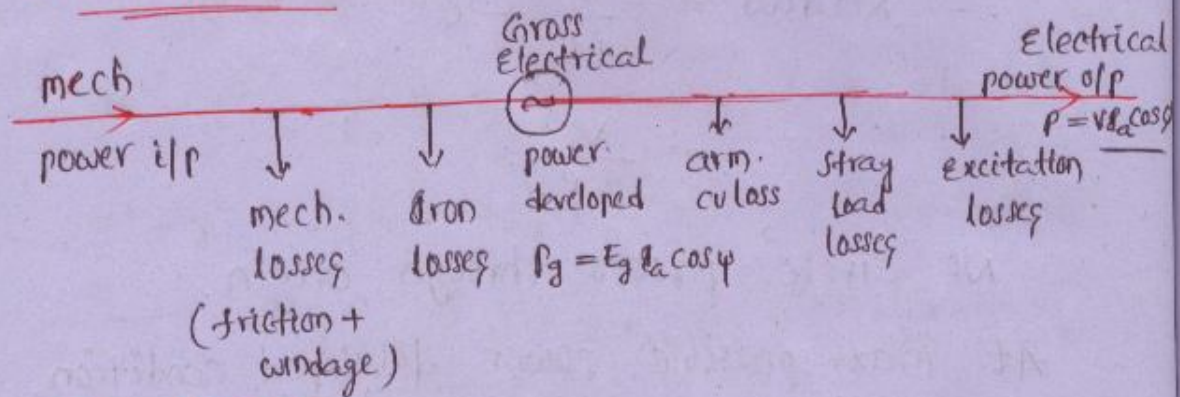
$$\eta = \frac{P_{out}}{P_{in}} = \frac{V^2/4R_a}{V^2/2R_a} \times 100$$

= 50%  $\rightarrow$  Efficiency at

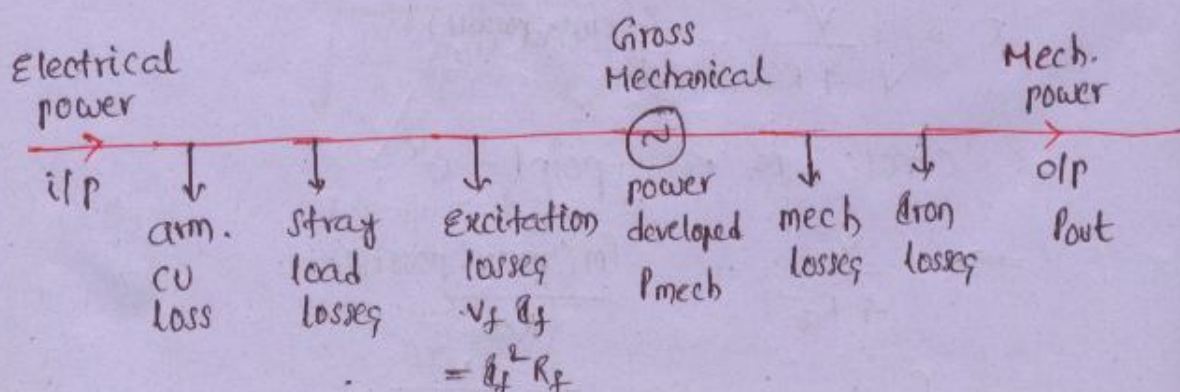
$P_m$  (max. possible).

### POWER STAGES:

#### ALTERNATOR:



#### SYN. MOTOR:



$$\rightarrow \text{Torque developed} = \frac{P_{\text{mech}}}{\omega} = \frac{E_b I_a \cos \phi}{\omega}$$

$$\rightarrow \text{shaft torque } T_{sh} = \frac{P_{\text{out}}}{\omega}$$

---



DC M/c's

03.  $I = \frac{12 \times 1000}{240} = 50 \text{ A}$

$$\frac{E_L}{E_\omega} = \frac{A_\omega}{A_L} \quad \& \quad \frac{I_L}{I_\omega} = \frac{A_L}{A_\omega}$$

power rating is const. [remain same]

EMF eq. of DC M/c :-

In dc m/c brushes collect the max. value  
 $\therefore$  flux distr. is a flat topped wave.

$$\begin{aligned} \therefore E &= E_{avg} = E_{max} = \sqrt{2} \times E_{rms} \\ &= \sqrt{2} \times \frac{\sqrt{2}\pi}{\pi} k_p k_d \phi f T \end{aligned}$$

$$\Rightarrow E = 2\pi k_p k_d \phi f T.$$

In dc m/c the arm. wdg is a full pitch  
 wdg.  $\therefore k_p = 1$ .

Arm. wdg is uniformly distributed  $\therefore$  EMF polygon  
 is a circle.  $\Rightarrow k_d = \frac{2}{\pi}$  [ $\because m_r = \pi$ ].

$$T_{path} = \frac{Z}{2} \times \frac{1}{A}$$

$$\begin{aligned} \Rightarrow E_{avg} &= 2\pi \times 1 \times \frac{2}{\pi} \times \phi \times \frac{PN}{120} \times \frac{Z}{2} \times \frac{1}{A} \\ &= \frac{\phi Z N}{60} \cdot \frac{P}{A} \end{aligned}$$

$$V = 220 \text{ V}; R_a = 1 \Omega.$$

$$I_a = \frac{V}{2R_a} = \frac{220}{2 \times 1} = 110 \text{ A} \leftarrow \text{Arm. current}$$

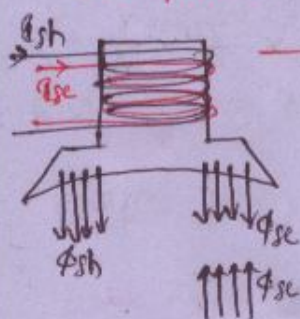
corr. to max. mech. power developed

At max. power developed condi. the  $\eta$  is nearly 50%.  $\therefore$  the m/c never be operated at max. power developed condi. b'coz due to large heating effect the insulation may spoil and arm wdg may get damage. All the m/c's are generally designed for max.  $\eta$  at rated power or load condition.

Shunt & Series dc m/c's :-

- \* Series field wdg cross section is more.  $R = \frac{\rho l}{A}$
- \* Shunt field wdg is made with more no. of turns with thin wire
- \* Series field wdg is made with less no. of turns with thick wire.
- \* The order of  $R_{sh} : 100 - 200 \Omega$   
 $R_{se} : 0.1 - 1 \Omega$
- \* The order of arm resistance is 1 or 2  $\Omega$ .
- \* Area CS (Series) > Area CS (arm) > Area CS (shunt)

Compound dc m/c's :-



→ Series field is placed on the top of shunt field since cu losses are more in series field so heat dissipation is effective.

- In long shunt, volt. reg is more when compared to short shunt with same terminal volt. b'coz series field wdg carries entire arm. current. b'coz generated volt. is more. Series flux is more in long shunt.



→ The generated volt. for long shunt connection is little more than the short shunt.

Volt. buildup in self excited dc m/c's :-

Magnetic Materials:

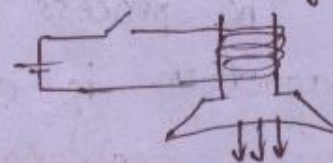
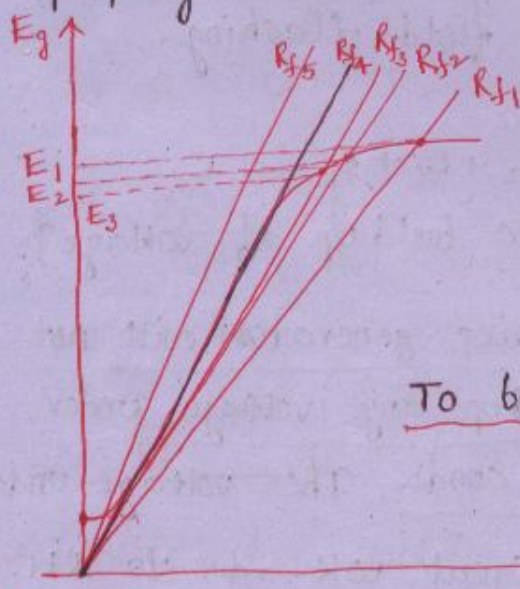
(1). Hard (2). Soft.

Hard → highly retentive.

Ex: Cobalt steel, Cobalt vanadium

Soft → cast steel, cast iron, Silicon steel.

Even field current is, they will possess some flux [ residual flux ] is called retentivity property.



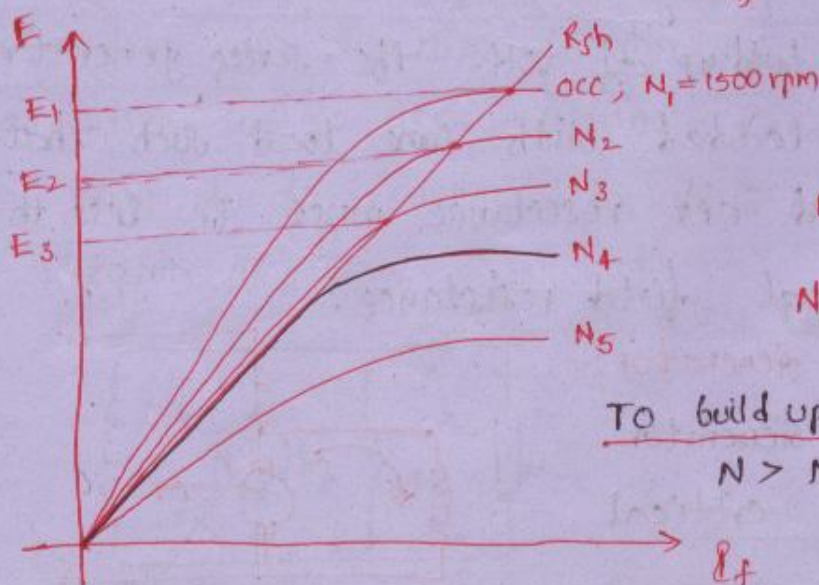
$$R_{f1} < R_{f2} < R_{f3} < R_{f4} < R_{f5}$$

$R_{f4} \rightarrow$  critical field resistance ( $R_c$ )

To build up of volt.:

$$R_f < R_c$$

$$\downarrow (R_{sh} + R_e)$$



$$\downarrow E \propto N \downarrow$$

$$N_1 > N_2 > N_3 > N_4 > N_5$$

$N_4 \rightarrow$  critical speed ( $N_c$ )

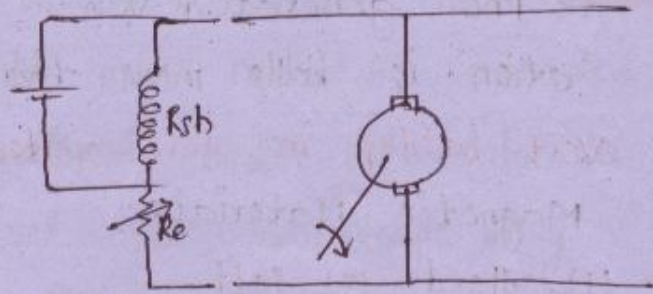
To build up of volt.:

$$N > N_c$$



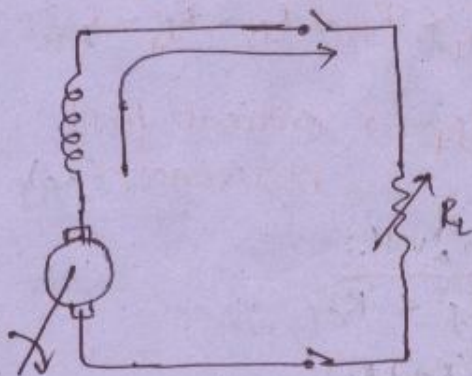
### field flashing :-

If the field terminals are not properly connected, the residual magnetism may be lost. To reestablish residual magnetism, the field wdg terminals are separated and excited with low volt. for some time. Then due to retentivity property the field poles, holds the residual magnetism.



The process of reestablishing the residual magnetism is called field flashing.

### Series Generator:



$$R_a + R_{se} + R_L < R_c$$

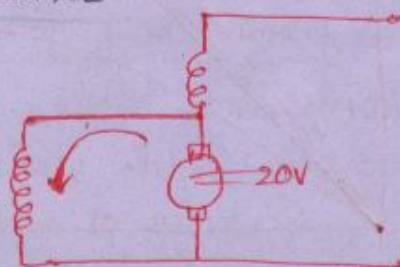
[To build up of voltage].

Series generator will not build up any voltage under NL condi. The voltage under

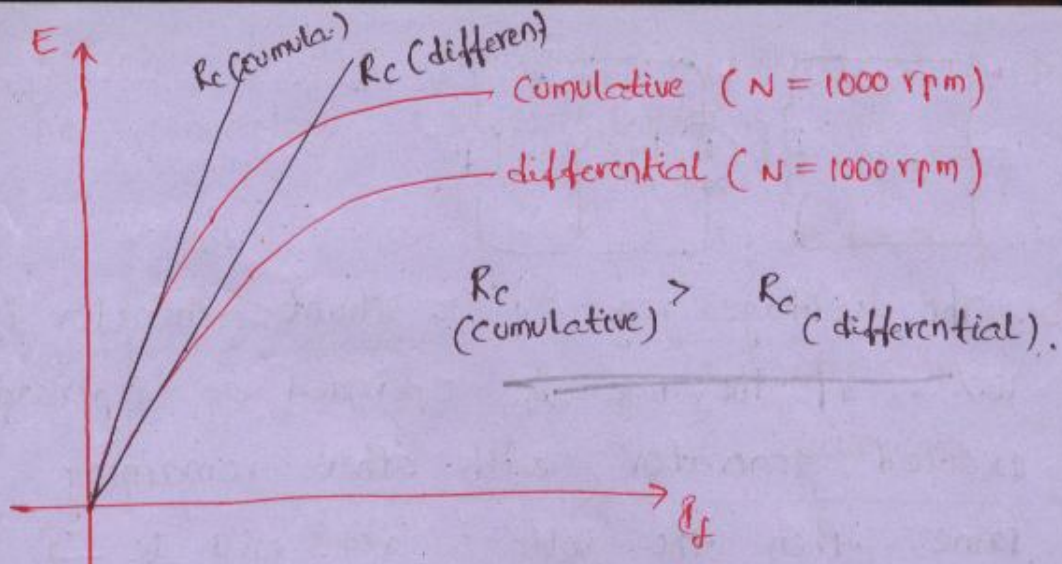
NL condi. is only a small volt. due to RH.  
for the build-up of volt. the series generator must be loaded with some load such that total field ckt resistance must be less than the critical field resistance.

### Compound Generator:-

Compound Generator having two critical resistances.







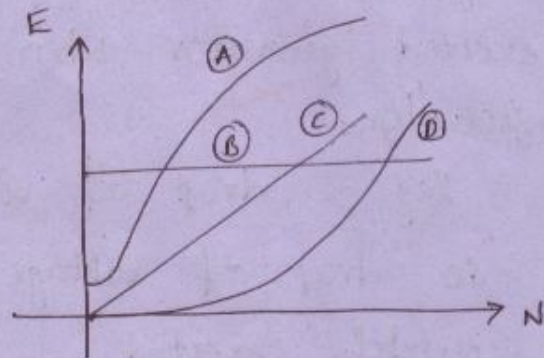
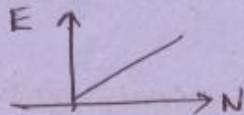
Q. which of the following char- $\phi$  represents voltage vs speed of DC shunt m/c.

(a). A (b). B

~~(c).~~ C (d). D.

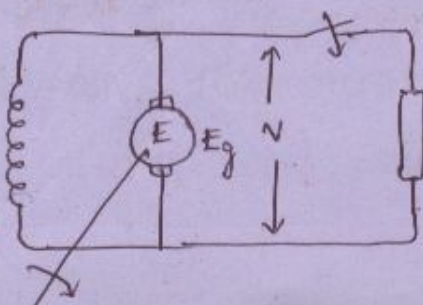
$$E = \frac{\phi Z N}{60} \cdot \frac{P}{A}$$

$$\Rightarrow E \propto N.$$



\* causes for voltage drop :

- (1). drop due to arm. reaction
- (2). drop due to arm. resistance,  $I_a R_a$  drop.
- (3). drop due to reduction in field current due to reason (1) & (2).

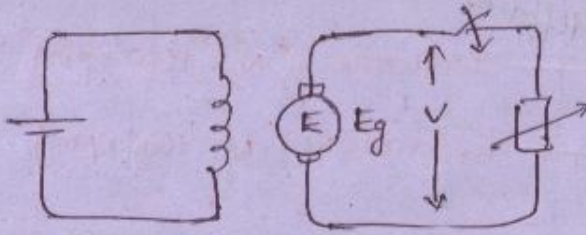


$$E = V + I_a R_a + \text{drop due to AR.}$$

$$= E_g + \text{drop due to AR.}$$

$$\therefore E_g = V + I_a R_a$$

$$I_{fb} = \frac{V}{R_{fb}}$$



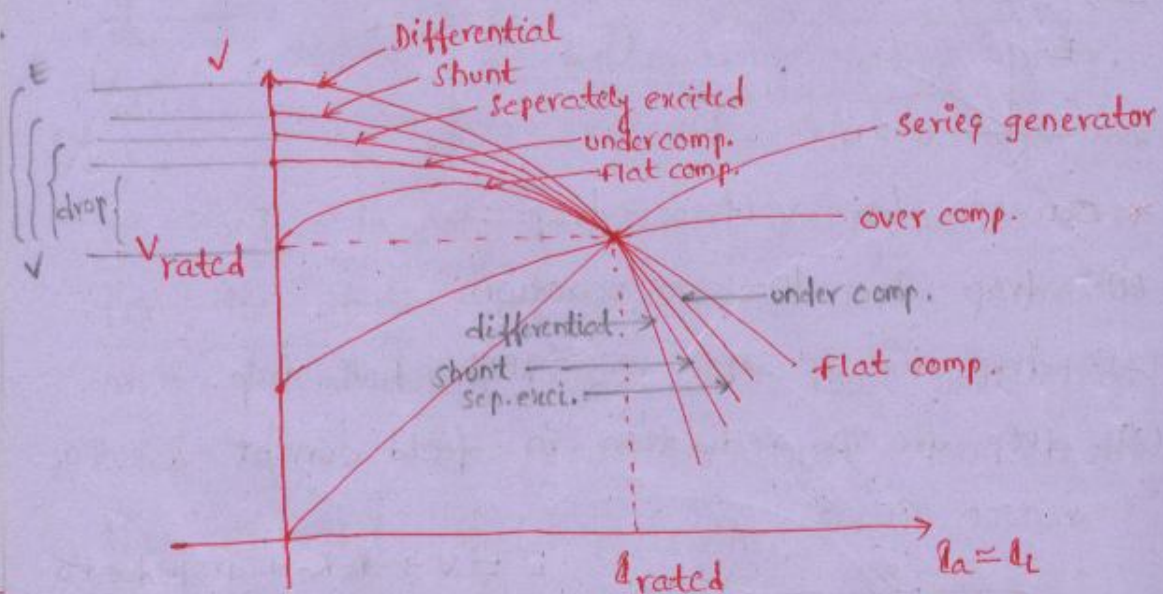
Q. The voltage reg. of a shunt generator is 10%. If the m/c is operated as separately excited generator, with other remaining same then the voltage reg. will be -?

- (a). reg. is 10%. (b)  $< 10\%$ . (c).  $> 10\%$ .

→ Regulation is better in case of separately excited generator when compared to shunt generator.

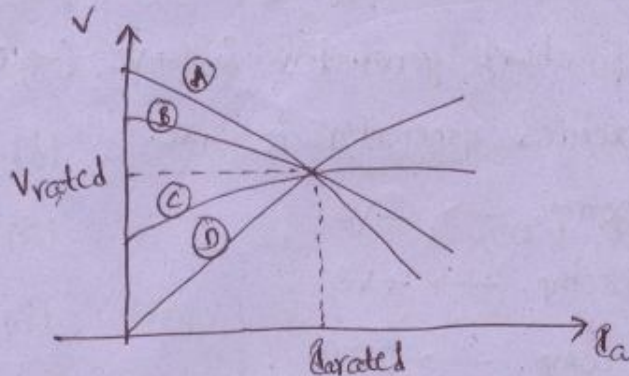
Reg  $\propto$  drop of voltage

so drop of voltage is less in case of separately excited.





Q. which of the following represents V-I char. DC generators. Match the following.



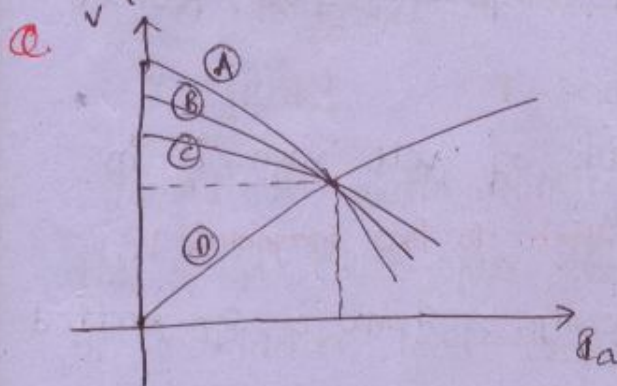
A : Differential

B : shunt

C : over comp.

D : series comp.

{ Series, over comp, differential, shunt }



A : shunt

B : series

C : diff

D : cumulative

### VOLTAGE REGULATION:

$$\frac{\text{NL voltage} - \text{FL voltage}}{\text{FL voltage}} = \frac{E - V}{V} \times 100$$

⇒ In DC generators volt. regn is proportional to speed.

∴ volt. regn ∝ speed.

But in syn. generator the volt. regn. is independent of speed, depends only on magnitude of load and load pf.

Q. The volt. reg. of a shunt generator at 1000 rpm is 10%. The volt. reg. at 1250 rpm will be —? (with other things remaining same).

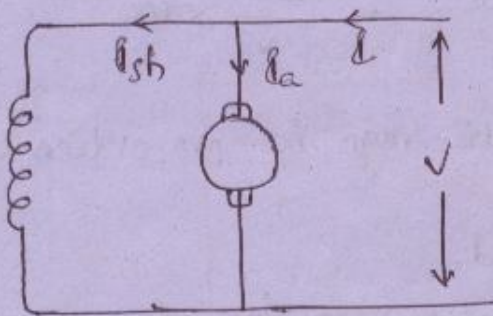
(a) < 10%      (b) = 10%      (c) > 10%

- The volt. regn. for series generator is  $-ve$  ( $\approx -100\%$ ) i.e. poorest regn. ( $-ve$  volt. regn.).
- The volt. regn. of shunt generator is  $+ve$  ( $< 10\%$ )
- The VR of sep. excited generator is  $+ve$ .
- The VR of over comp.  $\rightarrow -ve$ .
- The VR of under comp.  $\rightarrow +ve$
- The VR of flat comp.  $\rightarrow$  zero.
- The VR of differential comp.  $\rightarrow +ve$ , poorest  $+ve$  volt. regn.

\* The order of magnitude of volt. regn. is in descending order: (High to low magnitude).

Series  $>$  Diff.  $>$  over comp.  $>$  shunt  $>$  sep. excited  $>$  under comp.  $>$  flat comp.

### SHUNT MOTOR :



$$T \propto \phi I_a \Rightarrow +ve$$

$$T \propto (-\phi)(-I_a) \Rightarrow +ve.$$

- The dire. of rotation can be reversed by reversing either field or arm terminals but not both.
- If the supply terminals are changed then motor rotation can't be reversed.



Q. A shunt motor is running at rated speed, If the field ckt open then motor will

- (a). rotate at dangerously high speed
- (b). rotate at same speed
- (c). " " reduced speed
- (d). stops.

$$\uparrow N \propto \frac{1}{\Phi_{\text{residual}}} \rightarrow \text{small value}$$

$$T \propto \Phi I_a \uparrow ; \quad E_b \propto \Phi \downarrow ; \quad \uparrow I_a = \frac{V - E_b}{R_a}$$

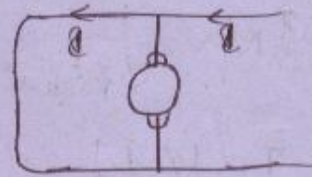
If shunt motor running under fl condi. if the field ckt open then back emf reduces, to maintain load torque<sup>const.</sup> motor will draw more  $I_a$ ,  $\therefore$  arm. wdg get damage and finally motor comes to stop.

Q. A shunt motor running at rated speed. If the arm ckt open then the motor will —

- (a). rotate with reduced speed
- (b). " " same "
- (c). " " dangerously high speed
- (d). stop. (motor would come to stop.)

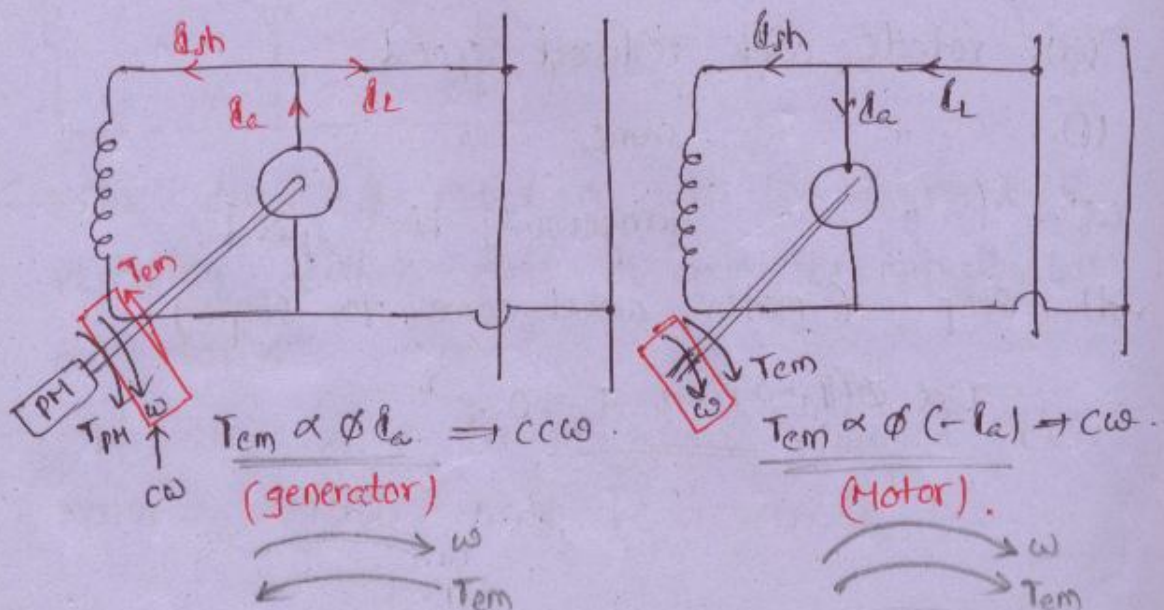
$$T \propto \Phi (I_a = 0) \Rightarrow T = 0.$$

- Q. A shunt motor running at rated speed. If its field wdg is stc'd then motor will
- Rotate with same speed.
  - " " dangerously high speed.
  - " " reduced speed.
  - would come to stop.

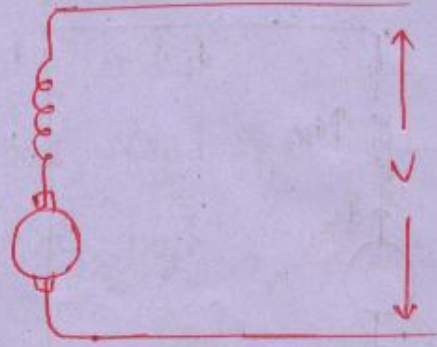


- Q. A shunt generator supplying power to the dc bus bar. If the PM fails, the m/c will behave as,

- shunt motor, rotate in the same dir.
- " " " opp. dir.
- shunt generator with reduced speed.
- m/c would come to stop.





SERIES MOTOR :

Q. A series is running at rated speed, if field ckt opens then the motor will -

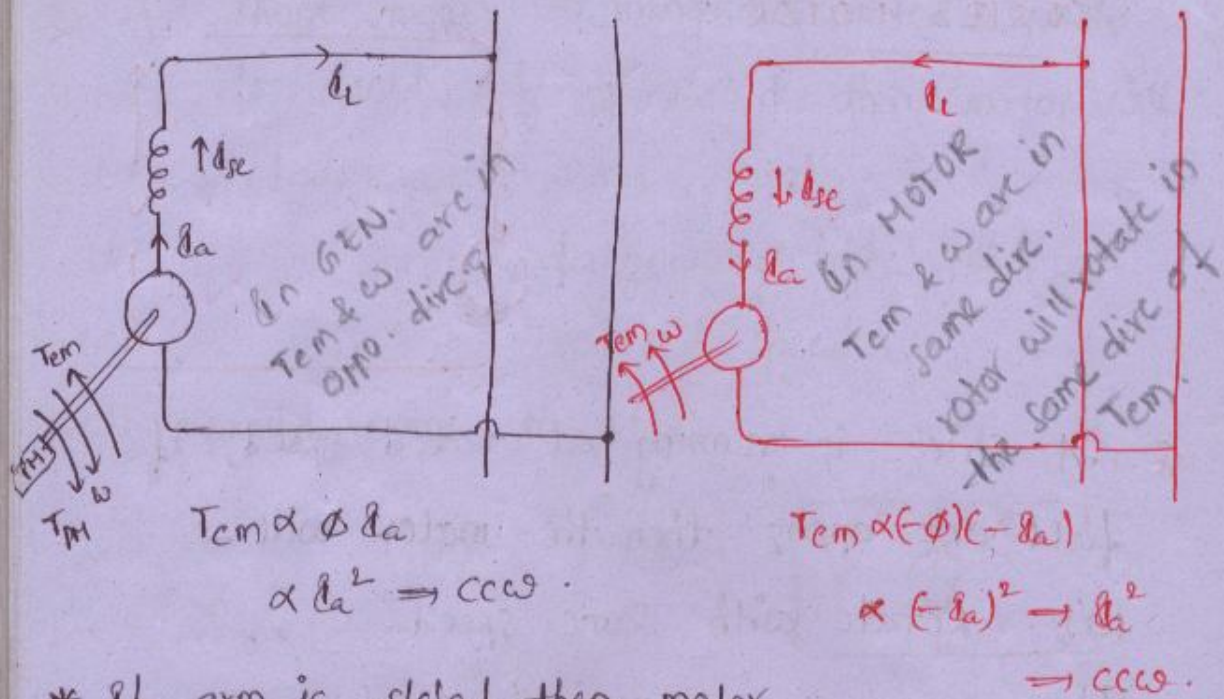
- (a). Rotate with same speed
- (b). " " reduced speed.
- (c). " " dangerously speed.
- ~~(d).~~ would comes to stop. → arm. also open

Q. A series motor running at rated speed. if its field wdg sct'd then the motor will -

- (a). Rotate with same speed
- (b). " " reduced speed
- ~~(c).~~ " " dangerously high
- (d). comes to rest.

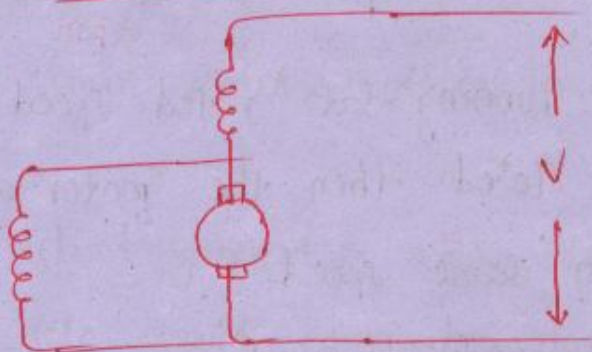
Q. A series generator supplying power to the dc bus bar. If the PM fails then the m/c will behaves as —

- (a). series motor rotate in the same dire
- ~~(b)~~ " " " opp. dire
- (c). series generator rotate at reduced speed
- (d). m/c would comes to stop.



\* If arm is staled then motor comes to rest.

### COMPOUND MOTOR:



$$N \propto \frac{1}{(\Phi_{sh} \pm \Phi_{se})} \quad \begin{array}{l} + \rightarrow \text{cumu.} \\ - \rightarrow \text{diff.} \end{array}$$

Q. A cumu. comp. motor running at rated speed. If the series field wdg opened then the motor would **come to stop**.

Q. A cumu. comp. motor running at rated speed. If the series field wdg is staled then the motor will —



- (a). Rotate with same speed  
 (b). " " reduced speed  
 (c). " " increased speed  $\uparrow N \propto \frac{1}{\Phi_{sh} + \Phi_{se}}$   
 (d). " " dangerously high  $\downarrow \Phi_{se}$   
 (e). come to stop.

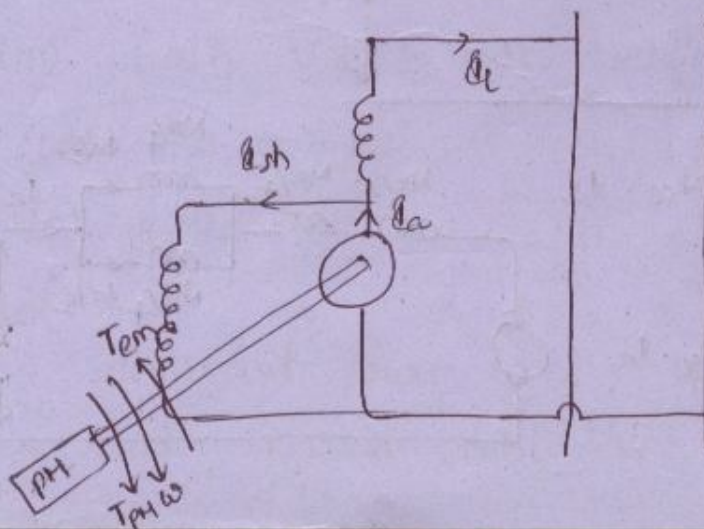
→ If it is differential comp. motor, if the series field wdg is sliced then,

$$\downarrow N \propto \frac{1}{\uparrow \Phi_{sh} - \Phi_{se}} \Rightarrow \text{Net flux } \Phi \text{ increases}$$

motor will rotate with reduced speed.

Q. A belt driven cumu. comp. generator supplying power to dc bus bar. If belt breaks then the m/c behaves as —

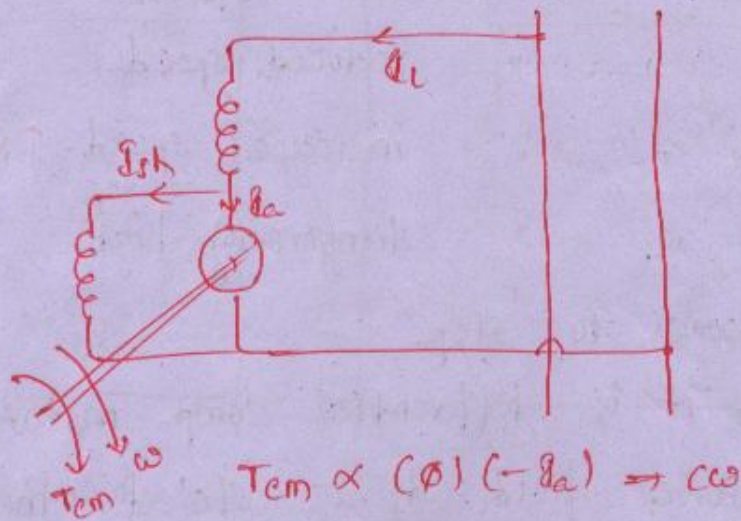
- (a). diff comp. motor, rotate in the same dire.  
 (b). " " " " the opp. dire.  
 (c). cumu. " " " the same dire.  
 (d). " " " " the opp. dire.



$$T_m \propto \Phi I_a \Rightarrow \text{ccw.}$$

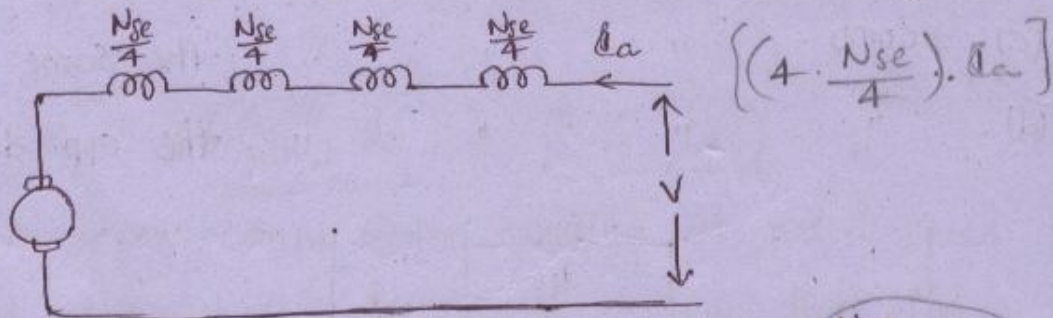
$$\Phi_{sh} > \Phi_{se} \Rightarrow \text{normally under comp. motor.}$$

$$\Phi = \Phi_{sh} + \Phi_{se}$$

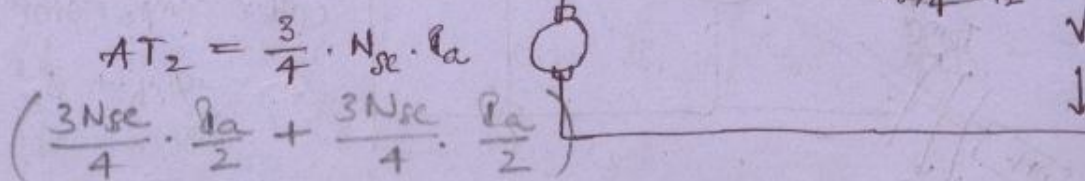


Here

Q. A series motor series field is divided into 4 groups. If all are connected in series, the speed is 1000 rpm. Then if 2 are connected in series and another 2 are connected in parallel and those are connected in series then the speed of the motor will be —?



$$\Rightarrow AT_1 = N_{se} \cdot I_a$$





$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}} \times \frac{AT_1}{AT_2}$$

$E_{b1} \approx E_{b2}$  if  $R_a + R_{se}$  is neglected

$$= \frac{AT_1}{AT_2}$$

$$= \frac{N_{se} \cdot \delta_a}{3/4 \cdot N_{se} \cdot \delta_a}$$

$$\Rightarrow N_2 = \frac{4}{3} \times 1000 \text{ rpm}$$

Q. DC shunt motor driving a const. power load. Under rated condi. motor takes rated arm. and runs at rated  $N$ . The speed and current for the following changes.

(i). Arm. terminal volt. is halved, field current unchanged.

(a). 2 pu, 0.5 pu (b). 0.5 pu, 2 pu.

(c). 1 pu, 1 pu (d). 1 pu, 0.5 pu

(ii).  $V$  is unchanged &  $\delta_f$  is halved.

(a). 2 pu, 1 pu (b). 1 pu, 2 pu

(c). 0.5 pu, 1 pu (d). 0.5 pu, 2 pu

(iii). Both  $V$  &  $\delta_f$  are halved,

(a). 1 pu, 0.5 pu (b). 1 pu, 2 pu

(c). 2 pu, 1 pu (d). 4 pu, 4 pu.

Sol:

constant power load,  $P_1 = P_2$

under rated condi.  $V_1 = 1 \text{ pu}$ ,  $I_{a1} = 1 \text{ pu}$

$$N_1 = 1 \text{ pu} \text{ \& } \delta_{f1} = 1 \text{ pu.}$$

$$(i). \quad V_2 = 0.5 \text{ pu} \text{ \& } \delta_{f2} = 1 \text{ pu.}$$

$$V_1 \delta_{a1} = V_2 \delta_{a2}$$

$$1 \times 1 = 0.5 \times \delta_{a2}$$

$$\Rightarrow \delta_{a2} = 2 \text{ pu.}$$

$$\delta_{f1} \cdot \delta_{a1} \cdot N_1 = \delta_{f2} \cdot \delta_{a2} \cdot N_2$$

$$\Rightarrow 1 \times 1 \times 1 = 1 \times 2 \times N_2$$

$$\Rightarrow N_2 = 0.5 \text{ pu}$$

$$\frac{N_2}{N_1} = \frac{V_2}{V_1} \times \frac{\delta_{f1}}{\delta_{f2}}$$

$$\Rightarrow \frac{N_2}{1} = \frac{0.5}{1} \times \frac{1}{1} = 0.5 \text{ pu.}$$

$$N_2 \text{ \& } \delta_{a2} \Rightarrow 0.5 \text{ pu \& } 2 \text{ pu.}$$

$$(ii). \quad V_2 = 1 \text{ pu}, \quad \delta_{f2} = 0.5 \text{ pu}$$

$$V_1 \delta_{a1} = V_2 \delta_{a2}$$

$$\Rightarrow 1 \times 1 = 1 \times \delta_{a2}$$

$$\Rightarrow \delta_{a2} = 1 \text{ pu.}$$

$$\delta_{f1} \cdot \delta_{a1} \cdot N_1 = \delta_{f2} \cdot \delta_{a2} \cdot N_2$$

$$\Rightarrow 1 \times 1 \times 1 = 0.5 \times 1 \times N_2$$

$$\Rightarrow 2 \text{ pu.}$$

constant power load

$$P_1 = P_2$$

$$V_1 \delta_{a1} = V_2 \delta_{a2}$$

$$N_1 T_1 = N_2 T_2$$

$$\Rightarrow \delta_{f1} \delta_{a1} \cdot N_1 = \delta_{f2} \delta_{a2} \cdot N_2$$

$$\Rightarrow \frac{N_2}{N_1} = \frac{V_2}{V_1} \times \frac{\delta_{f1}}{\delta_{f2}}$$



Q. A dc shunt motor driving a const. torque load and under rated condn. motor takes rated arm i, and runs at rated N. The speed & arm i for the following changes —

(i).  $V$  is halved,  $I_f$  is unchanged.

(a). 1 pu, 0.5 pu (b). 0.25 pu, 2 pu

(c). 1 pu, 2 pu (d). 0.5 pu, 1 pu.

(ii).  $V$  is unchanged,  $I_f$  is halved,

(a). 2 pu, 2 pu (b). 1 pu, 1 pu

(c). 0.5 pu, 0.5 pu (d). 2 pu, 0.5 pu.

(iii). Both  $V$  &  $I_f$  are halved.

(a). 1 pu, 2 pu (b). 2 pu, 1 pu

(c). 1 pu, 0.5 pu (d). 2 pu, 4 pu.

Sol:

const. torque load ie  $T_1 = T_2$

$V_1 = 1 \text{ pu}$ ,  $I_{a1} = 1 \text{ pu}$ ,  $I_{f1} = 1 \text{ pu}$  &  $N_1 = 1 \text{ pu}$ .

(i).  $V_2 = 0.5 \text{ pu}$

$I_{f2} = 1 \text{ pu}$

$$I_{f1} \cdot I_{a1} = I_{f2} \cdot I_{a2}$$

$$\Rightarrow 1 \times 1 = 1 \times I_{a2}$$

$$\Rightarrow I_{a2} = 1 \text{ pu}$$

Constant Torque Load

$$T_1 = T_2$$

$$I_{f1} \cdot I_{a1} = I_{f2} \cdot I_{a2}$$

$$\frac{N_2}{N_1} = \frac{V_2}{V_1} \times \frac{I_{f1}}{I_{f2}}$$

$$\frac{N_2}{N_1} = \frac{V_2}{V_1} \times \frac{I_{f1}}{I_{f2}}$$

$$\Rightarrow \frac{N_2}{1} = \frac{0.5}{1} \times \frac{1}{1} \Rightarrow N_2 = 0.5 \text{ pu.}$$

$$(ii). \quad V_2 = 1 \text{ pu}, \quad I_{f2} = 0.5 \text{ pu.}$$

$$I_{f1} \cdot I_{a1} = I_{a2} \cdot I_{f2}$$

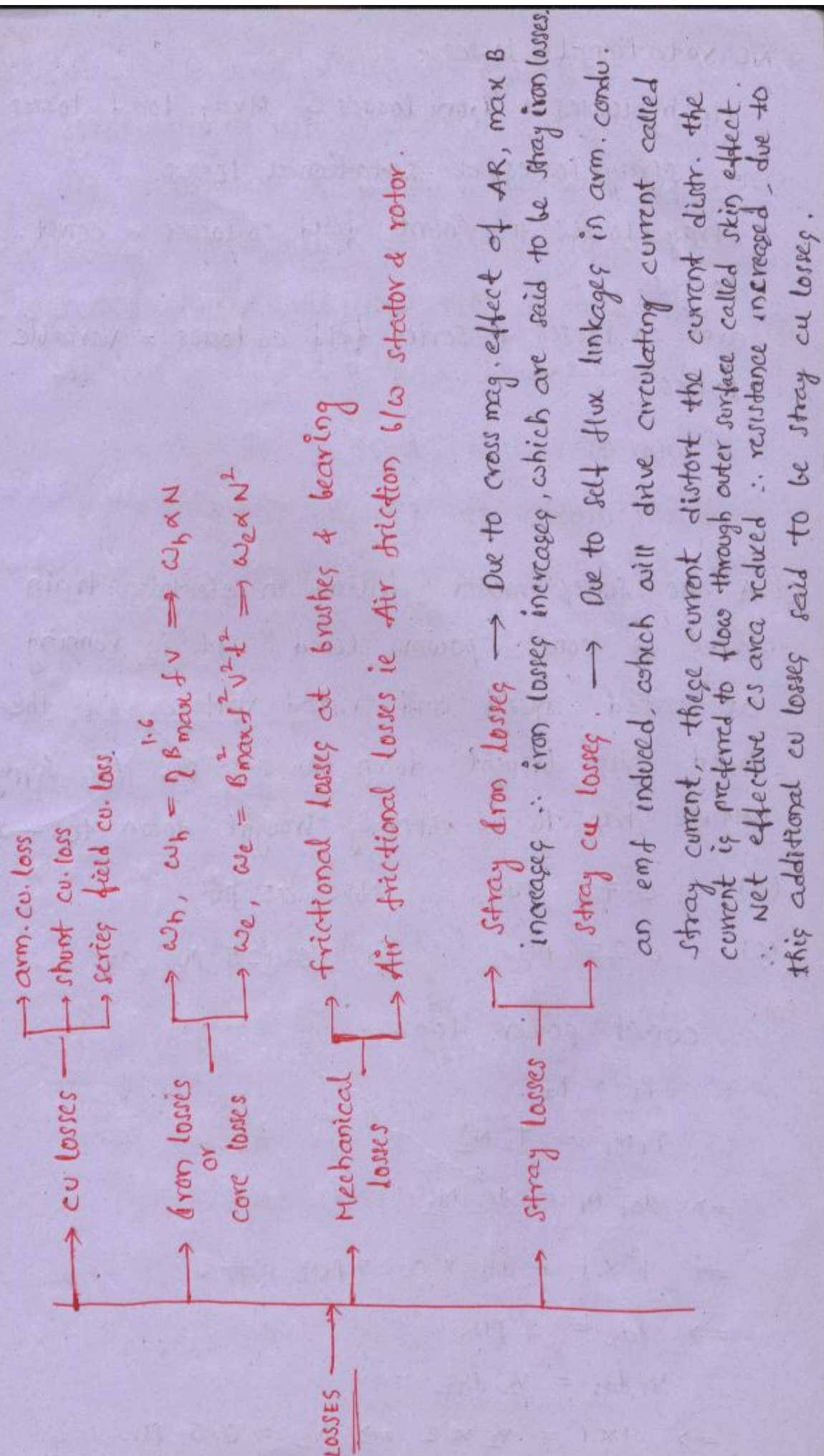
$$\rightarrow 1 \times 1 = 0.5 \times I_{a2}$$

$$\Rightarrow I_{a2} = 2 \text{ pu.}$$

$$\frac{N_2}{N_1} = \frac{V_2}{V} \times \frac{I_{f1}}{I_{f2}}$$

$$\Rightarrow \frac{N_2}{1} = \frac{1}{1} \times \frac{1}{0.5} \Rightarrow N_2 = 2 \text{ pu.}$$





NL rotational losses :

Mech. losses + Iron losses + stray load losses

= stray losses of rotational losses.

stray losses + shunt field cu losses = const. losses.

arm. cu. losses + series field cu losses = variable losses.

Q. A DC series motor driving an electric train faces a const. power load. It is running at rated speed and rated voltage. If the speed has brought down to 0.25 pu, the supply voltage has to be appr. ly brought down to. —?

(a). 0.75 pu

(b). 0.5 pu

(c). 0.25 pu

(d). 0.125 pu

Sol:

const. power load.

$$P_1 = P_2$$

$$T_1 N_1 = T_2 N_2$$

$$\Rightarrow \phi_{a1}^2 N_1 = \phi_{a2}^2 N_2$$

$$\Rightarrow 1^2 \times 1 = \phi_{a2}^2 \times 0.25 \text{ pu}$$

$$\Rightarrow \phi_{a2} = 2 \text{ pu.}$$

$$V_1 \phi_{a1} = V_2 \phi_{a2}$$

$$\Rightarrow 1 \times 1 = V_2 \times 2 \Rightarrow V_2 = 0.5 \text{ pu.}$$



Q. A 240 V DC series motor takes 40 A, when giving its rated O/p at 1500 rpm. Its resistance is  $0.3 \Omega$ . The value of resistance which must be added to obtain rated torque at 1000 rpm is — ?

- (a)  $6 \Omega$  (b)  $5.7 \Omega$  (c)  $2.2 \Omega$  (d)  $1.9 \Omega$

Sol: 240V,  $I_{a1} = 40 \text{ A}$ ,  $N_1 = 1500 \text{ rpm}$

$R_a = 0.3 \Omega$ ;  $R_e = ?$  to obtain rated torque at 1000 rpm.  $= N_2$ .

$$T_1 = T_2 \Rightarrow I_{a1}^2 = I_{a2}^2$$

$$\Rightarrow I_{a1} = I_{a2} = 40 \text{ A}$$

$$\begin{aligned} E_{b1} &= V - I_{a1} R_a \\ &= 240 - 40 \times 0.3 \\ &= 228 \text{ V} \end{aligned}$$

$$E_{b2} = V - I_{a2} (R_a + R_e)$$

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}} \times \frac{\Phi_1}{\Phi_2} = \frac{E_{b2}}{E_{b1}} \times \frac{I_{a1}}{I_{a2}} = \frac{E_{b2}}{E_{b1}}$$

$$\frac{1000}{1500} = \frac{E_{b2}}{228} \Rightarrow E_{b2} = 152$$

$$\therefore 152 = 240 - 40(0.3 + R_e)$$

$$\Rightarrow R_e = 1.9 \Omega$$

G105

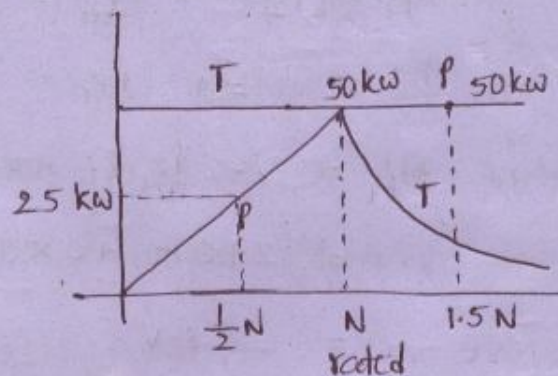
A 50 kW dc shunt motor is loaded to draw rated arm. current at any given speed when driven —

- (a). At half the rated speed by arm. volt control  
 (b). At 1.5 times rated speed by field control.

The res. power developed by motor are res. by —

- (a). 25 kW, 75 kW      (b). 25 kW, 50 kW  
 (c). 50 kW, 75 kW      (d). 50 kW, 50 kW

sol:

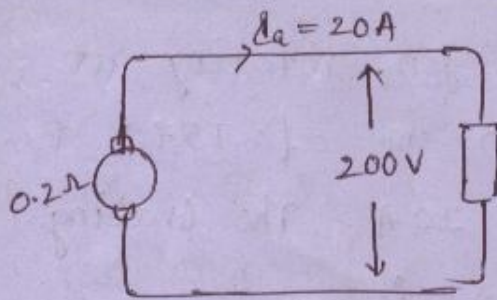


G106

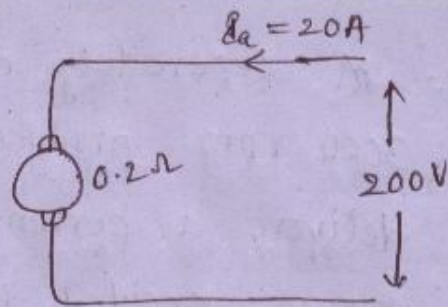
A 220V, dc m/c supplies 20 A, at 200V as a generator, the arm. resistance is  $0.2 \Omega$ . If the m/c is now operated as motor at the same terminal volt & current but with flux increased by 10%. The ratio of motor speed to generator speed is —

- (a). 0.87      (b). 0.95      (c). 0.96      (d) 1.06




 $N_g$ 

$$E_g = 200 + 20 \times 0.2 \\ = 204 \text{ V}$$


 $\phi_m = 1.1 \phi_g ; N_m$ 

$$E_m = 200 - 20 \times 0.2 \\ = 196 \text{ V}$$

$$\frac{N_m}{N_g} = \frac{E_m}{E_g} \times \frac{\phi_g}{\phi_m}$$

$$= \frac{196}{204} \times \frac{1}{1.1} = 0.87$$

DEDO  
Q.

A separately exc. dc gen. having arm. resis. of  $0.1\Omega$  supplies  $4\text{ kW}$  at a terminal voltage of  $200\text{ V}$ . If the m/c is now operated as a motor at the same terminal voltage & same arm. current with flux/pole being increased by  $10\%$ . The ratio of generator speed to motor speed will attr. by —

- (a).  $0.09$       (b).  $0.11$       (c).  $1.04$       (d).  $1.12$

Q. A separately exc. dc gen. rotating at 3000 rpm produces an emf of 157 V & delivers a current of 20 A. The braking torque excited by arm. is —

- (a) 0.17 Nm (b). 10 Nm (c). 12 Nm  
(d). 12.5 Nm

Sol:  $N = 3000 \text{ rpm}$ ,  $E = 157 \text{ V}$   
 $I_a = 20 \text{ A}$ ,  $\Rightarrow T_B = ?$

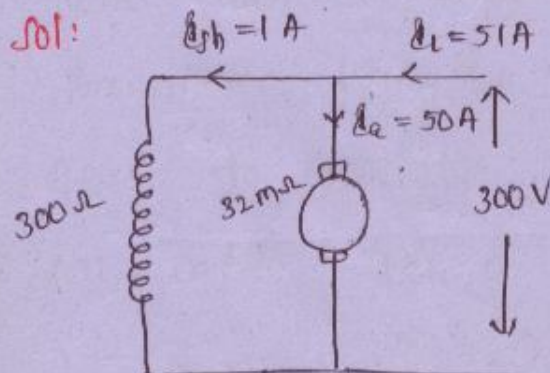
Braking torque  
(or) Electromagnetic  
torque

$$T_{em} = T_B = \frac{E_g I_a}{\omega}$$

$$= \frac{157 \times 20}{2\pi \times \frac{3000}{60}} = 10 \text{ Nm}$$

Q. A 300V, dc shunt motor draws a line current of 51 A. The arm & field resistances are 32 mΩ & 300 Ω res.ly. Assuming 1 Hp = 746 W. The mech. power developed by motor is —

- (a) 20 Hp (b) 20.1 Hp (c) 20.4 Hp  
(d). 20.5 Hp



$$E_b = V - I_a R_a$$

$$= 300 - 50 \times 32 \times 10^{-3}$$

$$= 298.4 \text{ V}$$

$$P_{mech} = E_b I_a$$

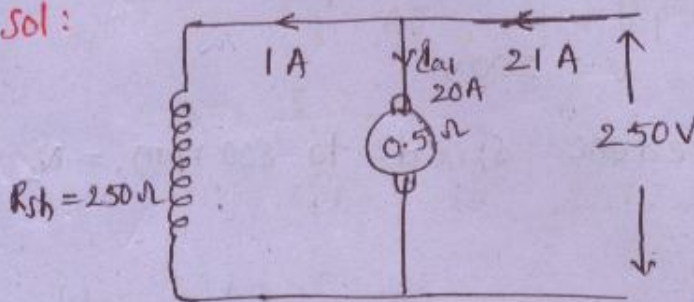
$$= 298.4 \times 50 \text{ W}$$



$$= \frac{298.4 \times 50}{746} = 20 \text{ Hp.}$$

Q. A 250 V, dc shunt motor has an arm. resistance of  $0.5 \Omega$  & field resistance of  $250 \Omega$ , when driving a const. <sup>torque</sup> load, at 600 rpm, motor draws 21 A. The new speed of the motor if an additional  $250 \Omega$  connected in the field ckt —

Sol:



$$N_1 = 600 \text{ rpm}$$

$$T_1 = T_2$$

$$I_{f1} \cdot I_{a1} = I_{f2} \cdot I_{a2}$$

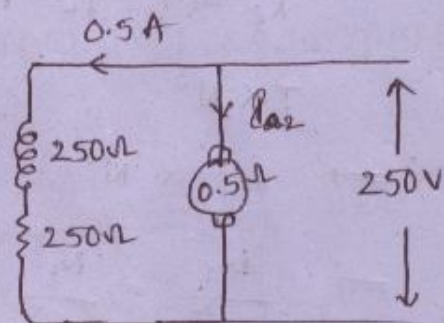
$$\Rightarrow I_{sh1} \cdot I_{a1} = I_{sh2} \cdot I_{a2}$$

$$\Rightarrow 1 \times 20 = 0.5 \times I_{a2}$$

$$\Rightarrow I_{a2} = 40 \text{ A}$$

$$E_{b1} = 250 - 20 \times 0.5$$

$$= 240 \text{ V}$$



$$N_2 = ?$$

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}} \times \frac{I_{sh1}}{I_{sh2}}$$

$$\Rightarrow \frac{N_2}{600} = \frac{230}{240} \times \frac{1}{0.5} \Rightarrow N_2 = 1150 \text{ rpm.}$$

a A dc series motor driving a fan load when the load torque is proportional to  $N^3$ . The resistance of arm & field is  $1\Omega$  and motor takes  $10A$  at  $1000$  rpm when operating from  $200V$ . the value of resistance inserted in series with arm. to reduce arm. speed  $800$  rpm.

Sol:  $T \propto N^3$ ,  $R_a + R_{se} = 1\Omega$ ,  $I_{a1} = 10A$

$N_1 = 1000$  rpm.  $V = 200V$

$R_e = ?$  to reduce speed to  $800$  rpm.  $= N_2$

$T \propto N^3$

$\Rightarrow I_a^2 \propto N^3$

$\Rightarrow \frac{I_{a1}^2}{I_{a2}^2} = \frac{N_1^3}{N_2^3}$

$\Rightarrow I_{a2} = \sqrt{\frac{800^3}{1000^3}} \times 10$   
 $= 7.15 A$

$E_{b1} = 200 - 10 \times 1 = 190V$

$E_{b2} = 200 - 7.15(1 + R_e)$

$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}} \times \frac{I_{a1}}{I_{a2}}$

$\Rightarrow \frac{800}{1000} = \frac{E_{b2}}{190} \times \frac{10}{7.15}$

$\Rightarrow E_{b2} = 108.76V$



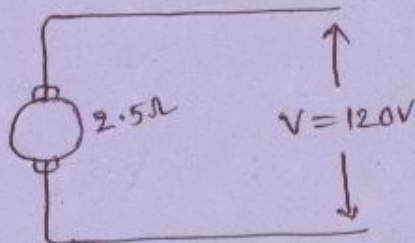
$$\Rightarrow 108.76 = 200 - 7.15(1 + R_e)$$

$$\Rightarrow R_e = 11.74 \Omega$$

<sup>600</sup>  
Q A permanent magnet dc commutator motor has NL speed of 6000 rpm, when connected to 120 V dc supply, the arm resistance is  $2.5 \Omega$  and other losses may be neglected. The speed of the motor if supply voltage of 60V developing a torque 0.5 Nm is —

- (a). 3000 rpm (b). 2673 rpm (c) 2836 rpm  
(d) 5346 rpm.

Sol:



$$N_1 = 6000 \text{ rpm}$$

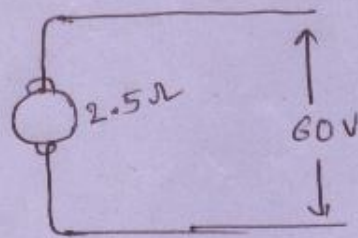
$$E_{b1} = V = 120 \text{ V}$$

$\therefore$  NL losses neglected  $\therefore I_a = 0$

$$E_{b1} = \frac{\Phi Z N}{60} \left( \frac{P}{A} \right) = 120$$

$$\Rightarrow \frac{\Phi Z}{60} \cdot \frac{P}{A} = 0.02$$

$$\Rightarrow \frac{\Phi Z P}{A} = 60 \times 0.02 = 1.2$$



$$T = 0.5 \text{ Nm}, N_2 = ?$$

$$T = \frac{E_{b2} \cdot I_{a2}}{\omega}$$

$$= \frac{\frac{\Phi Z N_2}{60} \times \frac{P}{A} \times I_{a2}}{2\pi \frac{N_2}{60}}$$

$$= \frac{\Phi Z P}{2\pi A} \cdot I_{a2}$$

$$\Rightarrow 0.5 = \frac{1}{2\pi} (1.2) I_{a2}$$

$$\Rightarrow I_{a2} = 2.61 \text{ A}$$

$$E_{b2} = V - I_{a2} \cdot R_a$$

$$= 60 - 2.61 \times 2.5$$

$$= 53.47 \text{ V}$$

$$\frac{N_2}{N_1} = \frac{E_{b2}}{E_{b1}} \times \frac{\phi_1}{\phi_2} \quad [\because \phi_1 = \phi_2]$$

$$\Rightarrow \frac{N_2}{6000} = \frac{53.47}{120} \Rightarrow N_2 = 2673 \text{ rpm.}$$





Q. A 230 V, 250 rpm, 100 A separately exc. dc motor has an arm resistance of  $0.5 \Omega$ . The motor is connected to 230 V dc supply and rated dc voltage applied to the field wdg. It is driving a load whose speed torque char. given by  $T_L = 500 - 10\omega$   $\omega$  - is the rotational speed expressed in rad/sec. and  $T_L$  = load torque in Nm. find ss speed at which the motor drive the load and arm. current drawn by it from the source, neglect rotational losses of m/c.

Sol:

$$230 \text{ V, } 250 \text{ rpm, } 100 \text{ A, } R_a = 0.5 \Omega$$

$$V = 230 \text{ V} \quad \text{Sep. exc. dc motor.}$$

$$T_L = 500 - 10\omega \Rightarrow N = ?, I_a = ?$$

At rated condition ie 250 rpm,

$$E_b = 230 - 100 \times 0.5$$

$$= 180 \text{ V}$$

$$\Rightarrow E_b = K\omega$$

$$\Rightarrow K = \frac{E_b}{\omega}$$

$$= \frac{180}{2\pi \times \frac{250}{60}} = 6.87 \text{ V/rad/sec} = \frac{E_b I_a}{\omega} = \frac{K\omega \cdot I_a}{\omega} = K \cdot I_a$$

for Sep. exc. & shunt  
m/c

$$E_b = K\omega$$

$$T = K I_a$$

Let  
 $\omega_m$  = Actual speed of  
 the motor.

$$k = \frac{E_b}{\omega} = V / \text{rad/sec}$$

$$k = \frac{T}{I_a} = \text{Nm/Amp.}$$

$$T_{em} = \frac{E_b I_a}{\omega_m}$$

$$= \frac{k \omega_m \cdot I_a}{\omega_m} = k \cdot I_a$$

$$T_{em} = \underbrace{j \frac{d\omega}{dt}}_{=0} + \underbrace{B\omega}_{=0} + T_L$$

$$= k \left[ \frac{V - E_b}{R_a} \right]$$

$$T_{em} = k \left[ \frac{V - k\omega_m}{R_a} \right] = T_L = 500 - 10\omega$$

$$\Rightarrow 6.87 \left[ \frac{230 - 6.87 \omega_m}{0.5} \right] = 500 - 10\omega_m$$

$$\Rightarrow \omega_m = 31.5 \text{ rad/sec}$$

$$= 31.5 \times \frac{60}{2\pi}$$

$$= 301 \text{ rpm.}$$

$$I_a = \left[ \frac{V - E_b}{R_a} \right]$$

$$= \frac{230 - 6.87 \times 31.5}{0.5}$$

$$= 26.9 \text{ A}$$



Q. A 250V dc series motor has arm & series field resistance of  $0.25 \Omega$ ,  $0.15 \Omega$  res. The current for developing 80 Nm at 1200 rpm is —

(a).  $86.4 \text{ A}$

(b).  $43.2 \text{ A}$

(c).  $(20+1) \text{ A}$

(d).  $50 \text{ A}$

Sol:

250V,  $R_a = 0.25 \Omega$ ,  $R_{se} = 0.15 \Omega$

$I_a = ?$  for  $T = 80 \text{ Nm}$ ,  $N = 1200 \text{ rpm}$ .

$$T_e = \frac{E_b I_a}{\omega}$$

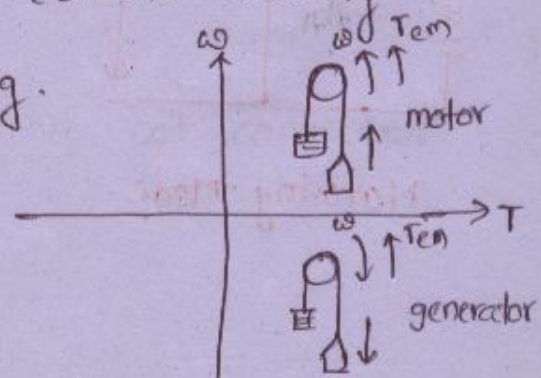
$$\Rightarrow T_e \cdot \omega = E_b \cdot I_a$$

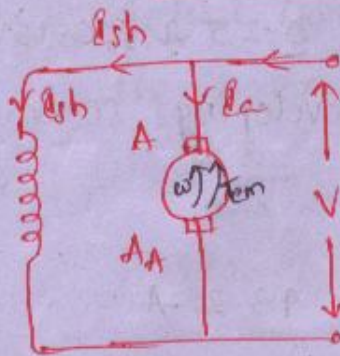
$$\Rightarrow 80 \times 2\pi \times \frac{1200}{60} = (250 - I_a \times 0.4) \cdot I_a$$

$$\Rightarrow I_a = 43.2 \text{ A}$$

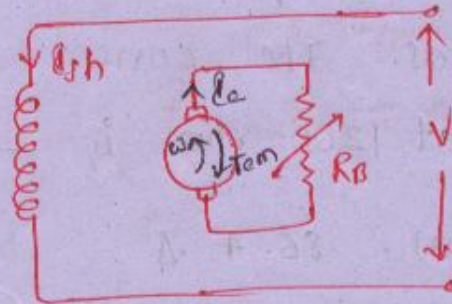
### ELECTRIC BRAKING:

1. Dynamic braking (or) Resistance (or) Rheostatic braking.
2. plugging (or) Reverse current braking
3. Regenerative braking.

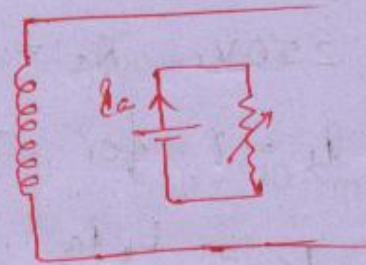
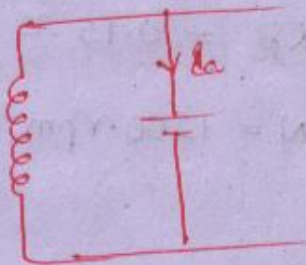


DYNAMIC BRAKING :

Motoring Mode



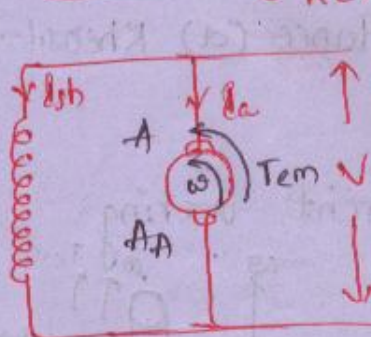
Braking mode



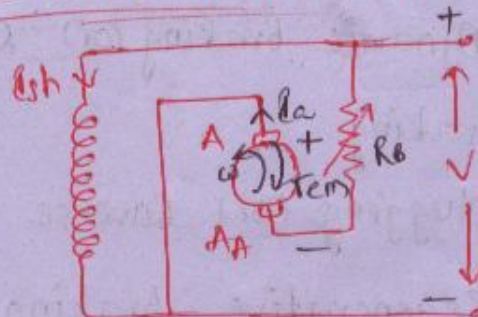
Braking torque  $T_B = \frac{E_b \cdot I_a}{\omega}$

$$= \frac{\frac{\Phi Z N}{60} \times \frac{P}{A} \cdot I_a}{\frac{2\pi N}{60}}$$

$$\propto \Phi I_a$$

PLUGGING :REVERSE CURRENT BRAKING :-

Motoring Mode



Plugging mode  
when current reverses, so that torque also reverses

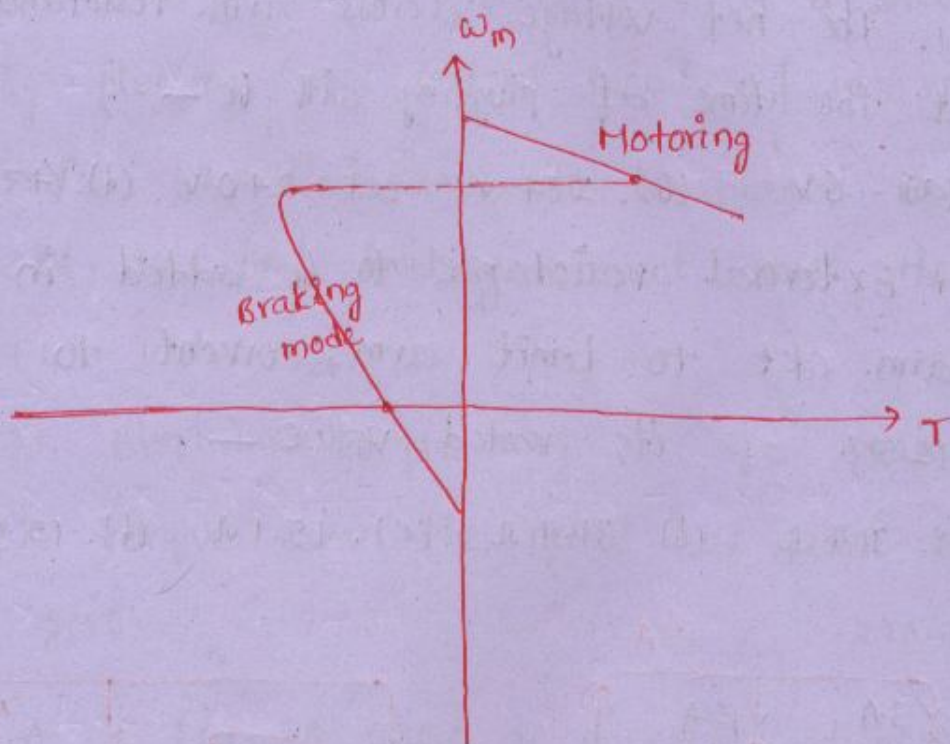


$R_B$  is inserted to limit current during plugging.  $I_a = \frac{V + E_b}{R_a + R_B} \rightarrow$  current

during plugging.

At standstill,  $N=0, \Rightarrow E_b=0$

$$\Rightarrow I_a = \frac{V}{R_a + R_B}$$



Under this method, braking torque is also available when motor is stopped. Then supply has to be disconnected and mech. brakes are applied.

Otherwise if supply is not connected properly due to

plugging is faster compared with dynamic braking.

Q. A 240 V dc shunt motor draws 15 A while supplying the rated load at rated speed of 80 rad/sec. The arm. resistance is  $0.5 \Omega$  & field wdg resistance is  $80 \Omega$ .

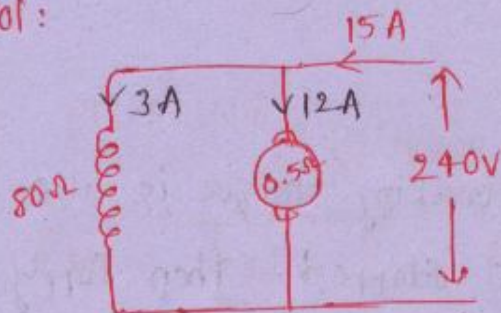
(1). The net voltage across arm. resistance at the time of plugging will be —

- (a). 6 V (b). 234 V (c). 240 V (d).  $(470+4)$  V

(2). External resistance to be added in arm. ckt to limit arm. current to 125% of its rated value —

- (a).  $31.1 \Omega$  (b)  $31.9 \Omega$  (c).  $15.1 \Omega$  (d).  $15.9 \Omega$

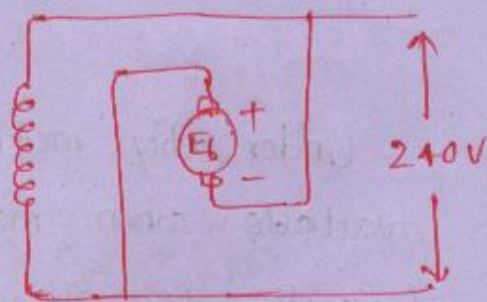
Sol:



During motoring

$$E_b = 240 - 12 \times 0.5$$

$$= 234 \text{ V}$$



During plugging

$$\therefore \text{Net voltage across the arm, \& arm. resistance}$$

$$= 240 + 234$$

$$=$$



$$I_a = 12 \times 12.5$$

Q. A 220V, 970, 100A dc shunt motor has an arm. resistance of  $0.05 \Omega$ , it is braked by plugging from initial speed of 1000 rpm.

calc. (1). Resistance to be placed in arm. ckt to limit braking current twice the FL value — ?

1.16

(2). Braking torque — ?

423.3 Nm

(3). Torque when the speed has fallen to zero

210.7 Nm

Q. A 10 kW, 4 pole, dc generator develop an emf of 200V at 1500 rpm, the arm. has lap connected wdg. The avg. flux density over a pole pitch is 0.9 T.

If the length and dia. of arm are 0.25m & 0.2m res. ly. Then the no. of arm. turns required will be — ?

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$$\phi_{av} = B_{av} \times \text{Area under each pole}$$

$$= B_{av} \times \frac{\pi DL}{p}$$

$$E_g = \frac{\phi Z N}{60} \cdot \frac{p}{A} = 200V$$

$$T = \frac{Z}{2}$$

